Lepton Flavor Violation in charged leptons: the next challenge in flavor physics

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Introduction: the SM as an effective theory

Flavor symmetry breaking in the quark sector

Minimal Flavor Violation in the lepton sector

Lepton Flavor symmetry breaking in GUTs

LFV in explicit SUSY models

Conclusions

### *Introduction: the SM as an effective theory*

The effects of new physics below the electroweak scale can be described in full generality by considering the SM as (the leading part) of an *effective field theory* :

 $\frac{1}{\Lambda_{LN}} (L_L^{T})^i g_{LL}^{ik} L_L^k \phi^T \phi$ 

 $(v_L^{\mathrm{T}})^i m_{\nu}^{ik} v_L^k$ 

### Introduction: the SM as an effective theory

The effects of new physics below the electroweak scale can be described in full generality by considering the SM as (the leading part) of an *effective field theory* :

$$\mathscr{L}_{eff} = \mathscr{L}_{gauge}(A_k, \psi_i) + \mathscr{L}_{Higgs}(\phi, A_k, \psi_i; Y, v) + \sum_{d \ge 5} \frac{C_n}{\Lambda^{d-4}} O_n^{-d}(\phi, A_k, \psi_i)$$
No neutrino masses
(& mixing angles)
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completely equivalent (but more general) of the usual see-saw mechanism  $[M_{VR} \sim \Lambda_{LN} \gg \langle \phi \rangle]$ 



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$$\mathscr{L}_{eff} = \mathscr{L}_{gauge}(A_k, \psi_i) + \mathscr{L}_{Higgs}(\phi, A_k, \psi_i; Y, \nu) + \sum_{d \ge 5} \frac{c_n}{\Lambda^{d-4}} O_n^{d}(\phi, A_k, \psi_i)$$

The dim-5 operator responsible for neutrino masses is quite special since it violates *lepton number* 

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Natural to assume that this symmetry of the pure SM Lagrangian is broken at very high scales

If  $\Lambda_{LN} \sim 10^{15}$  GeV some  $g_{LL}^{ik}$  can be O(1)  $\Rightarrow$  *natural* effective theory [no fine-tuning for the smallness of m<sub>v</sub>] *G. Isidori* – *LFV: the next challenge* 

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If  $\Lambda_{LN} \sim 10^{15}$  GeV some  $g_{LL}^{ik}$  can be O(1)  $\Rightarrow$  *natural* effective theory [no fine-tuning for the smallness of m<sub>v</sub>]  $\Lambda_{LN}$  cannot be the only scale of NP: new degrees of freedom in the TeV range are necessary to stabilize the Higgs sector  $\Rightarrow$  NP within the reach of the LHC

•  $\Lambda_{eff} \sim 1-10$  TeV is the natural scale of NP for processes which do not violate the total barion or lepton number

• In the case of flavor-changing processes, this is possible only if flavor-changing couplings have a non-trivial (*minimal*) form (*the lesson of quark flavor physics*)

some general conclusions about the size of LFV

# *Flavor symmetry breaking in the quark sector*

The consistency of the various experimental constraints appearing in CKM fits and the absence of significant deviations from SM in rare decays, such as  $B \rightarrow X_s \gamma(l^+l^-)$ , ... are a clear evidence that the SM is very successful in describing quark-flavor mixing.



↓

New physics effects in quark-flavor mixing can only appear as small corrections to the leading CKM mechanism

## *Flavor symmetry breaking in the quark sector*

The best way to quantify this success is to derive bounds on the scale of new physics:

$$M(B_{d}-\overline{B}_{d}) \sim \frac{(y_{t}V_{tb}^{*}V_{td})^{2}}{16 \pi^{2} M_{W}^{2}} + \left(c_{NP}\frac{1}{\Lambda^{2}}\right)^{2}$$

contribution of the new heavy degrees of freedom



MFV = <u>Minimal Flavor Violation</u> hypothesis

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The MFV hypothesis can be formulated in a general form as the assumption of a well-defined <u>symmetry</u> + <u>symmetry-breaking structure</u> in the flavor sector of the effective theory:

- <u>Flavor symmetry:</u>  $U(3)^{5} = SU(3)_{Q} \times SU(3)_{U} \times SU(3)_{D} \times ...$ [global symmetry of the SM gauge sector]
- <u>Symmetry-breaking terms:</u>  $Y_D \sim \overline{3}_Q \times 3_D$   $Y_U \sim \overline{3}_Q \times 3_U$ [quark Yukawa couplings]



 $\mathscr{L}_{q-Yukawa} = \overline{Q}_L Y_D D_R H + \overline{Q}_L Y_U U_R H_c + h.c.$ 

 $Y_D = \operatorname{diag}(y_d, y_s, y_b)$   $Y_U = (V_{ckm})^+ \times \operatorname{diag}(y_u, y_c, y_t)$ 

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 $MFV = Y_{U,D}$  are the only irreducible breaking sources of the flavor symmetry

New physics effects in flavor-changing processes naturally suppressed by the CKM matrix (as in SM) ⇒ Flavor observables do not exclude NP the TeV range.

## *Minimal Flavor Violation in the lepton sector*

Do we need a MFV hypothesis also in the lepton sector ?

A severe lepton-FCNC problem exists:

$$\mathscr{L}_{eff} \subset \frac{c_{\mu e}}{\Lambda^2} \overline{e}_L \sigma^{\mu\nu} \mu_R \phi F_{\mu\nu} \rightarrow \frac{\Lambda > 10^5 \,\text{TeV} \times (c_{\mu e})^{1/2}}{\text{from BR}(\mu \to e\gamma)^{exp} < 1.2 \times 10^{-11}}$$

However, in the lepton sector is not so easy to identify the irreducible sources of (lepton) flavor symmetry breaking.

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<u>extra assumptions needed</u> in order to define an effective theory approach similar to the quark sector The game become interesting when these extra assumptions leads to predictions on other observables (in particular FCNCs)  $\Rightarrow$  <u>testable hypotheses about the irreducible</u> <u>sources of LF breaking independent from dynamical details</u> <u>Cirigliano, Grinstein,</u> <u>G.I., Wise, '05</u>

<u>1<sup>st</sup> assumption (very natural)</u>

Decoupling of the U(1)<sub>L</sub> breaking [Lepton Number] - associated to some high scale  $[\Lambda_{LN} \gg \text{TeV}]$  - and the SU(3)<sub>L<sub>L</sub></sub> breaking [Lepton Flavor]  $\Rightarrow$  small neutrino masses with *natural* [ $g_v \sim O(1)$ ] flavor-violating couplings

$$\frac{1}{\Lambda_{\rm LN}} (L_L^{\rm T})^i g_V^{ik} L_L^k \phi^{\rm T} \phi$$

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Decoupling of U(1)<sub>L</sub> and SU(3)<sub>L<sub>1</sub></sub> breaking  $\Rightarrow g_{\nu} \sim O(1), \Lambda_{LN} \gg TeV$ 

<u>2<sup>nd</sup> assumption</u> (more model dependent) The effective neutrino couplings (masses + mixing) allow to determine completely the flavor-breaking structures



irreducible [ $g_v \sim 6 \text{ of } SU(3)_{L_L}$ ]

no further assumption needed

$$m_v = (U_{PMNS}) m_v^{diag} U_{PMNS} \longrightarrow \frac{g_v v^2}{\Lambda_{LN}}$$

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These predictive M(L)FV schemes are useful <u>working hypotheses to investigate</u> <u>some general properties of FCNC in the lepton sector</u> [ link between neutrino masses (& mixing) and lepton-flavor violating rare decays ]

Much more freedom/uncertainty with respect to the quark case because of

★ the overall scale

 $\bigstar$  the value of  $s_{13}$  ,  $\delta$  and the *spectrum ordering*:



★ the two scenarios

but some general phenomenological conclusions can still be obtained:

If the scale of  $U(1)_L$  breaking  $(M_R \text{ or } \Lambda_{LN})$  is sufficiently high, we should observe soon  $\mu \rightarrow e\gamma$  [general conclusion, almost independent of the MLFV hypothesis]:

 $M_R \ge 10^{12} \,\text{GeV} \times (\Lambda / 10 \,\text{TeV})^2 \qquad \longleftrightarrow \qquad B(\mu \rightarrow e\gamma) \ge 10^{-13}$ 

$$B(\mu \rightarrow e\gamma) \approx 10^{-13} \left[ \frac{10 \text{ TeV}}{\Lambda} \right]^4 \left[ \frac{M_R}{10^{12} \text{ GeV}} \right]^2$$

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The MLFV hypothesis implies a clear pattern for FCNC ratios  $B(\tau \rightarrow \mu \gamma) : B(\tau \rightarrow e \gamma) : B(\mu \rightarrow e \gamma) \sim [500 - 10] : 1 : 1$  [dictated by PMNS & m<sub>v</sub>] According to this scaling,  $\tau \rightarrow \mu \gamma$  is <u>unlikely to be seen</u>, especially if  $\theta_{13}$  is large

Relevant effective ops. for the radiative LFV decays:

$$\overline{L}_{L}^{i} Y_{v}^{+} Y_{v} Y_{e} \sigma^{\mu\nu} e_{R}^{j} F^{\mu\nu}$$
or
$$\overline{L}_{L}^{i} g_{v}^{+} g_{v} Y_{e} \sigma^{\mu\nu} e_{R}^{j} F^{\mu\nu}$$

N.B.: hierarchical structure quite similar in the two minimal schemes [with or without right-handed neutrinos]



Expected sensitivities:

BR( $\mu \rightarrow e\gamma$ ) ~10<sup>-13</sup> [MEG]

BR( $\tau \rightarrow \mu \gamma$ ) ~ 10<sup>-9</sup> [Super-B ?]

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In the case of degenerate  $M_R$  with the inclusion of CPV phases in the Yukawas the observed matter-antimatter asymmetry of the universe can be generated via <u>leptogenesis</u> [for natural values of the free parameters, especially if  $M_R$  is high]

> Cirigliano, GI, Porretti, '06 Branco et al. '06 De Simone, GI, Masina , Riotto, '08

The observed matter-antimatter asymmetry of the universe can be generated via leptogenesis [for very natural values of the free parameters, especially if  $M_R$  is high]:



<u>No need</u> to invoke non-trivial right-handed flavour structures and/or new CPV phase beyond the Yukawas to explain the matter-antimatter asymmetry: <u>the MFV scheme is phenomenologically consistent</u>

## *Lepton Flavor Symmetry breaking in Grand Unified Theories*

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<u>No!</u> [at least in the most pessimistic interpretation of MQFV+MLFV]:

within GUTs <u>quarks & leptons</u> are part of the <u>same multiplets</u>  $\Rightarrow$  we cannot avoid some contamination between quark & flavour mixing terms.

## Lepton Flavor Symmetry breaking in Grand Unified Theories

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E.g.: SU(5)<sub>gauge</sub> -- the standard GUT prototype

Cirigliano, Grinstein, G.I., Wise, '06

<u>Matter fields:</u>  $\Psi[\underline{5}] \subset L_L$ ,  $d_R^c$  $\chi[10] \subset Q_L$ ,  $u_R^c$ ,  $e_R^c$  $N[1] \subset V_R$ 

<u>Maximal flavour group:</u> [allowed by the gauge interaction]

 $U(3)_{\psi} \times U(3)_{\chi} \times U(3)_{N}$ 

The minimal GUT Yukawa interaction:

$$\mathscr{L}_{Y-GUT} = Y_D \psi^T \chi H_5 + Y_U \chi^T \chi H_5 + Y_V N^T \psi H_5$$
  
same Yukawa coupling for down quarks &  
charged lepton [bottom-tau unification]

#### Matter fields:

The minimal GUT Yukawa interaction:

When constructing the effective operators which contribute to rare processes we cannot forbid the appearance of

- $Y_D \& Y_U$  (hence the CKM matrix) in the charged-lepton sector
- $Y_{v}$  (hence the PMNS matrix) in the quark sector

 $m_v = \frac{\boldsymbol{Y}_v^{-1} \boldsymbol{Y}_v^{-1} \boldsymbol{V}^2}{M}$ 

#### Matter fields:

The minimal GUT Yukawa interaction:

 $\Psi [\underline{5}] \subset L_L, d_R^c$   $\chi [10] \subset Q_L, u_R^c, e_R^c$   $N [1] \subset V_R$   $\mathscr{L}_{Y-GUT} = Y_D \psi^T \chi H_{\underline{5}} + Y_U \chi^T \chi H_{\underline{5}}$   $+ Y_V N^T \psi H_{\underline{5}}$ 

 $M_{\rm R} > 10^{12} \, {\rm GeV}$ 

When constructing the effective operators which contribute to rare processes we cannot forbid the appearance of

•  $Y_D \& Y_U$  (hence the CKM matrix) in the charged-lepton sector

•  $Y_v$  (hence the PMNS matrix) in the quark sector

Depending on the value of  $M_{\rm R}$  [~ normalization of  $Y_{\rm v}$ ] one of this two non-MFV effects is relevant

$$M_{\rm R} < 10^{12} \, {\rm GeV}$$

Non-MFV in charged leptons  $[B(\tau \rightarrow \mu \gamma)/B(\mu \rightarrow e \gamma) \text{ enhancement}]$  Non-MFV effects in the quark sector [possible interesting effects in  $3\rightarrow 2$  transitions]

#### $\mu \rightarrow e \gamma \text{ vs. } \tau \rightarrow \mu(e) \gamma$

One of the most interesting consequences of flavour-mixing in GUTs is the fact that LFV rates cannot be arbitrarily suppressed by lowering  $M_R$ :



#### $\mu \rightarrow e \gamma \text{ vs. } \tau \rightarrow \mu(e) \gamma$

One of the most interesting consequences of flavour-mixing in GUTs is the fact that LFV rates cannot be arbitrarily suppressed by lowering  $M_{\rm R}$ :

 $A(\mathbf{l}_{i} \rightarrow \mathbf{l}_{i} \gamma) = a \left[Y_{e} Y_{v}^{+} Y_{v}\right]_{ij} + b \left[Y_{U}^{+} Y_{U} Y_{D}\right]_{ij}$ PMNS mixing structure [MLFV], dominant if  $M_P > 10^{12} \text{ GeV} \implies B(\mu \rightarrow e\gamma) \sim 10^{-13} (M_P / 10^{12} \text{GeV}) (\Lambda / 10 \text{ TeV})^4$ <u>CKM mixing structure</u> [~ Barbieri-Hall-Strumia '95] dominant if  $M_R < 10^{12} \text{ GeV} \implies B(\mu \rightarrow e\gamma) \sim 10^{-13} (\Lambda/10 \text{ TeV})^4$ 

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$$A(1_{i} \rightarrow 1_{j} \gamma) = a [Y_{e} Y_{v}^{+} Y_{v}]_{ij} + b [Y_{v}^{+} Y_{v} Y_{D}]_{ij}$$

$$PMNS \text{ mixing structure [MLFV],}$$

$$dominant \text{ if } M_{R} > 10^{12} \text{ GeV} \Rightarrow B(\mu \rightarrow e\gamma) \sim 10^{-13} (M_{R}/10^{12} \text{GeV}) (\Lambda/10 \text{ TeV})^{4}$$

$$CKM \text{ mixing structure } [\sim \text{ Barbieri-Hall-Strumia '95}]$$

$$dominant \text{ if } M_{R} < 10^{12} \text{ GeV} \Rightarrow B(\mu \rightarrow e\gamma) \sim 10^{-13} (\Lambda/10 \text{ TeV})^{4}$$

The search for  $\tau \rightarrow \mu(e) \gamma$  at B and super-B factories becomes very interesting  $\Rightarrow$  best tool to discriminate the two scenarios :

$$B(\tau \rightarrow \mu \gamma): B(\tau \rightarrow e \gamma): B(\mu \rightarrow e \gamma) \sim \lambda^{-6}: \lambda^{-4}: 1 \sim 10^4: 500: 1^{-4}$$

 $B(\tau \rightarrow \mu \gamma): B(\tau \rightarrow e \gamma): B(\mu \rightarrow e \gamma) \sim [500-10]:1:1$ 

# *LFV in SUSY models*

The main features emerging from the general effective-theory approach are naturally realized within the popular (and well motivated) SUSY extensions of the SM.

Two main scenarios [close correspondence with the general EFT approach]:

#### MSSM – GUT

Barbieri, Hall '94; Hisano *et al.* '95 Buchmuller *et al.* '99; Ellis *et al.* '00 Lavignac *et al.* '01; Masiero *et al.* '03 Ciuchini *et al.* '07 + <u>many others</u>

### $MSSM + heavy N_R$

Borzumati, Masiero '86; Hisano *et al.* '95 Davidson, Ibarra '01; Masina, Savoy, '03 Petcov *et al.* '05; Calibbi *et al.* '05 Herrero *et al.* '05-'08 + <u>many others</u>

Two *special* [model-dependent] features:

- If the dynamical mechanism of supersymmetry breaking occurs below the GUT scale, we can conceive specific scenarios [gauge mediation] where quark and lepton flavor sectors decouple completely ⇒ no observable LFV rates
- Two Higgs doublets  $\Rightarrow$  key role played by  $\tan\beta = \langle H_U \rangle / \langle H_D \rangle$  & possible sizable Higgs-mediated LFV amplitudes in  $\tau$  decays.

E.g. n.1:  $\tau \rightarrow \mu \gamma$  vs.  $\mu \rightarrow e \gamma$  in MSSM + heavy  $N_R$  [no GUT constraints]



### E.g. n.2: Higgs-mediated $\tau \rightarrow \mu \gamma$ vs. non-radiative $\tau$ decays at large tan $\beta$

Even in the most favourable scenario for Higgs-mediated amplitudes (sparticles decoupling regime) – the radiative mode is likely to dominate



m<sub>H</sub>

Paradisi '05

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E.g. n.3: The link between  $(g-2)_{\mu}$  and  $\mu \rightarrow e\gamma$ 

Effective ops. contributing to  $(g-2)_{\mu}$  and  $\mu \rightarrow e\gamma$  are very similar:



(same tanb enhancement, same dep. on slepton masses) only the flavor structure distinguish them

$$M_R \sim 10^{12} \text{ GeV} \implies (\delta_{LL})_{12} \sim 10^{-4}$$

No constraints from B physicsWith B physics constraints



G.I., Mescia, Paradisi, Temes, '07





Using a generic "minimalistic" EFT approach:

- $\mu \rightarrow e\gamma$  is likely to be seen at MEG [in most realistic scenarios]
- The observation of  $\tau \rightarrow \mu \gamma$  at super-B is not guaranteed, but its search at the 10<sup>-9</sup> level is a unique tool to discriminate GUT models