

SEE-SAW



LHC

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Bajc, G. S. hep-ph/0612029

Bajc, Nemevšek, G.S.,  
yesterday

•  $M_\nu \neq 0, \theta_e \neq 0$

$l = \begin{pmatrix} \nu \\ e \end{pmatrix}, \Phi = \begin{pmatrix} \psi^+ \\ \varphi_0 \end{pmatrix}$

$M_\nu \leq 10^{-1} \text{eV}$

Weinberg 75

• SM

•  $\mathcal{L}_\nu(\text{eff}) = \gamma_{\text{eff}} \frac{l c l \Phi \Phi}{M_\nu}$

neutrinos:  $m_\nu \approx \gamma_{\text{eff}} \frac{M_W^2}{M_\nu}$

$M_\nu \gg M_W \Rightarrow$

charged fermions }

$m_f \approx \gamma_f M_W$

$m_\nu \ll m_f$

$(M_\nu \leq 10^{14} \text{GeV})$

$\gamma_{\text{eff}} = ? \quad M_\nu = ? \quad \text{NO predictions } m_\nu, \theta_e$

SM: no predictions  $m_f, \theta_e$

NO PROBLEM in SM

issue

(large)  $\theta_e \longleftrightarrow \theta_e$  (small)

$m_e \longleftrightarrow m_e$

How to generate Weinberg's effective operator?

$$M_\nu \gg M_W$$

3 ways (see-saw)

Ma '98

I) add  $\nu_R$  ( $\geq 2$  for at least two massive  $\nu$ 's)

$$\mathcal{L}_Y = Y_0 \bar{\nu}_L \Phi \nu_R + M_R \nu_R^T C \nu_R + h.c.$$

$$Y_{\text{eff}}/M_\nu \approx Y_0^2/M_R$$

Minkowski; '77

Gell-Mann et al;

Glashow; Mohapatra, G.S. '79

II) add  $\Delta_H$ :  $SU(2)_L$  triplet,  $Y=2$

$$\mathcal{L}_Y = Y_\nu \Delta l l + \mu \Delta^* \Phi \Phi + M_\Delta \Delta^2$$

$$\mu = M_\Delta \Rightarrow \langle \Delta \rangle \approx M_W^2/M_\Delta$$

$$Y_{\text{eff}}/M_\nu \approx Y_\nu/M_\Delta$$

Lazandus, Shafi,  
Wetstenich

Mohapatra, G.S. '80

NO useful information  
if  $M_{\text{new}} \gg M_W$

Weinberg more  
useful

Analogy : ● Fermi theory of weak int.

$$\mathcal{L}_{eff} = \frac{G_F}{\sqrt{2}} \bar{\mu}_L \gamma^\mu \nu_{\mu L} \bar{\nu}_{eL} \gamma^\mu e_L$$

- $\mathcal{L}_{int} = g/\sqrt{2} \bar{l}_L \gamma^\mu \nu_L W_\mu^- + h.c.$

small energy:  $E \ll M_W$

$$\frac{G_F}{\sqrt{2}} = \frac{g^2}{8M_W^2}$$

↑ tells you nothing;  
instead of coupling between  $l, \nu \rightarrow$   
couplings with unknown,  
unreachable  $W^-$

- if  $E \approx M_W \Rightarrow$  useful ( $\sim$  Shaposhnikov)

- or if a theory of  $\bar{W}$  exists

e.g. SM =  $SU(2)_L \times U(1)_Y$

↓

neutral current - correlated with  
charged

See-saw useful iff one has a theory of  $Y_D, M_R, \dots$

connect neutrino mass, mixing with new physical phenomena

- e.g. **L-R** theory: restoration of parity ( $W_R^+, Z_{R-}$ )

$$\begin{pmatrix} \nu \\ e \end{pmatrix}_L \leftrightarrow \begin{pmatrix} \nu \\ e \end{pmatrix}_R$$

Minkowski,  
Mohapatra, G.S.

I + II naturally present

- scales, couplings?

GRAND UNIFICATION

G.S., see-saw 25

**SO(10)** : compute  $m_\nu, \theta_e$

e.g. SUSY SO(10) : normal hierarchy  
 $\theta_{12} \approx 10^\circ$

connection with proton decay

but  $M_R, M_\Delta \approx M_{GUT}$  only indirect tests

similar in ordinary SO(10) :  
 $M_R \rightarrow 10^{10} \text{ GeV}$

III) add  $T_F$  :  $SU(2)$  fermion triplet,  $Y=0$

$$\mathcal{L}_Y = Y_D T_F \Phi l + M_T T_F C T_F$$

$$Y_D^2 / M_T = Y_{\text{eff}} / M_\nu$$

Foot et al '89

(analogy type I)

$\Rightarrow$  at least two  $T_F$ ; or III+I

baroque? little studied, almost nothing

If  $m_T < T e \bar{V} \Rightarrow$  real exciting

**GUT** : grand unification to fix  $m_T$ ?

• Minimal :  **$SU(5)$**

Minimal  $SU(5)$  fails  $\left\{ \begin{array}{l} m_\nu = 0 \\ \text{no unification} \end{array} \right.$   
( $SM \subseteq SU(5)$ )

I) add  $1_F = \nu_R$  : fails (also expect:  $m_{T_F} > M_{\text{GUT}}$ )

II) add  $15_H \supseteq \Delta_H \Rightarrow$  ok, but no

interesting prediction

Donner, Filenig-Porz  
'06

III)  $24_F \geq T_F$  (need two?)

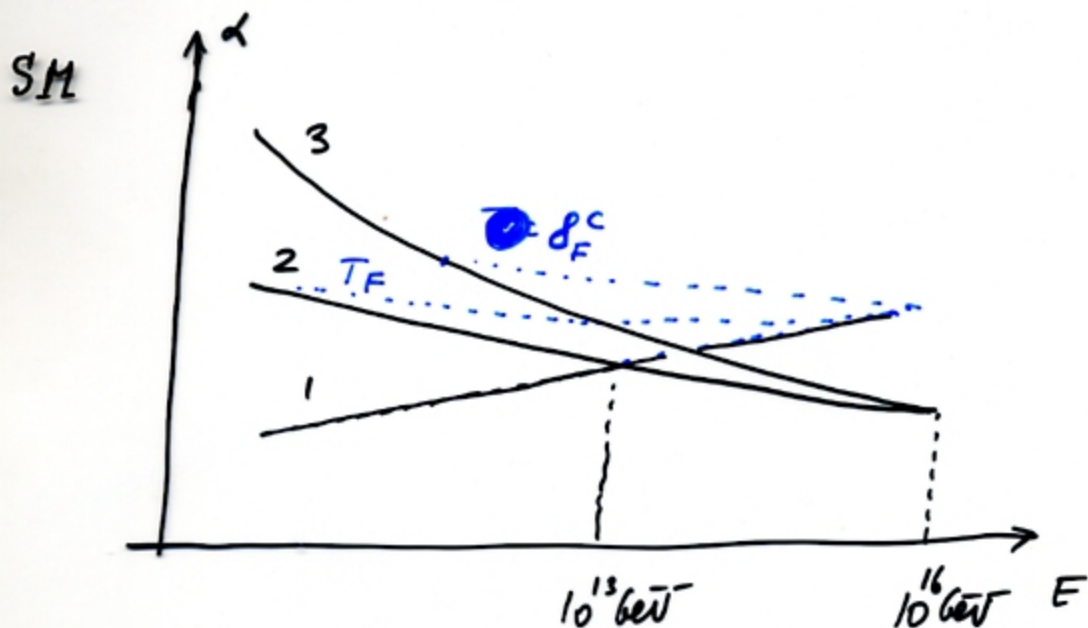
$$24_F = 1_F + 3_F + 8_F^c + (2, 3_c)_F$$

$\downarrow$                        $\downarrow$   
 I                      III                      sufficient

prediction:  $m_1 = 0$   
 (one neutrino massless)

Bayc, G.S. '06  
 Bayc, Nemerich, G.S.  
 (yesterday)

● UNIFICATION



new states: raise  $\alpha$ , unless  $\gamma = 0$

$T_F (\gamma = 0)$  ideal  $\Rightarrow m_T \leq T_e V$

$m_g \approx 10^7 - 10^9 \text{ GeV}$

$$\alpha_F = m_F T_\nu 2q_F^2 + \lambda T_\nu 2q_F^2 2q_H + \frac{1}{\Lambda} T_\nu 2q_F^2 2q_H^2 \quad (*)$$

$$\langle 2q_H \rangle = \text{diag} (\text{~~2, 2, 2~~ } 2, 2, 2, -3, -3)$$

↑  
higher dimensional  
operator

$$\mathcal{L}_Y = \gamma_d 10_F \bar{5}_F 5_H^* + \gamma_u 10_F 10_F 5_H$$

↓

$$\gamma_d = \gamma_e$$

$$+ \frac{1}{\Lambda} 10_F \bar{5}_F 5_H^* 2q_H$$

$$\bullet \gamma_b = \gamma_\tau + \mathcal{O}\left(\frac{M_{GUT}}{\Lambda}\right) \text{ at } M_{GUT}$$

$$\text{but } \gamma_b \leq 0.6 \gamma_\tau$$

$$\text{and } \gamma_b \sim 1/100 \Rightarrow \underline{\underline{\Lambda \approx 100 M_{GUT}}}$$

$$(*) \quad \left. \begin{aligned} m_0^F &= m_F - \lambda_F v_{GUT} + \mathcal{O}(v_{GUT}^2/\Lambda) \\ m_3^F &= m_F - 3\lambda_F v_{GUT} + \mathcal{O}(-) \\ m_2^F &= m_F + 2\lambda_F v_{GUT} + \mathcal{O}(-) \end{aligned} \right\} \text{fine-tuning}$$

$$m_{(3,2)}^F = m_F - \frac{\lambda_F v_{GUT}}{2} + \mathcal{O}(-) \Rightarrow \boxed{m_{(3,2)}^F \approx \frac{M_{GUT}^2}{\Lambda}}$$



1-loop

$$\exp \left[ 30 \pi \left( d_1^{-1} - d_2^{-1} \right) / M_2 \right] =$$
$$= \left( \frac{M_{GUT}}{M_2} \right)^{24} \left( \frac{(m_5^F)^4 m_3^B}{M_2^5} \right)^5 \left( \frac{M_{GUT}}{m_{(3,2)}^F} \right)^{20} \frac{M_{GUT}}{m_{\text{color triplet}}}$$

$\downarrow$   
24H

SM:  $m_3 = M_{GUT} \Rightarrow$

light triplet  $\nearrow M_{GUT}$  as needed

$m_3 \leq \text{TeV}$

$$\exp \left[ 20 \pi \left( d_1^{-1} - d_3^{-1} \right) / M_2 \right] =$$
$$= \left( \frac{M_{GUT}}{M_2} \right)^{26} \left( \frac{(m_8^F)^4 m_8^B}{M_2^5} \right)^5 \left( \frac{M_{GUT}}{m_{(3,2)}^F} \right)^{20} \left( \frac{M_{GUT}}{m_{\text{color triplet}}} \right)^{-1}$$

SM:  $m_8 = M_{GUT}$ ; but 1-3 meet after

1-2

$$\Rightarrow \left| m_8 \approx 10^7 \text{ GeV} \right.$$

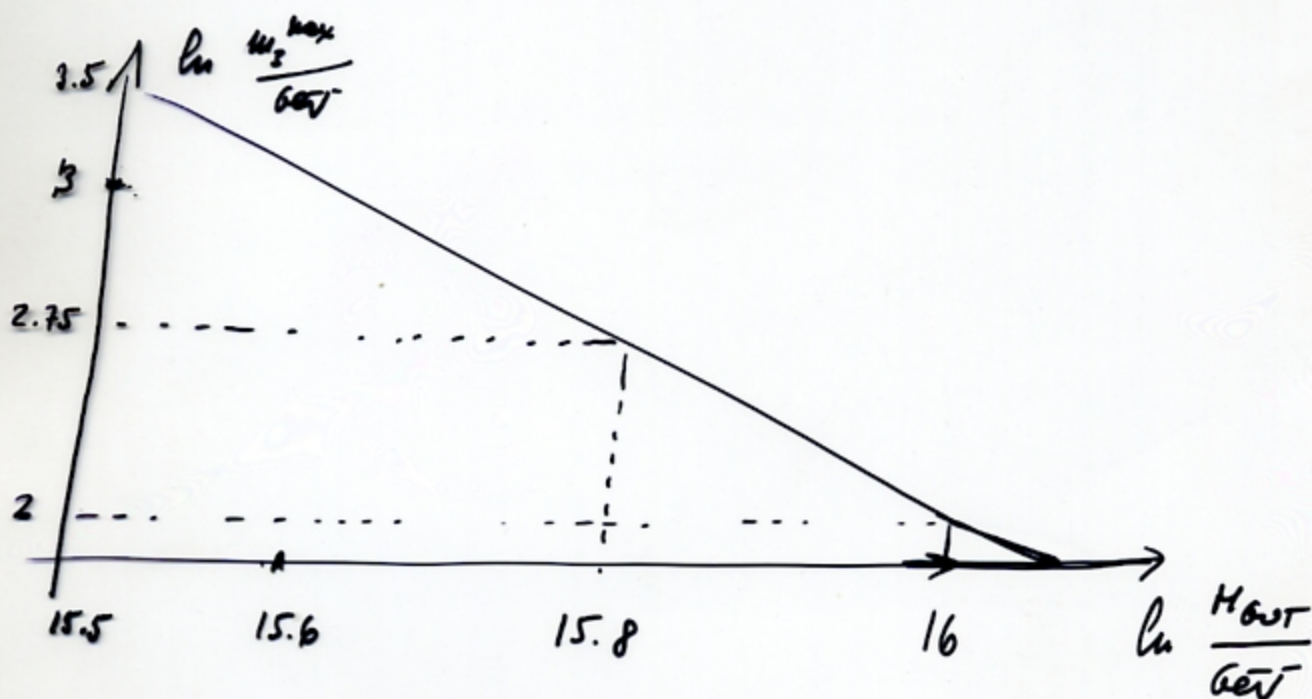
2-loop

- $m_{\text{color triplet}} > 10^{12} \text{ GeV}$  (proton decay)
- $M_{\text{GUT}} > 10^{15.5} \text{ GeV}$  (proton decay)
- $m_{(2,2)}^F \approx \frac{M_{\text{GUT}}}{100} \left( \frac{M_{\text{GUT}}^2}{\Lambda} \right)$



$$M_{\text{GUT}} \leq 10^{16} \text{ GeV} \quad (\text{hard prediction})$$

$$\tau_p < 10^{36} \text{ yr} \quad \text{observable?}$$



$$M_{\text{GUT}} \approx 10^{16} \text{ GeV} \quad m_F \approx 200 \text{ GeV}$$

$$m_F^2 \approx 10^7 - 10^8 \text{ GeV}^2$$

$$\bullet \mathcal{L}_Y = Y_{2F} \bar{5}_F 5_H^* + \frac{2F 5_F 5_H^* 2H}{\Lambda}$$

$$\begin{array}{cccc} \downarrow & \downarrow & \downarrow & \downarrow \\ T_F, S_F & l & \bar{\Phi}^* & \text{necessary} \end{array}$$



would not split  $Y_T, Y_S$



$$\mathcal{L}_Y(\text{eff}) = Y_T^i T_F \bar{\Phi}^* l_i + Y_S^i S_F \bar{\Phi}^* l_i \\ + m_T T_F T_F + m_S S_F S_F \quad i=1, 2, 3$$

3 + 3 complex Yukawas

↳ make real by phase convention



3 + 6 = 9 real couplings

→ 2 masses ( $m_1 = 0$ )

3 mixings

1 + 1 = 2 phases (only one Majorana phase)

## Light triplets

$$\text{LHC: } m_T < 500 \text{ GeV} \quad (\sim \text{Winos})$$

- weakly produced,  $\sim$  winos

- decays  $T^- \rightarrow W^- + \nu$   $T^0 \rightarrow Z + \nu$   
 $Z + l$   $\rightarrow W^+ + l$

directly through Yukawa

$$\mathcal{L}_Y = Y_T^k T \Phi l_k + Y_S^k S \Phi l_k \quad k=1,2,3$$

(3+6=9)

$$\Gamma(T^- \rightarrow Z l_k^-) = \frac{m_T}{32\pi} |Y_T^k|^2 \left(1 - \frac{m_Z^2}{m_T^2}\right) \left(1 + 2 \frac{m_Z^2}{m_T^2}\right)$$

$$\sum_k \Gamma(T^- \rightarrow W^- \nu_k) = \frac{m_T}{16\pi} (\sum |Y_T^k|^2) \quad \text{---}$$

and similar for  $T^0$

- $m_T \approx 300 \text{ GeV}$ :  $|Y_T^{\text{max}}| \geq 5 \times 10^{-7} \Rightarrow$

$$(10^{-11} \text{ mm} \lesssim) \tau_T \lesssim 10^{-1} \text{ mm}$$

- one massless neutrino

e.g. ~~normal~~ <sup>normal</sup> hierarchy  $m_1^{\nu} = 0$

$$\frac{i \frac{d_w y_T}{\sqrt{2m_T}}}{i \frac{d_w y_T}{\sqrt{2m_T}}} = U_{12} \sqrt{m_2^{\nu}} \cos z \pm U_{13} \sqrt{m_3^{\nu}} \sin z$$

$$\frac{i \frac{d_w y_S}{\sqrt{2m_S}}}{i \frac{d_w y_S}{\sqrt{2m_S}}} = U_{12} \sqrt{m_2^{\nu}} \sin z \mp U_{13} \sqrt{m_3^{\nu}} \cos z$$

$z \in \mathbb{C}$ ,  $U = PMNS$  (1 + 1 phase only)  
 $\uparrow$  Majorana

- $\text{Im}(A) \gg 1$  (large Yukawa's)

$\rightarrow LFV$

$$\theta_{13} = 5^\circ: \left\{ \begin{array}{l} .25 \leq \frac{\Gamma(\mu)}{\Gamma(\tau)} \leq 4.3 \\ .02 \leq \frac{\Gamma(e)}{\Gamma(\mu, \tau)} \leq .5 \end{array} \right\} \quad \text{expected} \quad \theta_{13} = 0^\circ \left\{ \Gamma(e) = \Gamma(\mu) = \Gamma(\tau) \right\}$$

inverse hierarchy:  $\Gamma(\mu) = \Gamma(\tau)$

$$.07 \leq \frac{\Gamma(e)}{\Gamma(\mu)} \leq 50$$

no  $\theta_{13}$  dependence!

• COSMOLOGICAL IMPLICATIONS

• LEPTOGENESIS

$$\Sigma_{\max} \approx \frac{1}{16\pi} \frac{M_T (m_3^\nu - m_2^\nu)}{v^2} \quad M_T \ll M_S$$

↑ neutrinos - no

assumptions as in the three

$\nu_R$  case (Davidson, Ibarra)

Raidel, Strumia,  
Tuttyushki '04

$M_T \approx \text{TeV}$   $\Downarrow$

$\Sigma_{\max} \leq 10^{-12}$  - far too small



only resonant leptogenesis:  $M_T \approx M_S$

is hard to produce:

$$|Y_S| \ll 1/10$$

unitarity of  $\rho_{MN}$   $\Leftrightarrow$  LFV

Biggio et al '06

• NO DARK MATTER CANDIDATE

e.g.  $T_F$  (unlike  $W_{ino}$ ) decays through  $Y_T$

# OUTLOOK

Minimal  $SU(5)$  (type III see saw)

$\oplus 24_F$

$T_F$  ( $SU(2)$  triplet  $\sim$  winos)  $\therefore m_T \lesssim \text{TeV}$

$M_{GUT} \leq 10^{16} \text{ GeV} \Rightarrow \tau_p \leq 10^{36} \text{ yr}$

LHC - proton decay connection

$\downarrow$  measure directly see-saw

• comparison with supersymmetry

$\sim$  : light wino ( $\leq \text{TeV}$ )

heavy gluino ( $10^7 - 10^9 \text{ GeV}$ )

decoupled Higgsino ( $m_{\tilde{h}} > M_{GUT}$ )

⇒ consistent with unification :

gluino  $M_W \sim 10^9 \text{ GeV}$

Higgsino  $M_W \sim M_{\text{pe}}$

split (more)  
supersymmetry

\*

• loophole : leptogenesis ?

$$\left. \begin{array}{l} \nu_R \rightarrow \phi + l \\ \phantom{\nu_R \rightarrow} \phi^* + l^c \end{array} \right\} \begin{array}{l} \Delta L \neq 0 \Rightarrow \\ \Delta B \neq 0 \text{ (sphalerons)} \end{array}$$

↓  
lightest right-handed neutrino

$$\Rightarrow M_R \gtrsim 10^9 \text{ GeV}^-$$

Davidson, Ibarra '02

↓ needs assumptions about Yukawas

$$m_\nu \propto Y^T Y, \quad \epsilon \propto Y^* Y$$

⇓

even TeV ok!

Reidel, Strumia,

Taruyoshi '04

(or resonant - Pilaftsis)