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What kind of ν beam ?

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1. ν oscillations
2. ν beams @ accelerators
3. ν -factory
4. superbeams

conclusions

1. ν oscillations

Atmospheric & solar data $\rightarrow$ 3 ν mixing

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = V \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

V : 3x3 mixing matrix, 6 parameters

2 mass differences $\Delta m_{12}^2, \Delta m_{23}^2$

3 mixing angles $\theta_{12}, \theta_{23}, \theta_{13}$

1 CP phase δ

$$(\Delta m_{ij}^2 = m_i^2 - m_j^2)$$

ν oscillation date (2 state mixing)

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \sin^2 2\theta \cdot \sin^2 \left(1.27 \frac{\Delta m^2 (\text{eV}^2) L (\text{km})}{E_\nu (\text{GeV})} \right)$$

today:

- atmosph. ν : $\nu_\mu \rightarrow \nu_\tau$

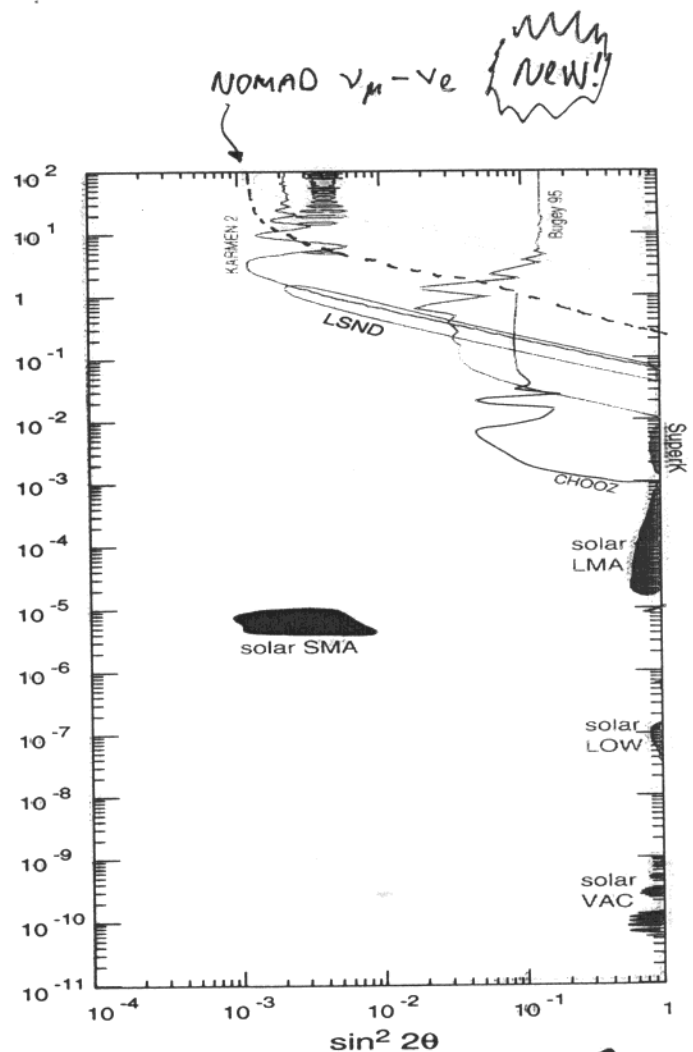
$$|\Delta m_{23}^2| \sim 1.5 \div 5 \cdot 10^{-3} \text{eV}^2, \sin^2 2\theta_{23} \sim 1$$

- solar ν : $\nu_e \rightarrow \nu_\mu$

$$|\Delta m_{12}^2| \sim 10^{-5} \div 10^{-4} \text{eV}^2, \text{SMA or LMA } \Delta m^2 (\text{eV}^2) \sim 10^{-7}, \text{max. mixing}$$

- CHOOZ: $\sin^2 2\theta_{13} \lesssim 0.05$

- all 3 known ν s participate in the oscillations



- in the limit $|\Delta m_{23}^2| \gg |\Delta m_{12}^2|$

solar & atmosp. ν oscillations largely decoupled:

$$P(\nu_e \rightarrow \nu_\mu) = \sin^2 \theta_{23} \cdot \sin^2 2\theta_{13} \cdot \sin^2 \left(\frac{\Delta m_{23}^2 \cdot L}{4 E_\nu} \right)$$

$$P(\nu_e \rightarrow \nu_\tau) = \cos^2 \theta_{23} \cdot \sin^2 2\theta_{13} \cdot \sin^2 \left(\frac{\Delta m_{23}^2 \cdot L}{4 E_\nu} \right)$$

$$P(\nu_\mu \rightarrow \nu_\tau) = \cos^4 \theta_{13} \cdot \sin^2 2\theta_{23} \cdot \sin^2 \left(\frac{\Delta m_{23}^2 \cdot L}{4 E_\nu} \right)$$

in this approx., very good for SMA & LOW,

ν oscillations are described by only θ_{13} , θ_{23} , Δm_{23}^2

in LMA scenario (Δm_{12}^2) $\Rightarrow$ all 6 parameters:

$$\begin{aligned} P(\nu_e \rightarrow \nu_\mu) = & \sin^2 \theta_{23} \cdot \sin^2 2\theta_{13} \cdot \sin^2 \left(\frac{\Delta m_{23}^2 \cdot L}{4 E_\nu} \right) \\ & + \cos^2 \theta_{23} \cdot \sin^2 2\theta_{12} \cdot \sin^2 \left(\frac{\Delta m_{12}^2 \cdot L}{4 E_\nu} \right) \\ & + \tilde{J} \cdot \cos \left(\delta - \frac{\Delta m_{23}^2 \cdot L}{4 E_\nu} \right) \cdot \frac{\Delta m_{12}^2 \cdot L}{4 E_\nu} \cdot \sin \left(\frac{\Delta m_{23}^2 \cdot L}{4 E_\nu} \right) \end{aligned}$$

where

$$\tilde{J} = \cos \theta_{13} \cdot \sin 2\theta_{12} \cdot \sin 2\theta_{23} \cdot \sin 2\theta_{13}$$

- if LSND confirmed, the situation ... more complex...

near future: what will we know in 10 years?

- oscillation pattern $\nu_\alpha \rightarrow \nu_\beta$, ν_β appearance?
 - solar/reactor exp.: SNO, Borexino, KamLAND, ICARUS, GAD...
 - accelerator exp.: K2K, MINOS, OPERA, ICARUS, MiniBooNE
- if ν oscillation confirmed:
 - SMA or LMA? 10 ÷ 20% accuracy on θ_{12} , Δm_{12}^2
 - $|\Delta m_{23}^2|$, $\sin^2 2\theta_{23}$ at 10% level
 - $\sin^2 2\theta_{13}$ explored down $\sim 10^{-2}$



remaining questions:

1. θ_{13} : link solar $\leftrightarrow$ atmosph. ν ?
2. sign of Δm_{23}^2 : ν -mass spectrum ?
3. CP δ ?

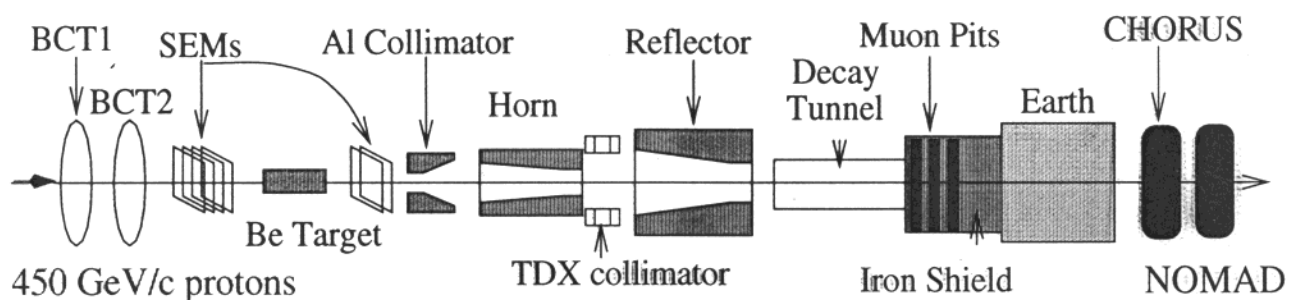
future: $\rightarrow$ small coupling & mass differences:

$\Rightarrow$ increase ν intensity & L/E
more than a factor 10 !!!

2. ν beams @ accelerators

high energy accelerators provide ν_μ beams by the decay of π, K s produced by high energy protons on light targets

i.e. WANF @ CERN SPS



- 450 GeV/c protons on Be rods, $\phi = 3 \text{ mm}$, $3 \times 10^{13} \text{ pot}/14.4 \text{ s}$
- + (-) mesons focussed (defocussed) by magnetic horns to CHORUS, NOMAD detectors, $L = 860 \text{ m}$

$$\Rightarrow 0.95 \cdot 10^{-2} \nu_\mu / \text{pot} / 6.8 \text{ m}^2 \quad E_{\nu_\mu} \sim 24.3 \text{ GeV}$$

$$\frac{\bar{\nu}_\mu}{\nu_\mu} \sim 6.9 \% \quad \frac{\nu_e}{\nu_\mu} \sim 1 \% \quad \frac{\bar{\nu}_e}{\nu_\mu} \sim 0.26 \%$$

- high resolution & granularity of NOMAD detector

$\Rightarrow$ study of ν beam with unprecedented accuracy ($1.3 \cdot 10^6 \nu_\mu \text{ cc}$)

$\hookrightarrow$ benchmark for conventional ν beams!

CNGS, K2K, NUMI...

to predict ν beam intensity, spectrum & composition:

- precise description of π, κ yields by 450 GeV/c protons on Be ($\kappa/\pi \leftrightarrow \nu_e/\nu_\mu$!)

• experimental data on π, κ, p by 400, 450 GeV/c protons on Be

$\left\{ \begin{array}{l} \text{Atherton et al. (198)} \\ \text{SPY Collob (1999)} \end{array} \right.$

• MC hadronic generators: FLUKA, 20% of accuracy
 $\hookrightarrow$ limit to sensitivity! K_L^0 ?

- accurate description of the focussing system

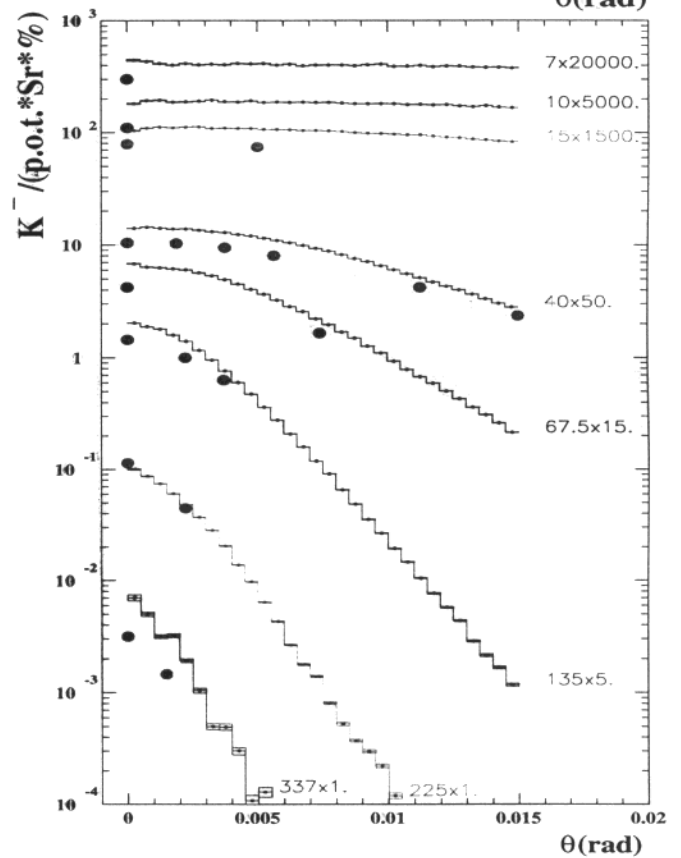
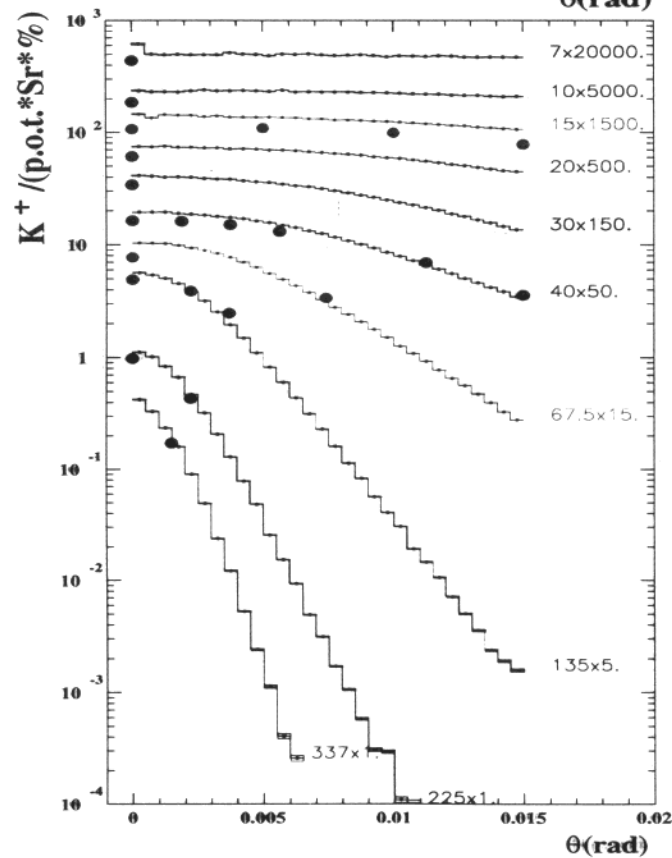
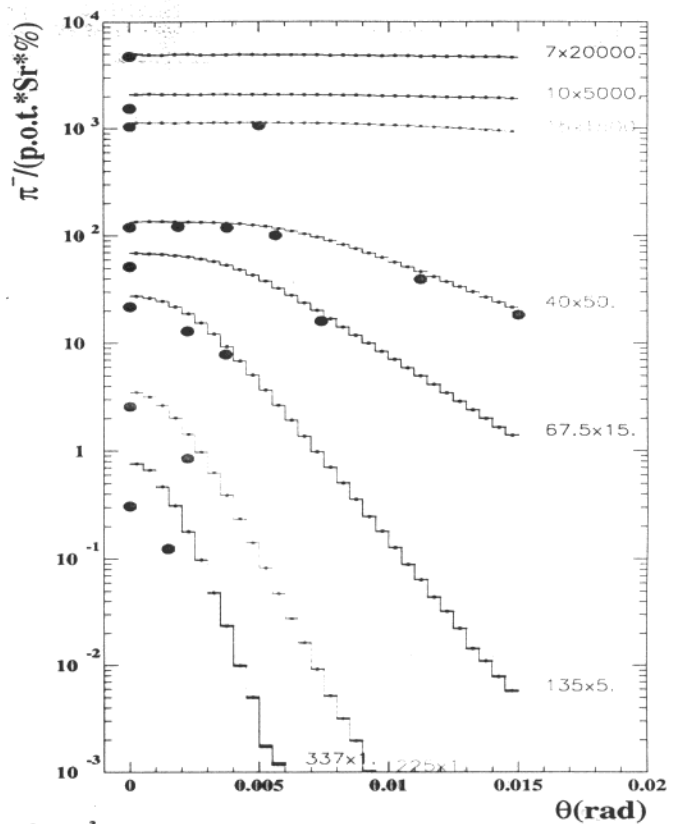
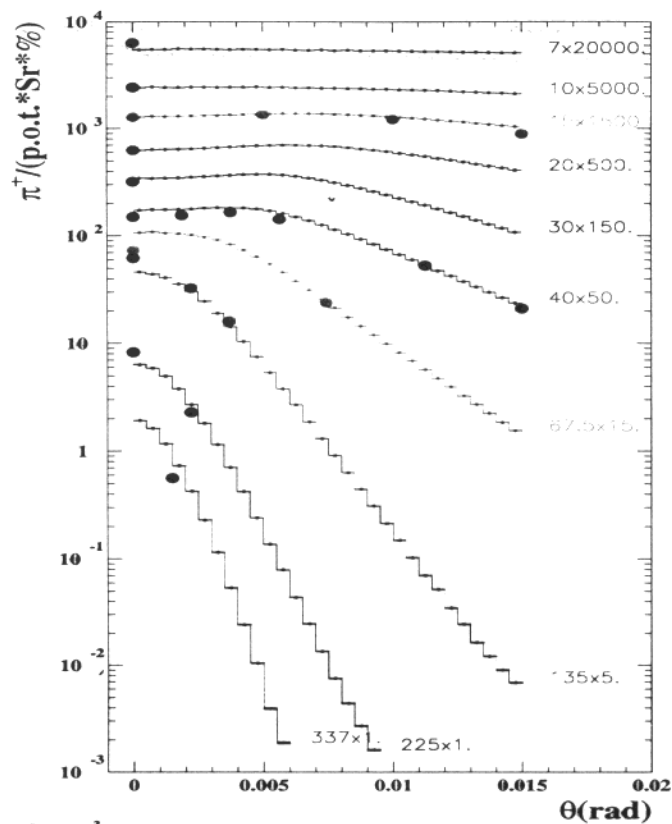
- accurate description of primary proton spot:

tails of protons missing the target will interact in the downstream material $\leadsto \sim 30\%$ of $\bar{\nu}_\mu, \bar{\nu}_e$ (minor components from defocussed $\pi^-, \kappa^-; \dots$)

- accurate description of particle propagation in the material of the beam line (reinteractions...)

$\Rightarrow$ Simulation of a real ν beam

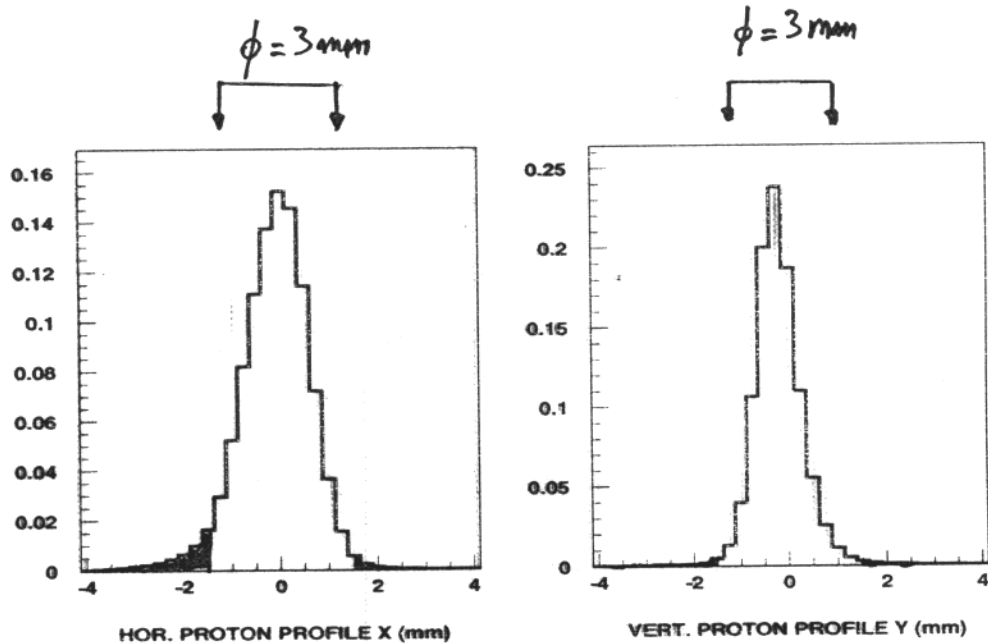
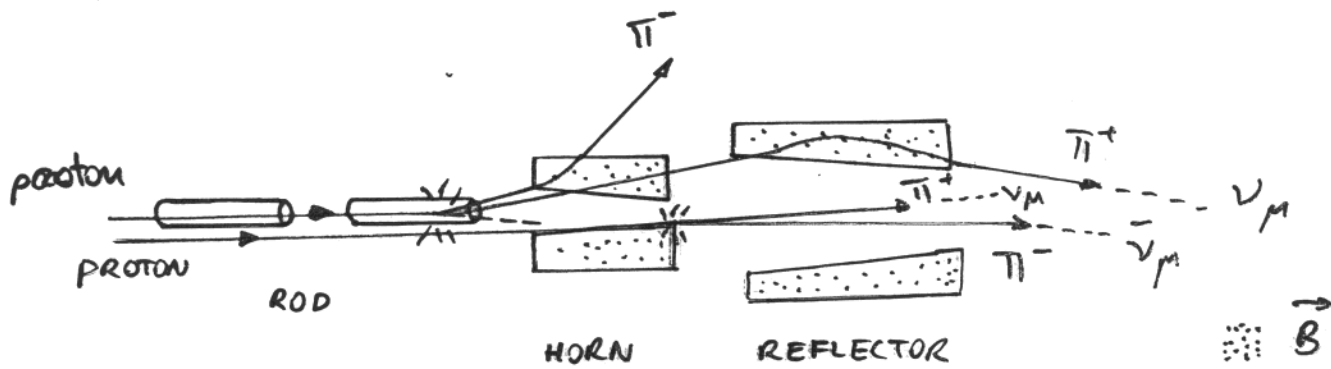
is $\sim$ complicated cascade of physical processes and not just a calculation of π, κ production where mesons decay in a vacuum tunnel...



• SPY/Atherton (rescaled) data

— FLUKA predictions : accuracy $\sim 20\%$!
(the best hadronic generator)

450 GeV/c protons on 100 mm Be target

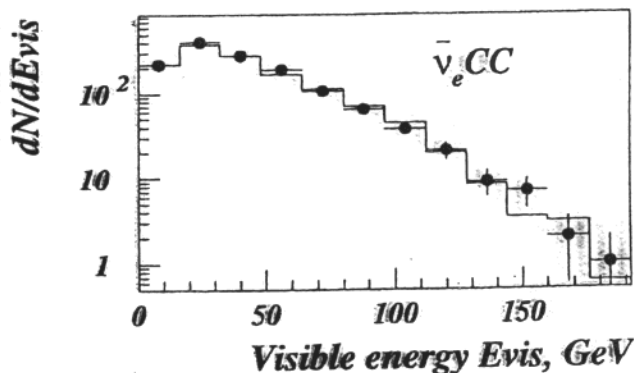
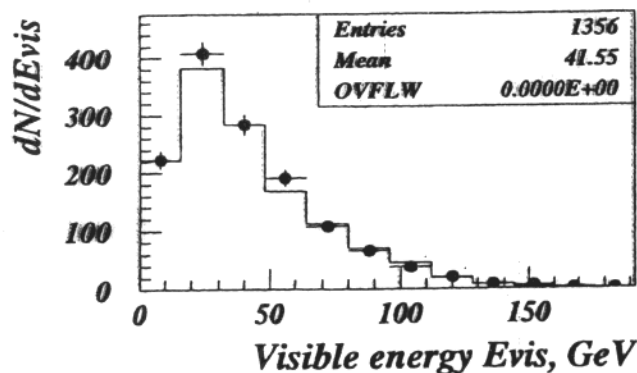
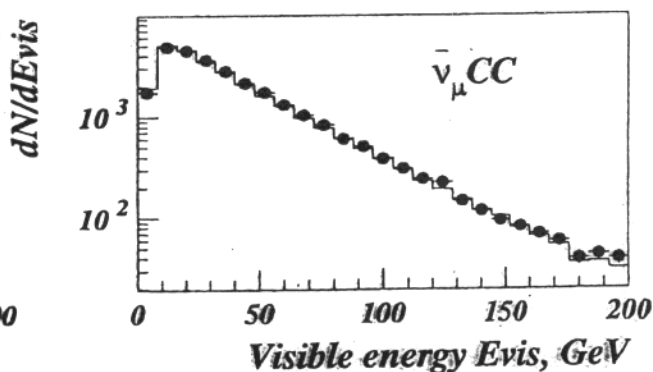
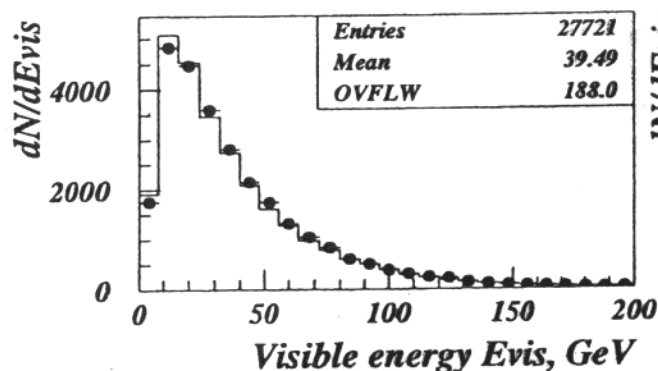
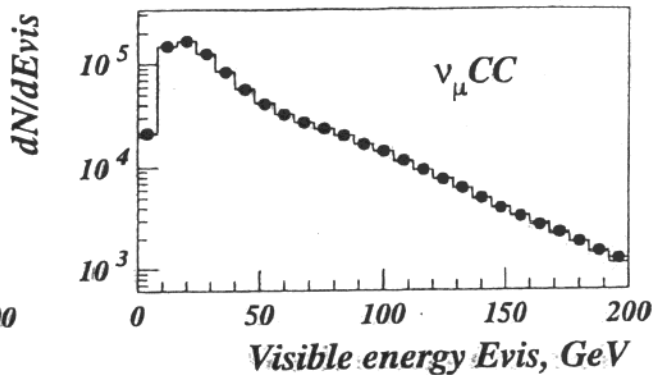
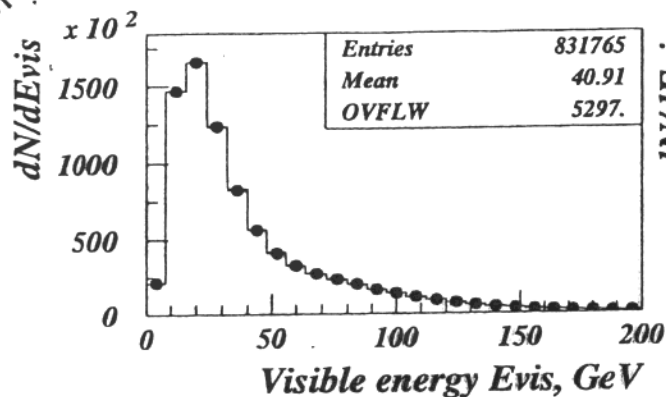


Knowledge { p beam profiles / stability in the accelerator
material in the beam line

is critical for $\bar{\nu}_\mu$, $\bar{\nu}_e$ fluxes !

NOMAD final results

State of the Art!



• data

└ MC - Feuka tuned to SPY/Atherton data
 ν_μ CC MC normalized to the data

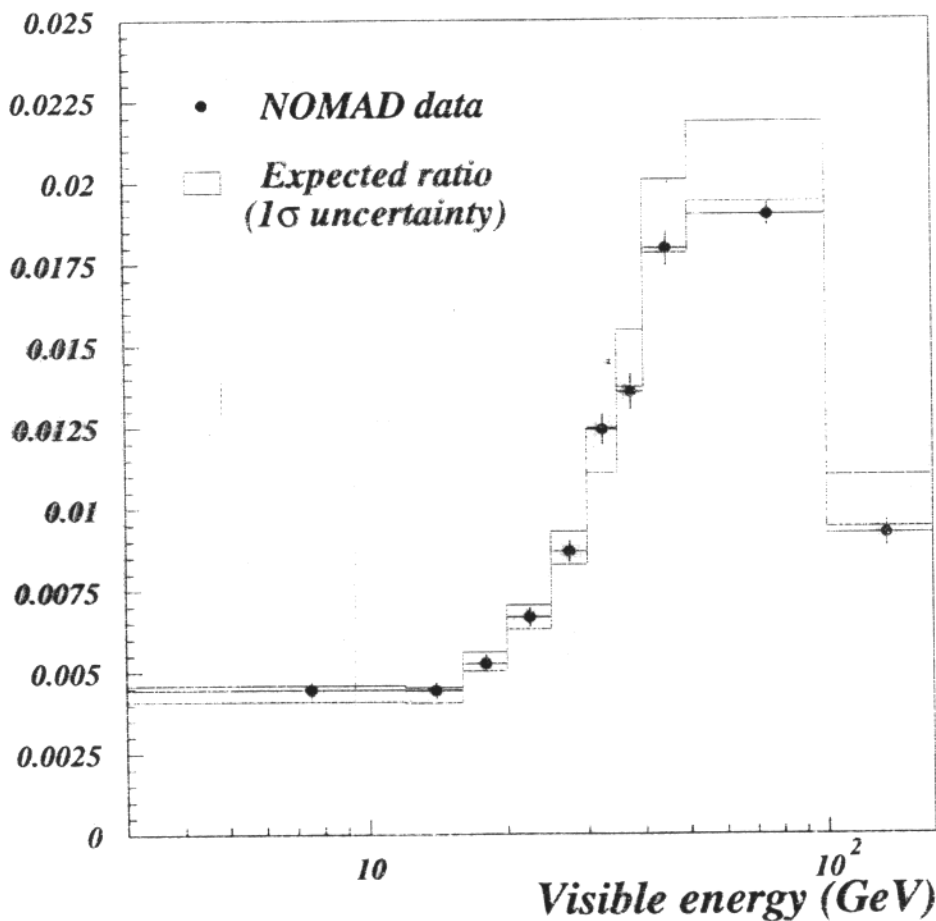
- agreement MC - ν_{cc} / data @ few % level (shape)

- systematics on ν_e/ν_μ ~ 5 % (beam)

Preliminary Results

- Bin-to-bin systematic errors: 5-8%
(mainly due to uncertainties in π^+ , K^+ and K_L^0 yields)
- Overall (normalization) uncertainty: 2%

$R_{e\mu}$ ratio as a function of neutrino energy:



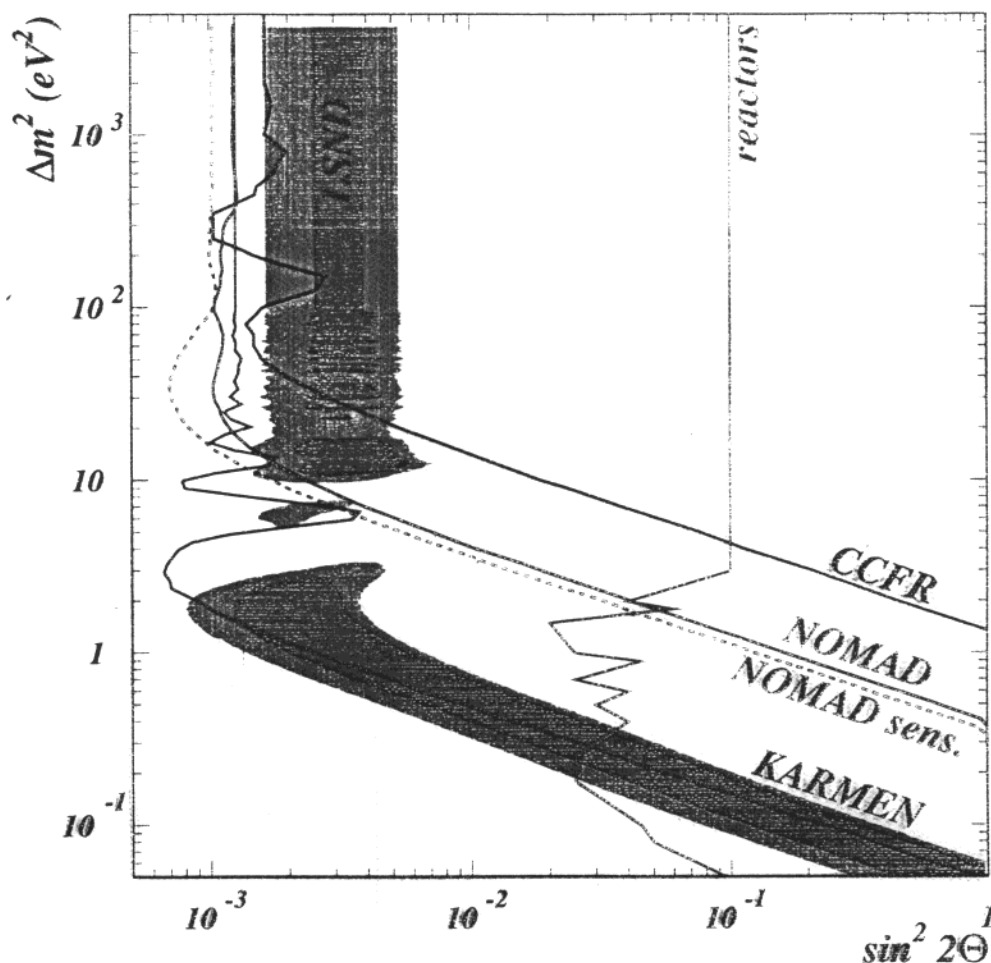
Data are analysed in 10 energy and 3 radial bins:

- χ^2 in the absence of oscillations: 19.7 / 29 d.o.f.
- $\chi_{\min}^2$ with oscillation hypothesis: 18.6 / 27 d.o.f.

No evidence for oscillations

Exclusion Region (Preliminary)

(full NOMAD data sample)



At large Δm^2 : $\sin^2 2\theta < 1.2 \times 10^{-3}$ @ 90% C.L.
(Feldman-Cousins method)

- Exclude high Δm^2 region of oscillation parameters from LSND down to $\sim 10 \text{ eV}^2$
- NOMAD is not sensitive to low Δm^2 LSND solutions (limited by beam energy and source-detector distance)

Conventional ν beams @ accelerators

from π, K decay:

- not pure $\nu_\mu (\nu_e)$ beams
- caveat of hadronic cross-section, particle transport which limit the sensitivity



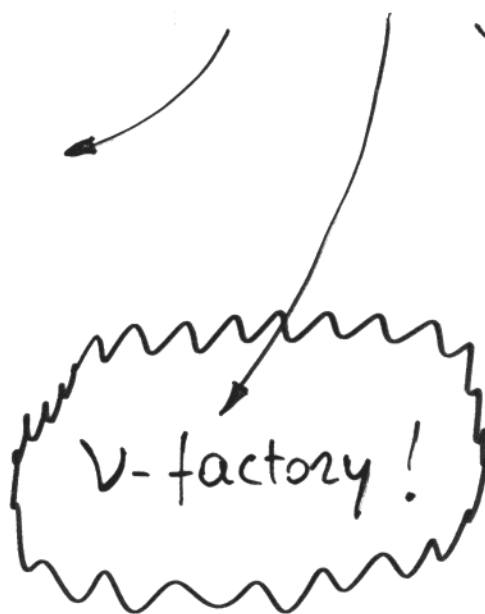
- small coupling
& Δm_{ij}^2 -

more intense, more collimated, better defined

ν beams than the conventional-ones !!!

Super beam

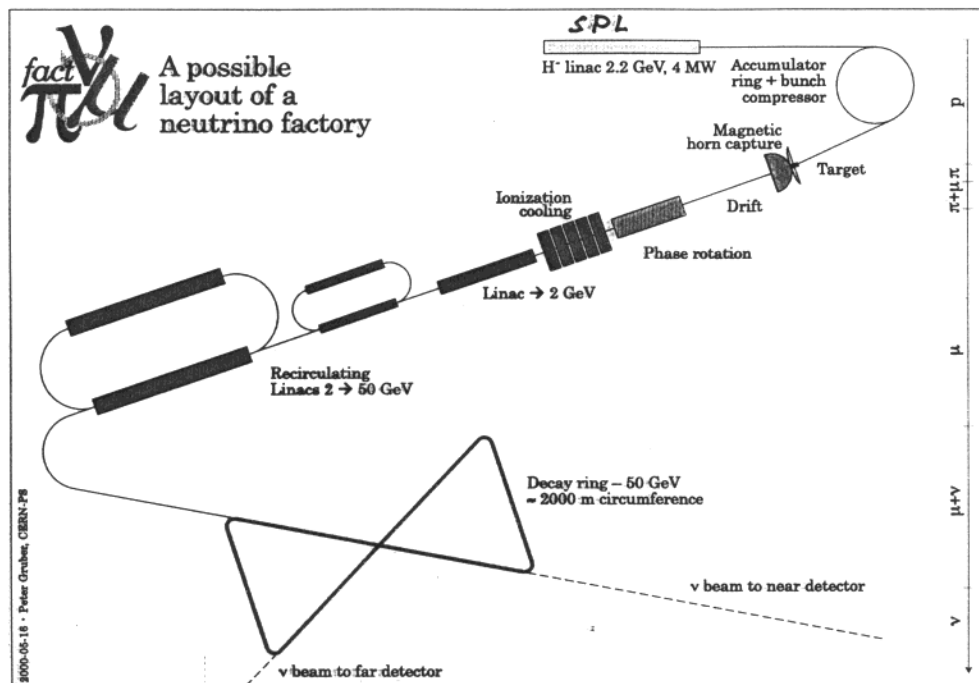
β -beam



3. ν -factory: ν from μ -decay

νF @ CERN

$$\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$$



- 2.2 GeV/c protons from SPL (4 MW) $\rightarrow$ Accumulator
- π s produced in thin target (Hg)
captured by Magnetic Horn $\rightarrow$ Drift space
- μ s cooled/accelerated by a linac up to 2 GeV/c
- μ s accelerated up to 50 GeV/c by Recirculating Linacs
- μ s injected in the μ -accumulator
deliver in the straight sections ν s to experiments

$$SPL : 1.1 \cdot 10^{16} \text{ p/s} \rightarrow 10^{23} \text{ p/year}$$

$$0.3 \cdot 10^{21} \mu \text{ decay/year } (\rightarrow \nu)$$

Several advantages of νF over conventional ν sources:

- decay is $\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$

$\Rightarrow$ pure beam of equal number of $\bar{\nu}_\mu, \nu_e$ ($2\nu/\mu$ -decay!)

- μ momentum is well defined

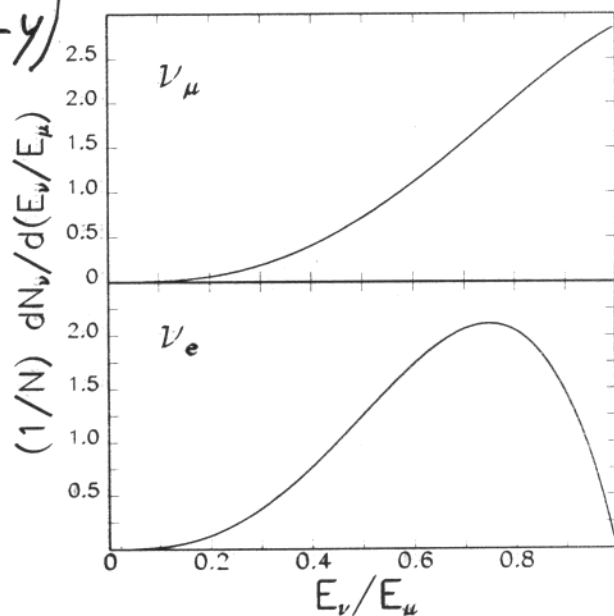
$\Rightarrow$ perfectly calculable E_ν -spectra and ϕ_s

$$\left. \frac{d^2 N_{\nu_\mu, \bar{\nu}_\mu}}{dy ds} \right|_{\theta \approx 0} \approx \frac{E_\mu^2}{\pi m_\mu^2 L^2} \cdot 2y^2 \cdot (3-2y) \cdot \theta(y) \theta(1-y)$$

$$\left. \frac{d^2 N_{\nu_e, \bar{\nu}_e}}{dy ds} \right|_{\theta \approx 0} \approx \frac{E_\mu^2}{\pi m_\mu^2 L^2} \cdot 12y^2 (1-y) \cdot \theta(y) \cdot \theta(1-y)$$

ds : detector area

$$y = E_\nu / E_\mu$$



- ϕ_ν grows like E_ν^2

(conventional ν beam $\phi_\nu \propto E_\nu$)

$$N_{cc} \sim \phi_\nu \cdot \tau_\nu \sim \frac{E_\nu^3}{L^2}$$

$$N_{osc} \sim \phi_\nu \cdot \tau_\nu \cdot P \approx \frac{E_\nu^3}{L^2} \cdot \sin^2 \frac{L}{E_\nu} \sim E_\nu$$

$\Rightarrow$ optimal beam energy as large as possible: $E_\mu = 50 \text{ GeV}$

- pure ν beam: sensitivity to oscillations increases linearly with statistics

$$P(\bar{\nu}_{\mu} - \bar{\nu}_e) \propto \frac{1}{N_{\mu^+}}$$

conventional ν beams: sensitivity $\propto$ square root of statistics

$$P(\nu_{\mu} - \nu_e) \propto \frac{\sqrt{N_{e^-}}}{N_{\mu^-}} = \frac{\sqrt{f}}{\sqrt{N_{\mu^-}}} \quad f = \frac{\nu_e}{\nu_{\mu}} : \text{beam content}$$

- extended ν -flux intensity: more $\times 100$ w.r.t. conventional beam

$$E_{\mu} = 50 \text{ GeV} , \quad 0.3 \cdot 10^{21} \mu\text{-decay/year}$$

$$\left. \begin{array}{l} \bar{\nu}_{\mu} \text{ CC/KT/year} \simeq 0.3 \cdot 10^6 \\ \nu_e \text{ CC/KT/year} \simeq 0.5 \cdot 10^6 \end{array} \right\} \text{ at } 732 \text{ km}$$

$$\text{cf } \text{CNGS} : \begin{array}{l} 2.4 \cdot 10^3 \nu_{\mu} \text{ CC/KT/year} \\ 20 \nu_e \text{ CC/KT/year} \end{array}$$

- extended ν angular divergence $\times 1/5$ w.r.t. conventional beam

$$\Rightarrow \text{VLBL}, L \sim 3000 \text{ km}, 7000 \text{ km}, E_{\nu} \sim 30 \text{ GeV} !!!$$

- ν intensity precisely determined from μ -current ($\lesssim 1\%$)

- ν à la carte: μ -momentum tunable to experimental requirements!

νF : very intense, pure, collimated, well defined ν beams

short-baseline
medium-baseline
long-baseline
very long-baseline $\frac{L}{E} \geq 10^3 \text{ Km/GeV}$

} $\Rightarrow \approx \text{full } \Delta m^2 \text{ exploration}$

νF : available oscillation channels ($\mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$)

$\nu_e - \nu_\mu$ appearance, wrong-sign muons, μ^-

$\bar{\nu}_\mu - \bar{\nu}_e$ " " " electrons, e^+

$\nu_e - \nu_x$ disappearance, E spectrum, NC/CC

$\bar{\nu}_\mu - \nu_x$ " " "

$\nu_e - \nu_\tau$ appearance, τ^- events

$\bar{\nu}_\mu - \bar{\nu}_\tau$ " τ^+ events

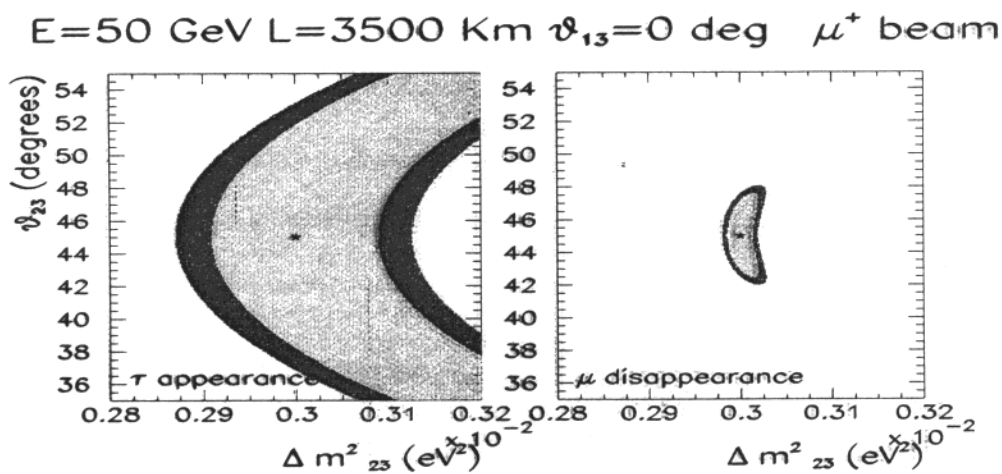
↘ charge identification is mandatory !!!

measurement of θ_{23} & $|\Delta m_{23}^2|$ ($\bar{\nu}_\mu \rightarrow \bar{\nu}_\tau$)

$\bar{\nu}_\mu$ -disappearance basic measurement @ νF (μ^+ identif.)

~~backgr.~~, only $\bar{\nu}_\mu \rightarrow \bar{\nu}_\tau$
 $\searrow$
 τ^+
 $\searrow$
 μ^+

$\bar{\nu}_\tau$ -appearance but... backgr. from charm



$\Rightarrow \theta_{23}, |\Delta m_{23}^2|$ within 1% down $\sim 10^{-4} \text{ eV}^2$

40 kt, $\vec{B}$ detector à la MINOS for 10^{21} useful μ -decays
 $E_\mu = 50 \text{ GeV}$, $L = 3500 \text{ km}$

measurement of θ_{13} ($\nu_e \rightarrow \nu_\mu$)

ν_μ -appearance

- basic measurement @ νF !

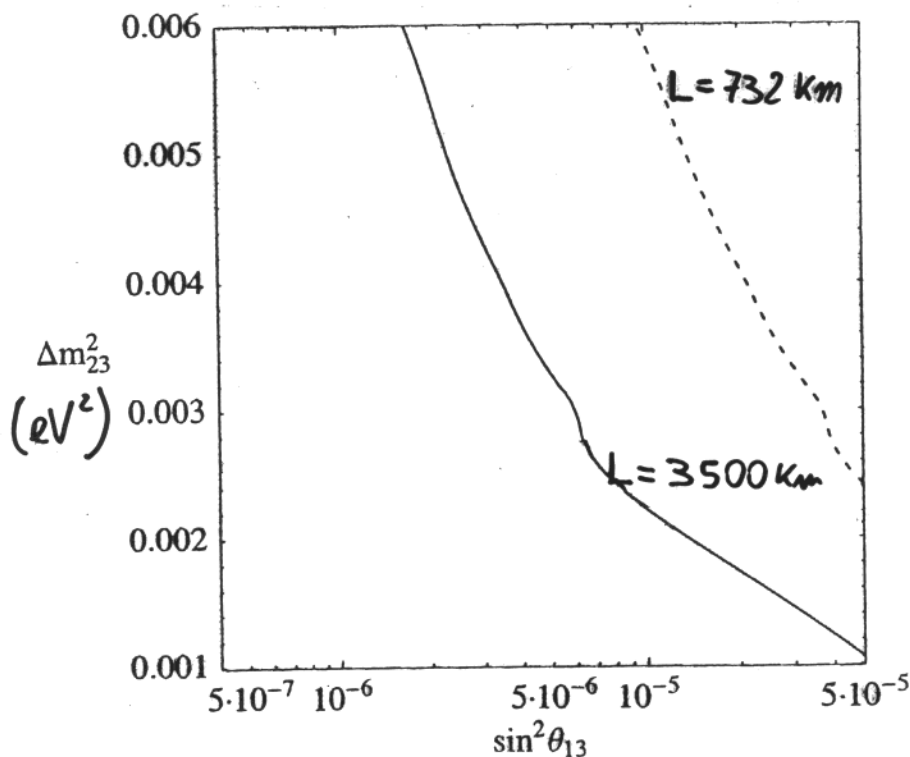
- search for "wrong sign" μ^-

θ_{13} measured with $\Delta\theta \sim 0.1^\circ$ down to 1°

with 40 kT, $\vec{B}$ detector

- S.K. region well covered:

asymptotic sensitivity: more x 3 order of magnitude w.r.t. present limit



- if LMA scenario

θ_{13} correlated to δ

measurement of the sign of Δm_{23}^2

LBL, VLBL $\Rightarrow$ ν propagate inside the Earth $\Rightarrow$ MSW effect

if $\Delta m^2 \gg A = 2\sqrt{2} G_F n_e E_\nu$ (matter mass term)

oscillation probability depends on sign of Δm_{13}^2 (Δm_{12}^2)

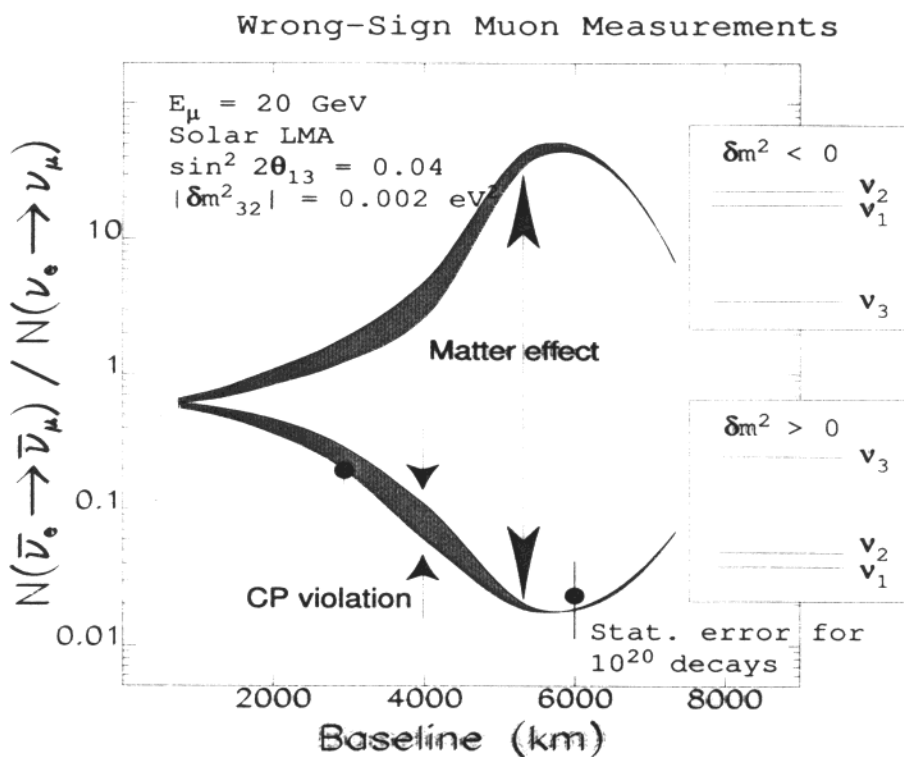
$$\Delta m_{32}^2 \rightarrow -\Delta m_{32}^2 \iff P_{\nu_e \rightarrow \nu_\mu} \rightarrow P_{\bar{\nu}_e \rightarrow \bar{\nu}_\mu}$$

($A \rightarrow -A$ in the oscill. probability)

for: $\Delta m_{32}^2 > 0$ $P(\nu_e \rightarrow \nu_\mu)$ enhanced, $P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)$ suppressed

$\Delta m_{32}^2 < 0$ " suppressed, " enhanced

$\Rightarrow$ with both μ^+ , μ^- beams:



$L \sim 3500 \text{ km}$

40 KT, $\vec{B}$ detector

sign (Δm_{23}^2) determined
 @ 99% C.L. for

$\sigma_{13} \sim 1^\circ \div 10^\circ$

$|\Delta m_{23}^2|^2 \sim 1 \div 5 \cdot 10^{-3} \text{ eV}^2$

CP: measurement of δ

- basic measurement @ νF with both μ^+, μ^- beams

$$A = \frac{P(\nu_e - \nu_\mu) - P(\bar{\nu}_e - \bar{\nu}_\mu)}{+} = \frac{\sin 2\theta_{12}}{\sin \theta_{13}} \cdot \sin \delta \cdot \sin \frac{\Delta m_{12}^2 \cdot L}{4E}$$

via "wrong-sign" μ s.

- CP observable if LMA (favoured by most recent data)

- δ and θ_{13} to be determined simultaneously in both μ^+, μ^- beams

↳ As. E, L to disentangle δ, θ_{13}

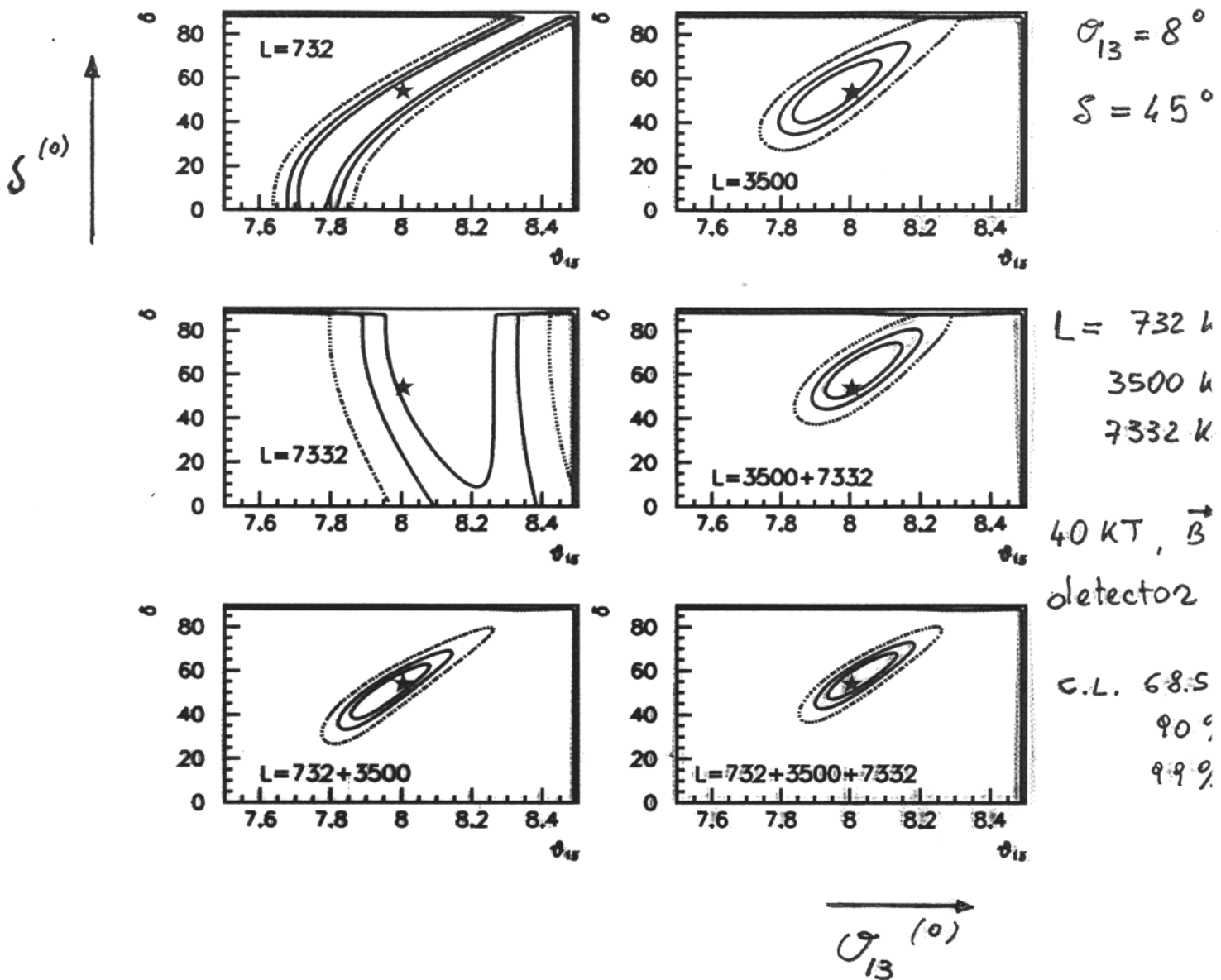
- matter effects $\Rightarrow$ fake CP term which hides genuine CP

↳ careful choice of L

- sensitivity to CP decreases linearly with Δm_{12}^2

40 kt, $\vec{B}$ detector: for $|\Delta m_{12}^2| \geq 2 \cdot 10^{-5} \text{ eV}^2$ $\delta = \begin{matrix} 0^\circ \\ \swarrow \searrow \\ 90^\circ \end{matrix}$

well separated @ 99% C.L.



two detectors:

"near" $L = 732 \text{ km}$

"far" $= 3500 \text{ km}$



νF : complete measurement of mixing matrix
 CP measurement in the leptonic sector

fundamental impact on the ν physics !!!

4. super beams

- CERN-MODANE high intensity, low energy ν_μ beam from π

$$\pi^+ \rightarrow \mu^+ \nu_\mu$$

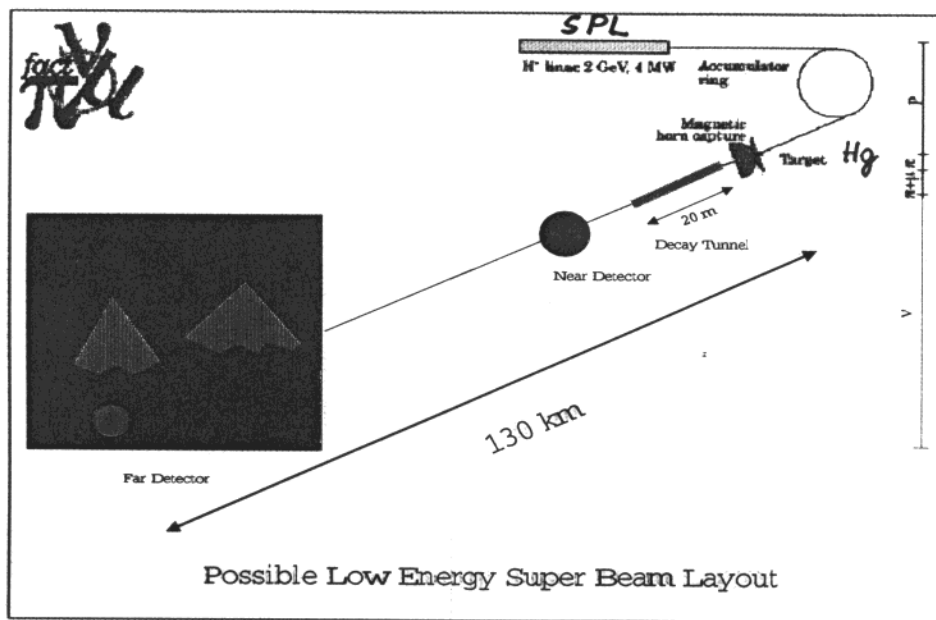
$$\downarrow$$

$$e^+ \nu_e \bar{\nu}_\mu$$

$$\phi_{\nu_\mu} = 1.7 \cdot 10^{14} \nu_\mu / 10^{23} \text{ pot/1a}$$

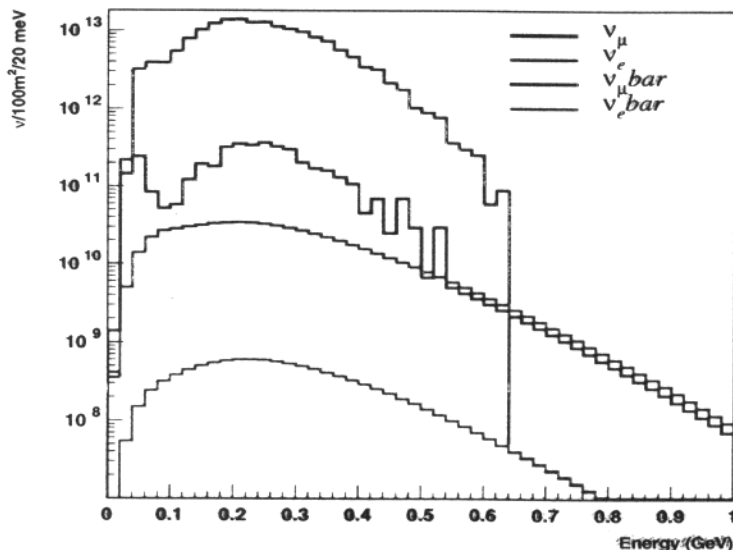
$$E_{\nu_\mu} \sim 0.25 \text{ GeV}$$

$$L = 50 \text{ km}$$



$$P_{\text{proton}} = 22 \text{ GeV,}$$

$$I_{\text{prot}} > 10^{23} \text{ p/yea}$$



- ν_e production by K largely suppressed by threshold effects

$$\hookrightarrow \nu_e \text{ from } \mu\text{-decay}$$

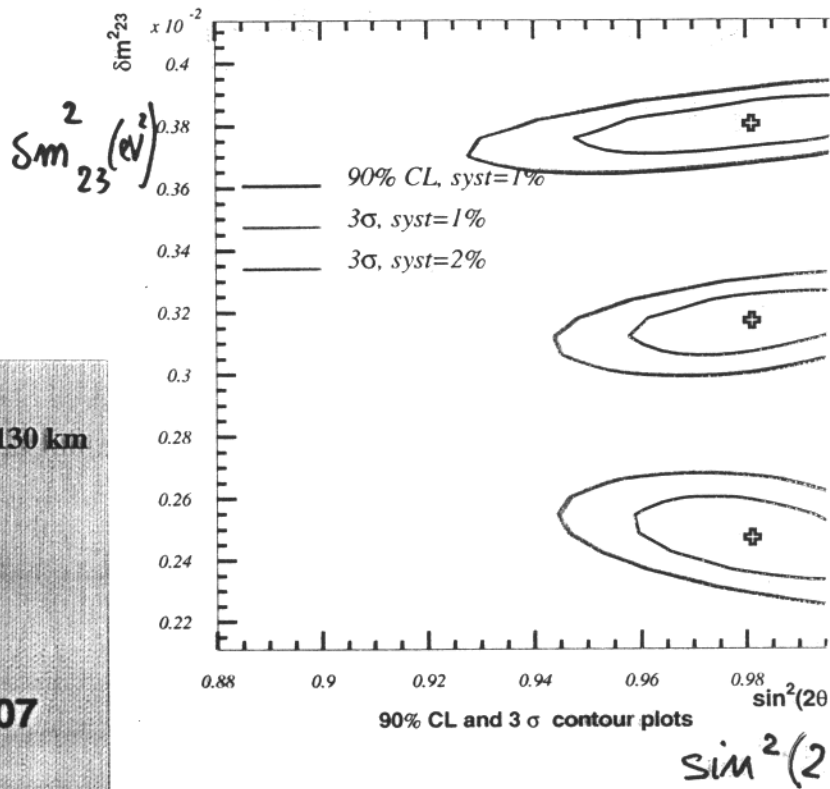
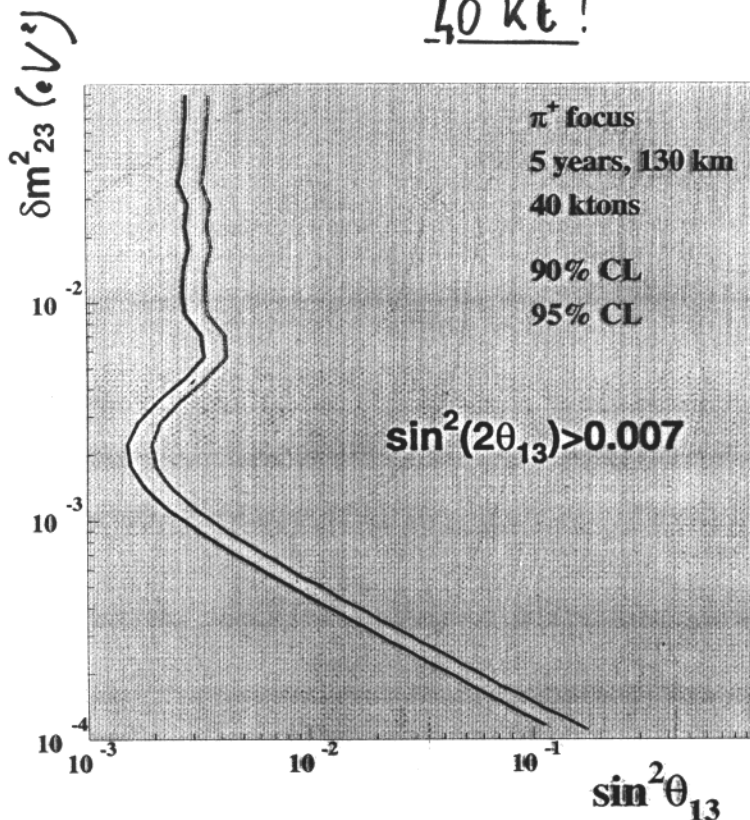
$$(\nu_e/\nu_\mu \sim 0.4\%)$$

- close / far detectors: syst. error $\sim 2\%$

$$\nu_\mu \rightarrow \nu_e \text{ appearance!}$$

... expected sensitivity

5 years!
40 kt!



- $\sin^2(2\theta_{13}) > 0.007$

- $\sin^2(2\theta_{23}), |\Delta m_{23}^2|$ within $\sim 2\%$

- poor sensitivity to δP , $\delta = 0^\circ$ separated from $\delta = 90^\circ$
in a small region of parameters $\Rightarrow 400 \text{ kt}?$

- JHF project 50 GeV/c protons (PS), 0.77 MW ($\rightarrow 4 \text{ MW}$)

$\sim 1 \text{ GeV } \nu_\mu \text{ beam} \rightarrow \text{S.K. } L = 295 \text{ km}$

5000 $\nu_\mu \text{ cc/year} \dots 3.3 \cdot 10^{14} \text{ P}/3.45 \cdot 10^{21} \text{ P/year}$

but... a real conventional ν beam... κ/π ?

sensitivity $\simeq \text{CERN-MODANE exp. } 23$

APPROVED
 $\sim 2007!$

Conclusions

- conventional ν beams @ accelerators
 - will hopefully confirm ν oscillations
 - predicted 45 years ago by B. Pontecorvo -
 - as a first signal of new phenomena
 - beyond the Standard Model -
- νF based on μ -decay: the only way we know
to produce a ν beam suitable for solve
the ν oscillation puzzle and
investigate CP in leptons !
- superbeams: only a first step toward νF ?
 - A.O.B. ?