

Unified Analysis of Solar and Atmospheric Neutrino Data

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OUTLINE

1. Introduction

- *The solar neutrino problem*
- *The atmospheric neutrino problem*

2. Three-neutrino oscillations

- *Unified analysis of solar neutrino data*
- *Global analysis of atmospheric neutrino data (including Chooz)*
- *Combined analysis of solar, atmospheric and reactor results*

3. Four-neutrino oscillations

- *Active vs sterile in solar and atmospheric experiments*
- *Combined analysis of solar and atmospheric ν*

4. Conclusions

Based on

- ⇒ M.C. Gonzalez-Garcia, M.M., C. Peña-Garay, J.W.F. Valle, *Global three-neutrino oscillation analysis of neutrino data*, *Phys. Rev.* **D63** (2001) 033005, [hep-ph/0009350](https://arxiv.org/abs/hep-ph/0009350).
- ⇒ M.C. Gonzalez-Garcia, M.M., C. Peña-Garay, *Solar and Atmospheric Four-Neutrino Oscillations*, [hep-ph/0105269](https://arxiv.org/abs/hep-ph/0105269) (to appear in PRD).

Three-neutrino oscillation parameters

- Equation of motion: 5 parameters (neglecting CP violating effects):

$$i \frac{d\vec{\nu}}{dt} = \mathbf{H} \vec{\nu}; \quad \mathbf{H} = \mathbf{O} \cdot \mathbf{H}_0^d \cdot \mathbf{O}^\dagger + \mathbf{V};$$

$$\mathbf{O} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23} & c_{12}c_{23} - s_{12}s_{13}s_{23} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23} & -c_{12}s_{23} - s_{12}s_{13}c_{23} & c_{13}c_{23} \end{pmatrix}, \quad \vec{\nu} = \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix};$$

$$\mathbf{H}_0^d = \frac{1}{2E_\nu} \text{diag}(-\Delta m_{21}^2, 0, \Delta m_{32}^2);$$

$$\mathbf{V} = \text{diag}(\pm \sqrt{2}G_F N_e, 0, 0);$$

- from solar ν data: $\Delta m_{21}^2 \ll \Delta m_{32}^2$.

Atmospheric case

- Simplifying assumption: $\Delta m_{21}^2 \approx 0 \Rightarrow$ get rid also of θ_{12} :

$$\mathbf{O} = \begin{pmatrix} c_{13} & 0 & s_{13} \\ -s_{13}s_{23} & c_{23} & c_{13}s_{23} \\ -s_{13}c_{23} & -s_{23} & c_{13}c_{23} \end{pmatrix}, \quad \mathbf{H}_0^d = \frac{1}{2E_\nu} \text{diag}(0, 0, \Delta m_{32}^2);$$

\Rightarrow only 3 parameters left.

Solar case

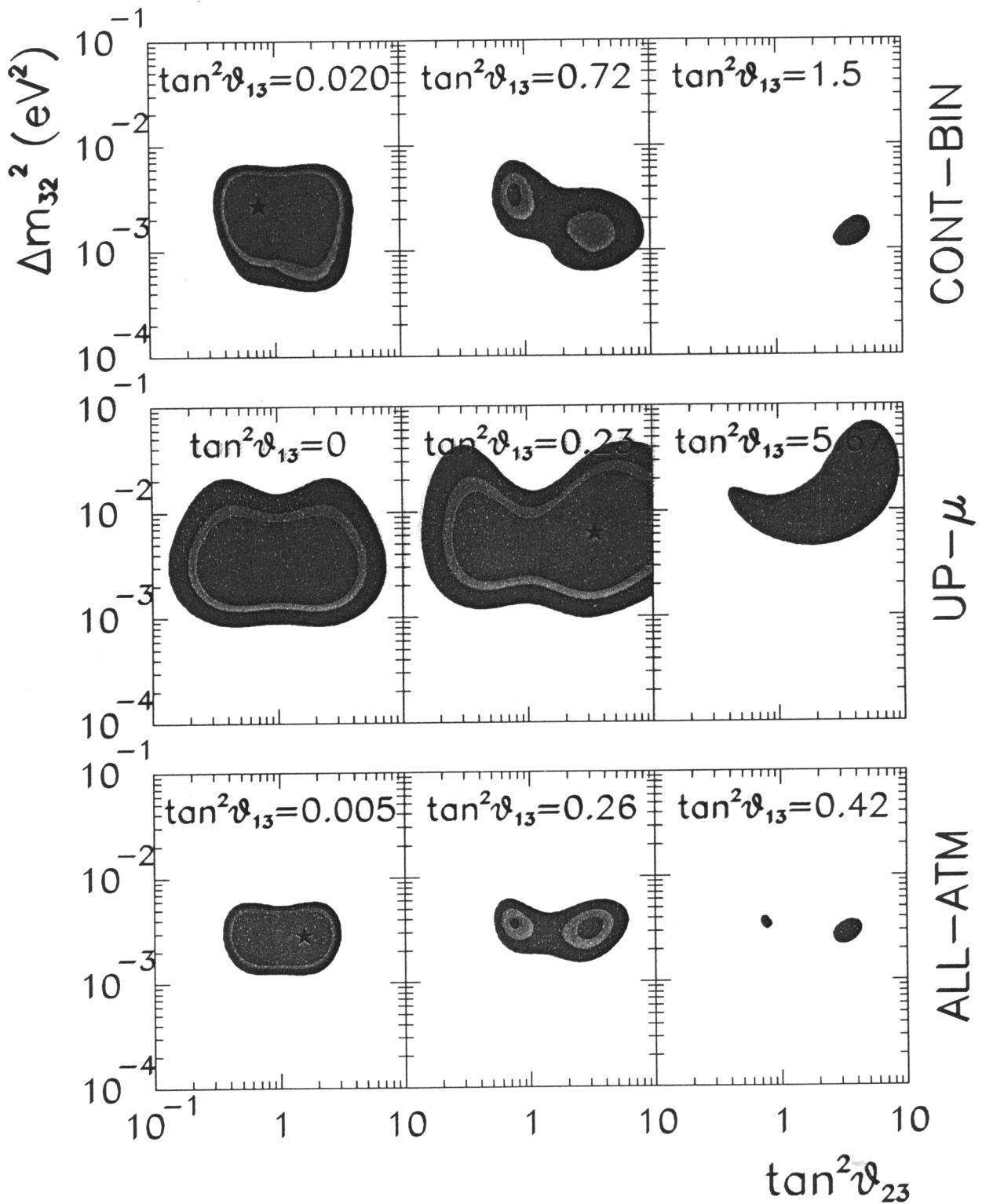
- Simplifying assumption: $\Delta m_{32}^2 \approx \infty$;
- moreover, θ_{23} cancels out from P_{ee} :

$$\mathbf{O} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13} \\ -s_{12} & c_{12} & 0 \\ -c_{12}s_{13} & -s_{12}s_{13} & c_{13} \end{pmatrix}, \quad \mathbf{H}_0^d = \frac{1}{2E_\nu} \text{diag}(-\Delta m_{21}^2, 0, \infty);$$

\Rightarrow again, only 3 parameters left.

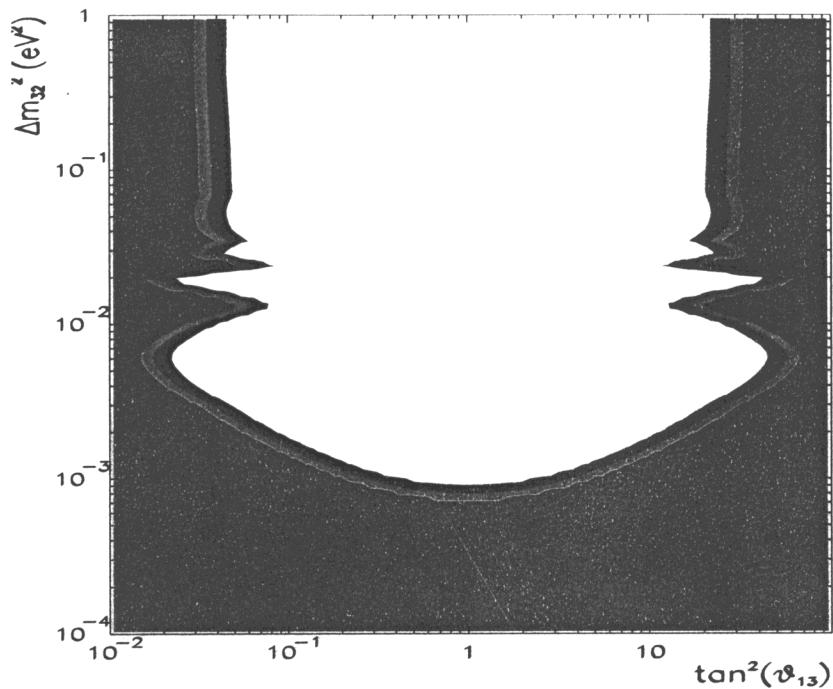
Contained and Upgoing events

Bound	Contained	Upgoing- μ	Combined
Δm_{32}^2 , upper	strong	weak	strong
Δm_{32}^2 , lower	weak	strong	strong
$\tan^2 \theta_{13}$	mild	weak	strong

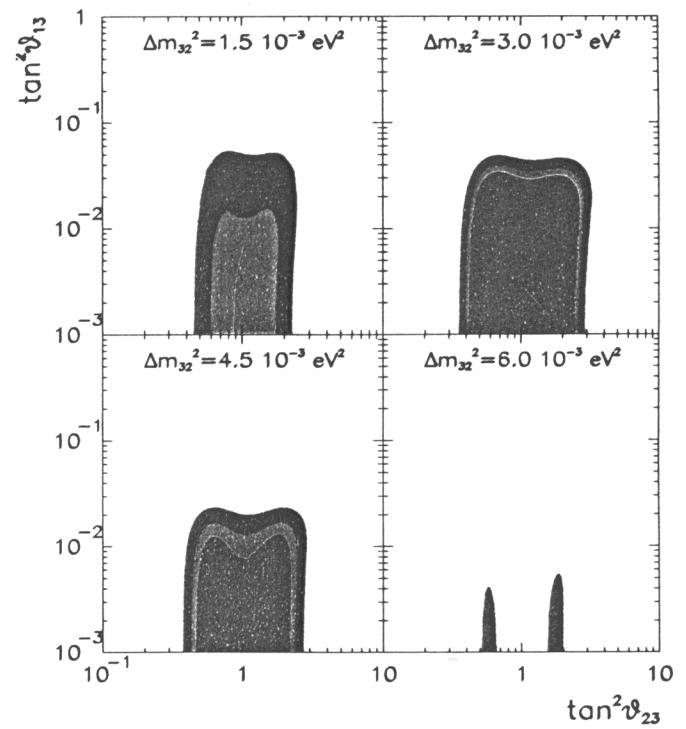
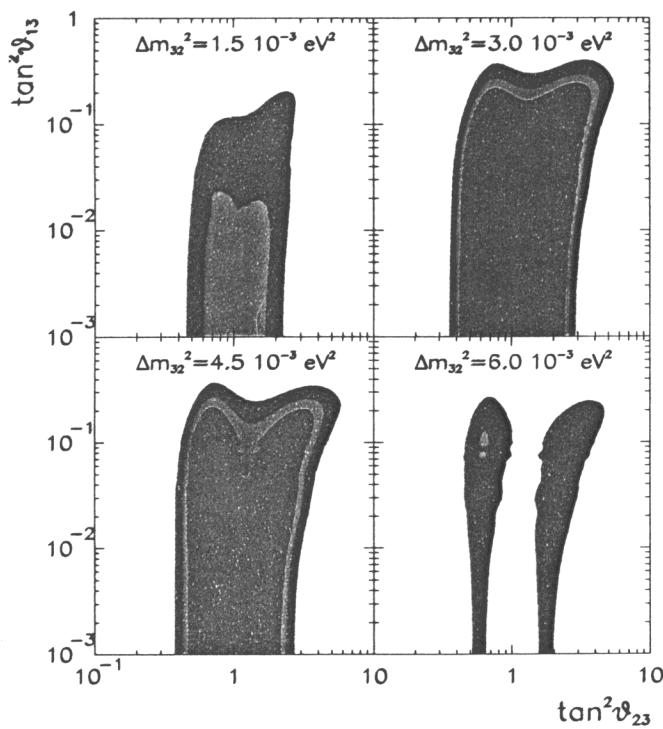


The CHOOZ experiment

- Bound from *non-observation* of $\bar{\nu}_e$ disappearance;
- from solar data: $\Delta m_{21}^2 \ll 10^{-3} \text{ eV}^2 \Rightarrow \text{NO bound}$ on $\tan^2 \theta_{23}$;
- Excluded region: $\Delta m_{32}^2 \gtrsim 10^{-3} \text{ eV}^2$, $0.03 \lesssim \tan^2 \theta_{13} \lesssim 30$.

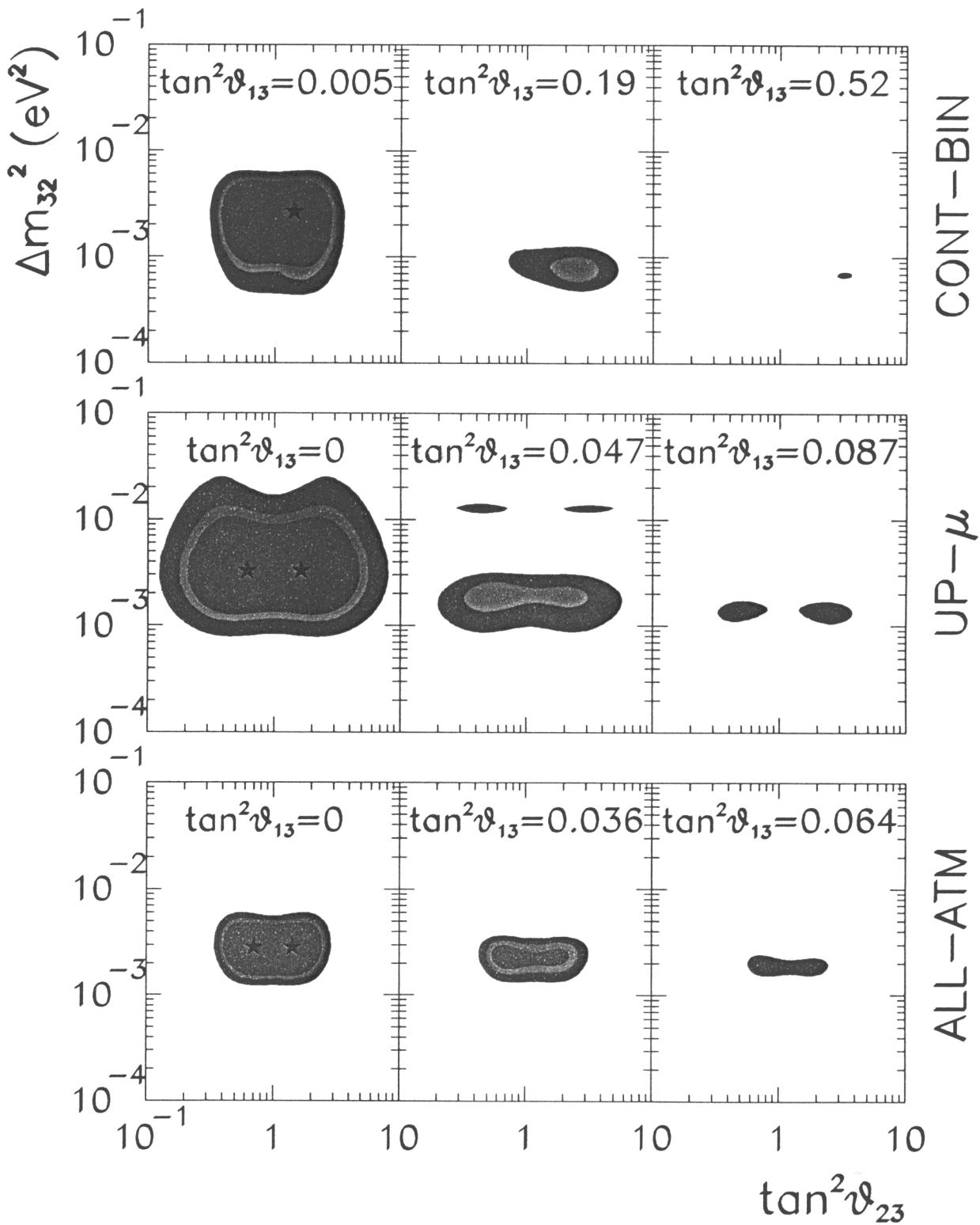


Contour regions in the $(\tan^2 \theta_{13}, \tan^2 \theta_{23})$ plane



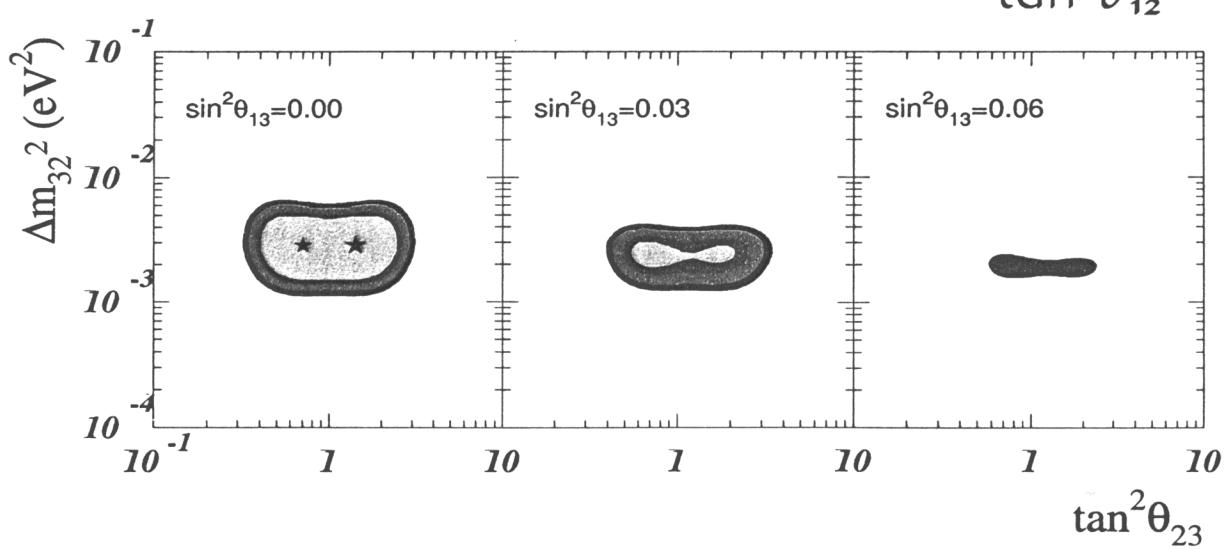
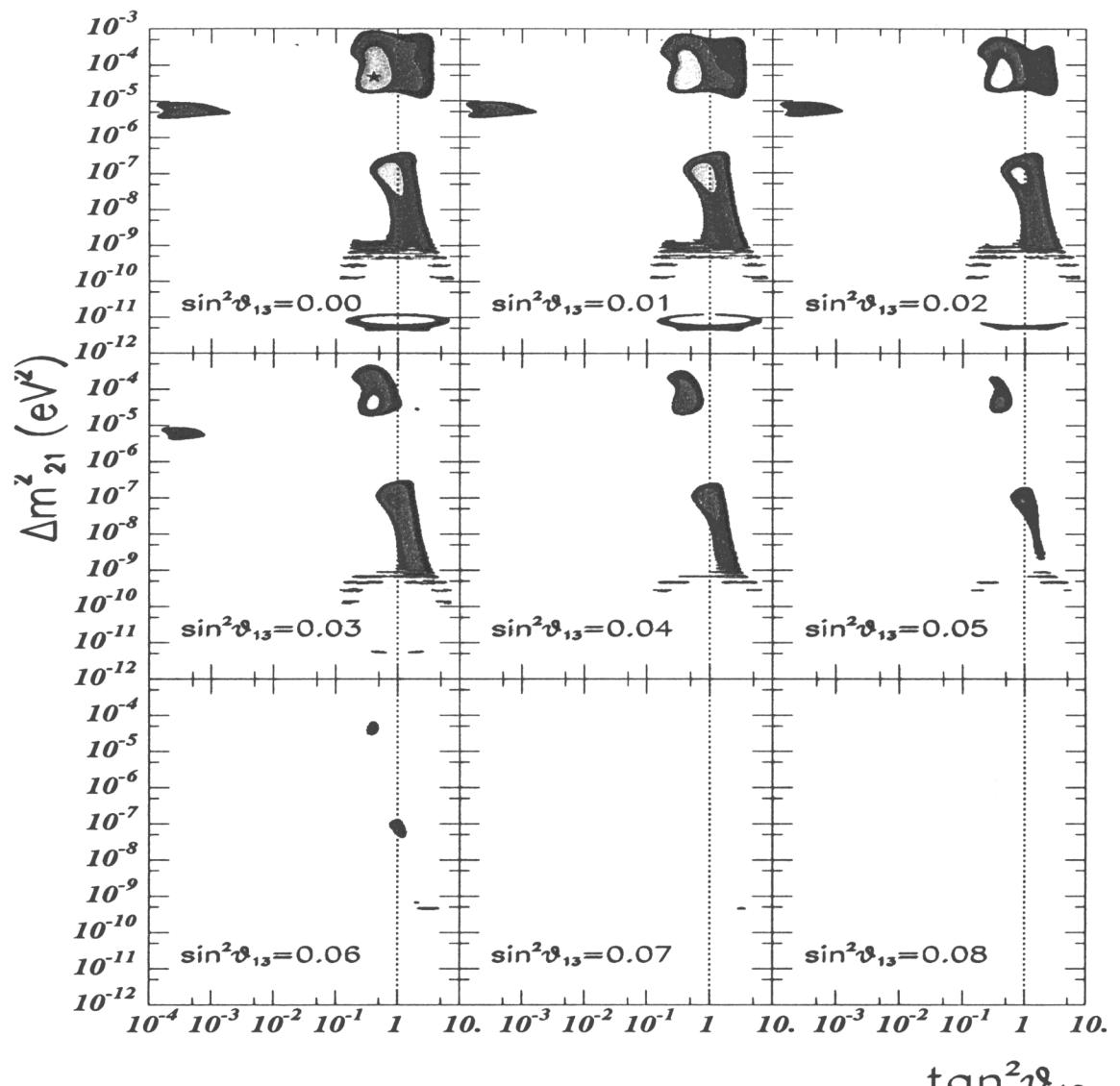
Effect of Chooz on the Atmospheric results

Bound	Contained	Upgoing- μ	Combined
Δm_{32}^2 , upper	strong	weak	strong
Δm_{32}^2 , lower	weak	strong	strong
$\tan^2 \theta_{13}$	mild	very strong	very strong



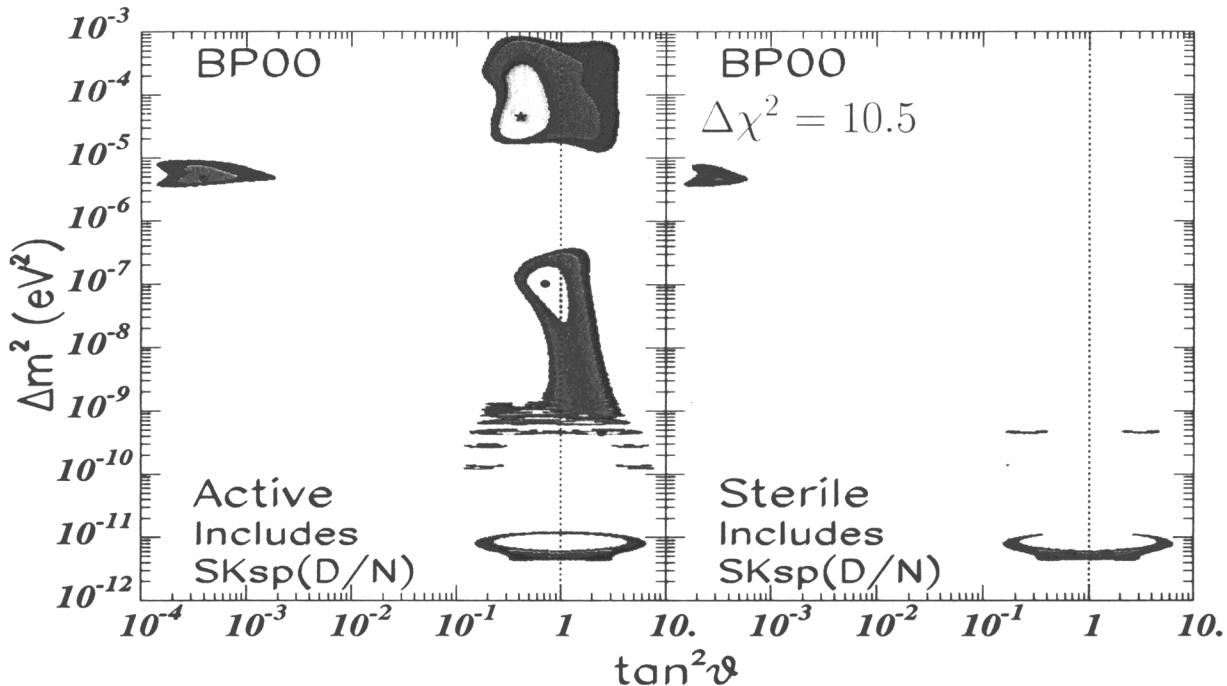
GLOBAL: combined Solar + ATM + Reactor analysis

- Homestake • SAGE+GALLEX/GNO ★ SK-1258 • SNO-CC
- ★ ATM-ALL • Chooz

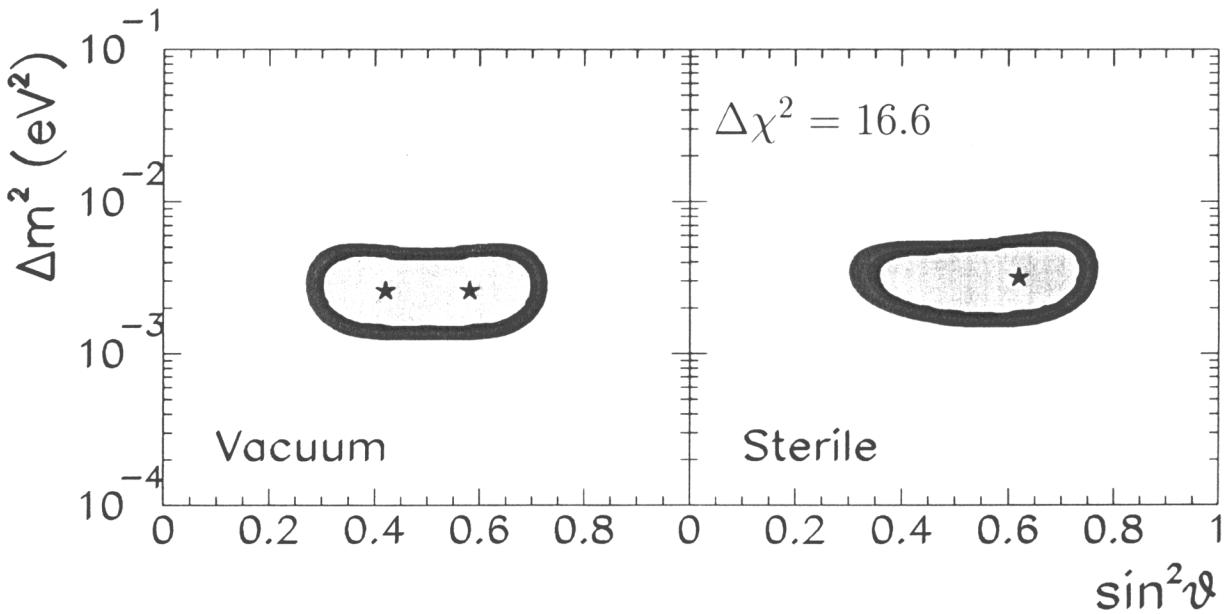


Four neutrino oscillations

- A 4th light ν is needed to reconcile LSND with Solar and ATM results;
- Z width in agreement with SM \Rightarrow new neutrino must be *sterile*;
- however, solar data disfavour ν_e oscillations into a sterile state...



- ... and atmospheric data also disfavour $\nu_\mu \rightarrow \nu_s$ oscillations:



- therefore, 2ν analyses of solar and atmospheric data seems incompatible;
 \Rightarrow a global and unified 4ν analysis is needed.

Four-neutrino oscillation parameters

- Equation of motion: 9 parameters (neglecting CP violating effects):

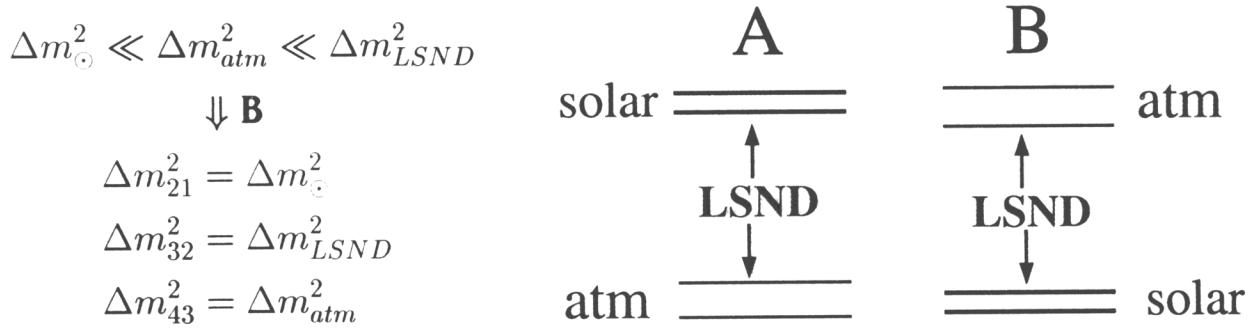
$$i \frac{d\vec{\nu}}{dt} = \mathbf{H} \vec{\nu}; \quad \mathbf{H} = \mathbf{O} \cdot \mathbf{H}_0^d \cdot \mathbf{O}^\dagger + \mathbf{V};$$

$$\mathbf{O} = \mathbf{O}_{24}(\theta_{24}) \cdot \mathbf{O}_{23}(\theta_{23}) \cdot \mathbf{O}_{14}(\theta_{14}) \cdot \mathbf{O}_{13}(\theta_{13}) \cdot \mathbf{O}_{34}(\theta_{34}) \cdot \mathbf{O}_{12}(\theta_{12}); \quad \vec{\nu} = \begin{pmatrix} \nu_e \\ \nu_s \\ \nu_\mu \\ \nu_\tau \end{pmatrix};$$

$$\mathbf{H}_0^d = \frac{1}{2E_\nu} \text{diag}(-\Delta m_{21}^2, 0, \Delta m_{32}^2, \Delta m_{32}^2 + \Delta m_{43}^2);$$

$$\mathbf{V} = \pm \sqrt{2} G_F \text{diag}\left(N_e, \frac{1}{2}N_n, 0, 0\right);$$

- 3 + 1 models are now disfavoured. In 2 + 2 models:



- from the result of the Bugey experiment:

$$|O_{e3}|^2 + |O_{e4}|^2 = c_{14}^2 s_{13}^2 + s_{14}^2 \lesssim 10^{-2} \Rightarrow \theta_{13} \approx \theta_{14} \approx 0;$$

- simplified form of the \mathbf{O} matrix:

$$\mathbf{O} = \begin{pmatrix} c_{12} & s_{12} & 0 & 0 \\ -s_{12}c_{23}c_{24} & c_{12}c_{23}c_{24} & -s_{34}s_{24} + c_{34}s_{23}c_{24} & c_{34}s_{24} + s_{34}s_{23}c_{24} \\ s_{12}s_{23} & -c_{12}s_{23} & c_{34}c_{23} & s_{34}c_{23} \\ s_{12}c_{23}s_{24} & -c_{12}c_{23}s_{24} & -s_{34}c_{24} - c_{34}s_{23}s_{24} & c_{34}c_{24} - s_{34}s_{23}s_{24} \end{pmatrix}.$$

Atmospheric case

- $\Delta m_{21}^2 \approx 0, \Delta m_{32}^2 \approx \infty;$
 - θ_{12} cancels out $\Rightarrow \nu_e$ decouples;
 - θ_{23} and θ_{24} contribute separately;
- $\Rightarrow 4 (= 1_m + 3_\theta)$ parameters left.

Solar case

- $\Delta m_{32}^2 \approx \infty, \Delta m_{43}^2 \approx \infty;$
 - θ_{34} does not contribute to P_{ee} ;
 - only $c_{23}^2 c_{24}^2$ appears in P_{ee} ;
- $\Rightarrow 3 (= 1_m + 2_\theta)$ parameters left.

SOLAR PARAMETERS

- $\Delta m_{\odot}^2, \vartheta_{12}$: RELEVANT MASS-SQUARED DIFF., MIXING ANGLE;
- $c_{23}^2 c_{24}^2 = |U_{S1}|^2 + |U_{S2}|^2$: ACTIVE-STERILE ADMIXTURE;
- CASES:
 - $c_{23}^2 c_{24}^2 = 0 \Rightarrow$ PURE $\nu_e \rightarrow \nu_{\text{ACTIVE}}$ OSCILLATIONS;
 - $c_{23}^2 c_{24}^2 = 1 \Rightarrow$ PURE $\nu_e \rightarrow \nu_{\text{STERILE}}$ OSCILLATIONS.

ATMOSPHERIC PARAMETERS

- $\Delta m_{\text{ATM}}^2, \vartheta_{34}$: RELEVANT OSCILLATION-PARAMETERS;
- $c_{23}^2 c_{24}^2 = |U_{S1}|^2 + |U_{S2}|^2$: ACTIVE-STERILE ADMIXTURE;
- $c_{23}^2 = |U_{M3}|^2 + |U_{M4}|^2$: ν_μ PROJECTION ON ATM STATES.
- CASES:
 - $c_{23}^2 = 0 \Rightarrow$ NO ATMOSPHERIC ν_μ OSCILLATIONS;
 - $c_{23}^2 = 1 \Rightarrow$ "RESTRICTED" CASE:
 - $c_{23}^2 c_{24}^2 = 0 \Rightarrow$ PURE $\nu_\mu \rightarrow \nu_s$ OSCILLATIONS;
 - $c_{23}^2 c_{24}^2 = 1 \Rightarrow$ PURE $\nu_\mu \rightarrow \nu_\tau$ OSCILLATIONS.

* s_{23}^2 LIMITED BY THE ATM ANALYSIS;

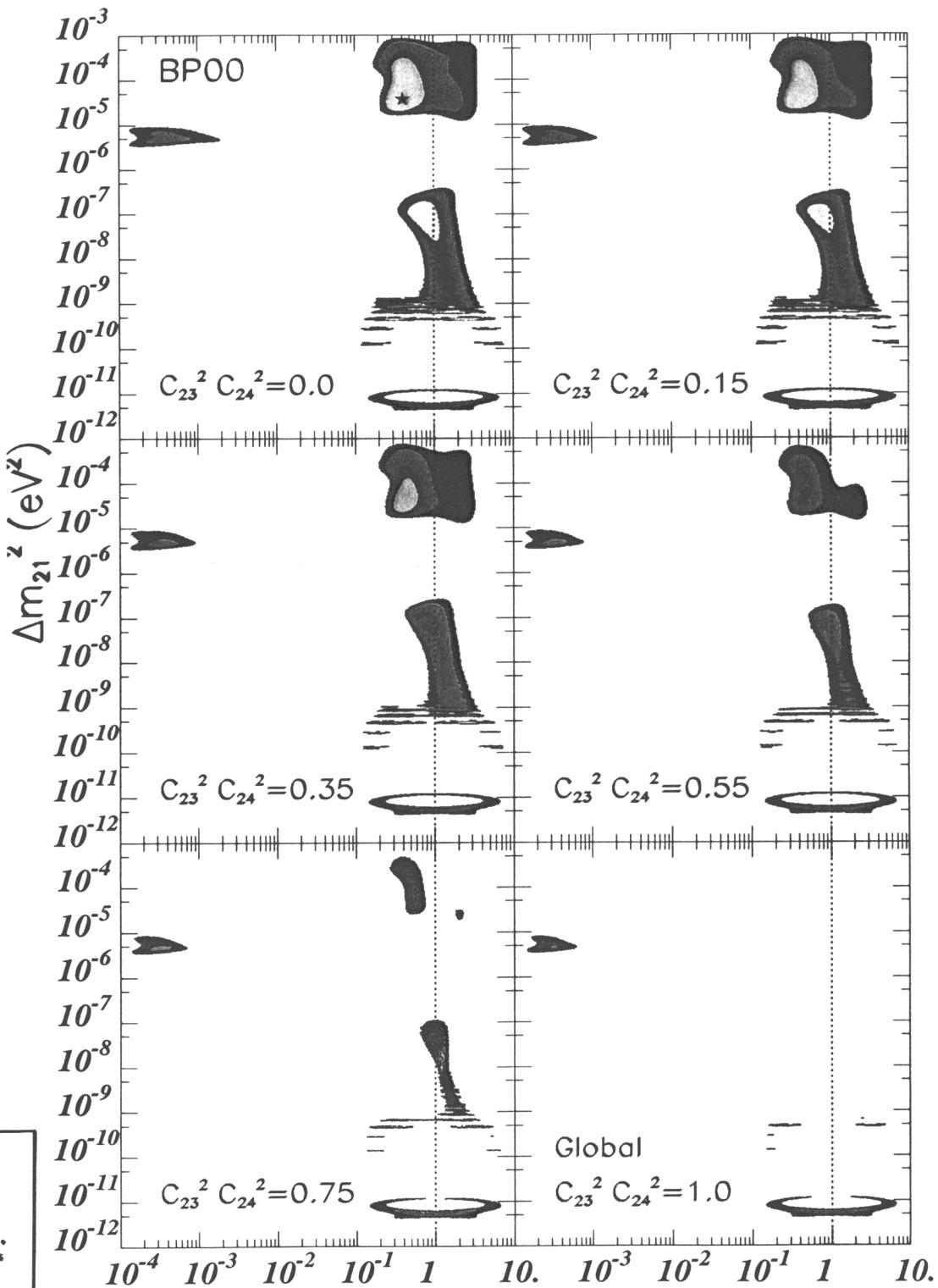
* ALSO ν_μ DISAPP. SEARCHES AT CDHSW $\Rightarrow s_{23}^2 \lesssim 0.2$.

PARAMETER RANGES.

- $\Delta m_{\odot}^2 \geq 0 ; \Delta m_{\text{ATM}}^2 \geq 0$;
- $0 \leq \vartheta_{12} \leq \pi/2 \Rightarrow 0 \leq \tan^2 \vartheta_{12} \leq +\infty$;
- $0 \leq \vartheta_{23} \leq \pi/2 \& 0 \leq \vartheta_{24} \leq \pi/2 \Rightarrow 0 \leq c_{23}^2 c_{24}^2 \leq 1 \& 0 \leq s_{23}^2 \leq 1$;
- $-\pi/2 \leq \vartheta_{34} \leq \pi/2 \Rightarrow -1 \leq \text{sgn}(\vartheta_{34}) \sin^2(\vartheta_{34}) \leq +1$.

Active vs Sterile: Solar case

- Homestake • SAGE+GALLEX/GNO ★ SK-1258 • SNO-CC
- ⇒ Best fit point: LMA, $c_{23}^2 c_{24}^2 = 0$; SMA strongly disfavoured;
- ⇒ however, for large values of $c_{23}^2 c_{24}^2$ the LMA region disappears.

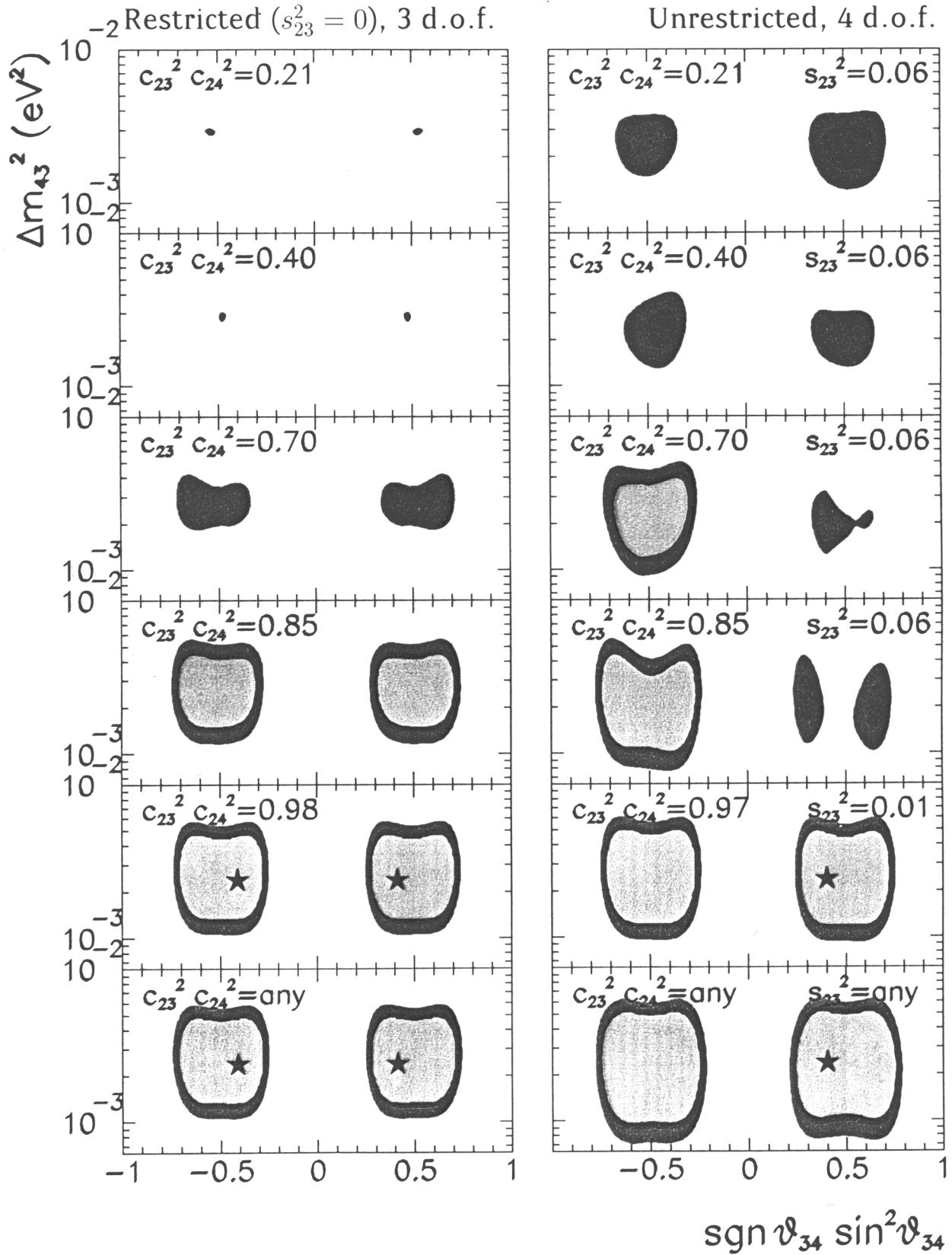


C.L.	SMA	LMA	LOW
90%	≥ 0.0	≥ 0.45	≥ 0.4
99%	NEVER	≥ 0.72	≥ 0.99

$\tan^2 \theta_{12}$

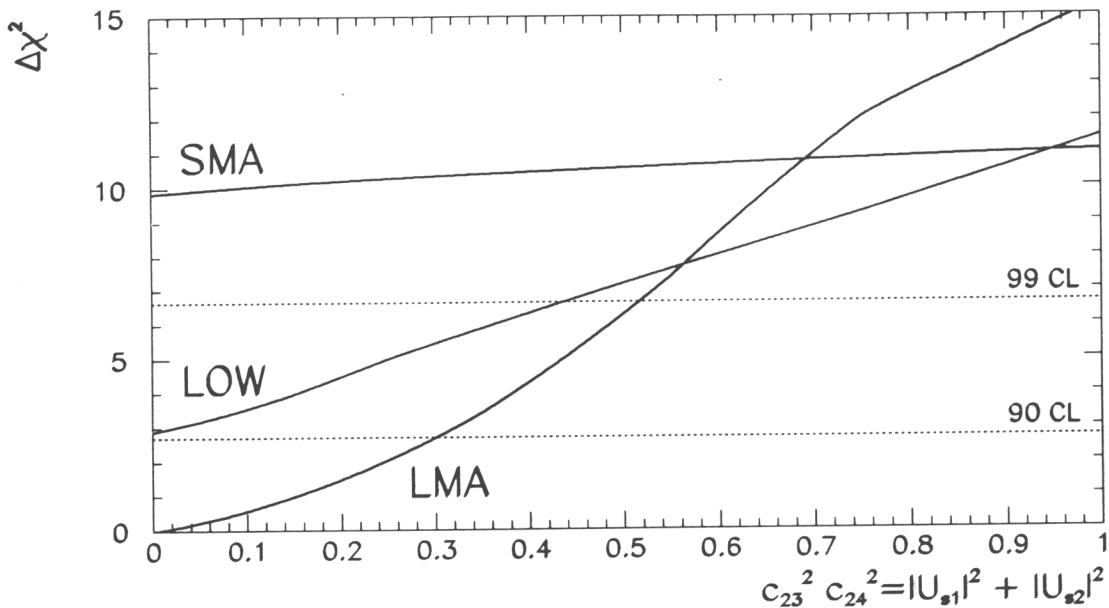
Active vs Sterile: Atmospheric case

- ★ SK sub-GeV ★ SK stopping μ ★ Macro
- ★ SK multi-GeV ★ SK thru-going μ

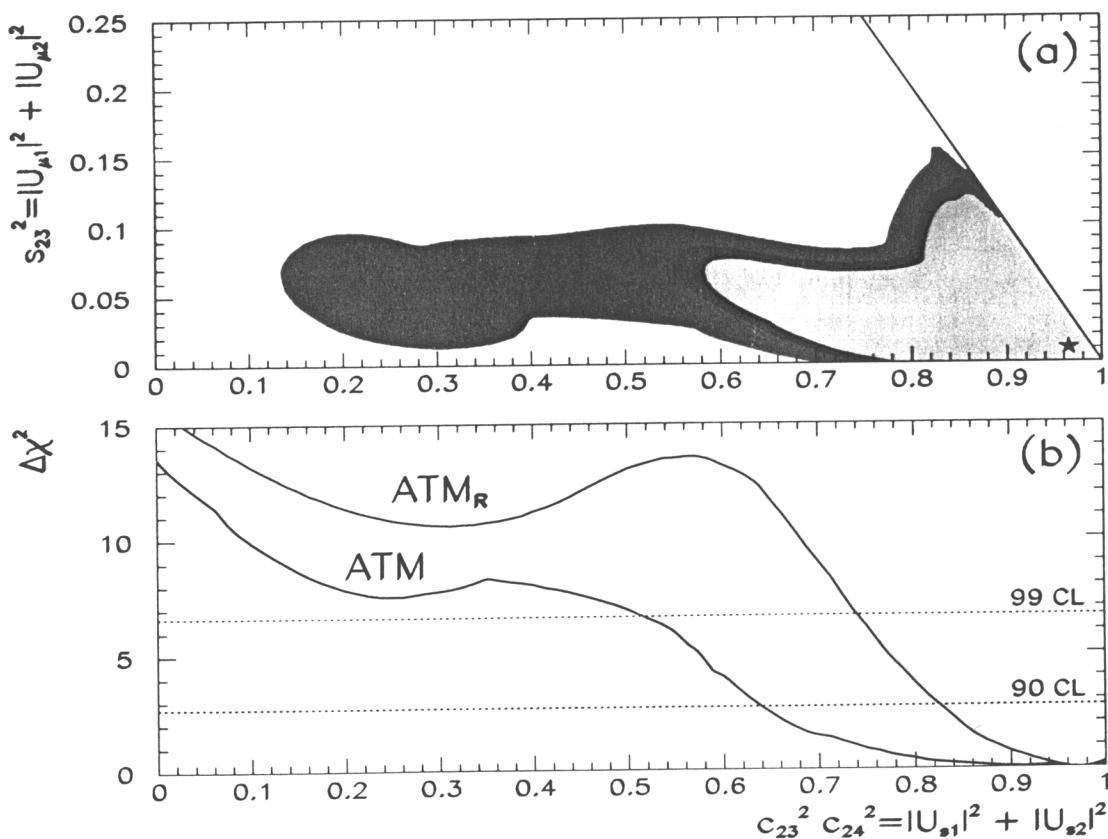


Active/sterile admixture in Solar & Atmospheric

- Solar case: $c_{23}^2 c_{24}^2 = 0$ preferred, but larger values allowed:

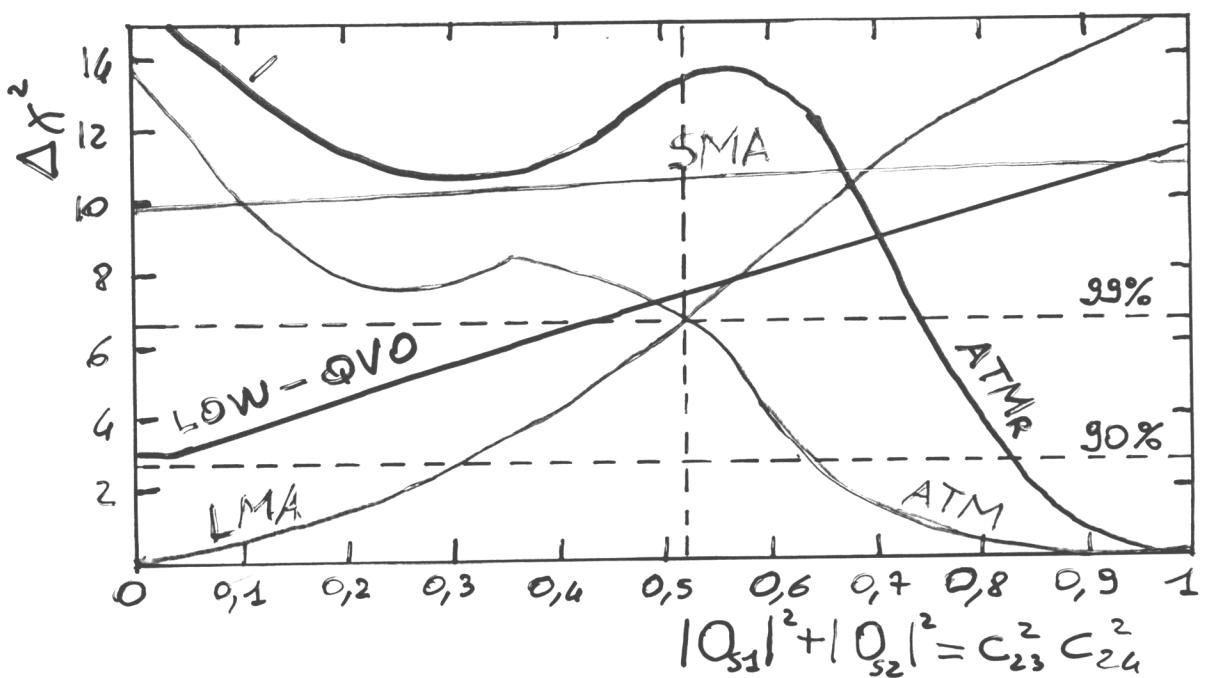


- Atmospheric case: $c_{23}^2 c_{24}^2 \approx 1$ preferred, but smaller values possible:



⇒ a chance for maximal active-sterile admixture?

SOLAR VS. ATMOSPHERIC DATA

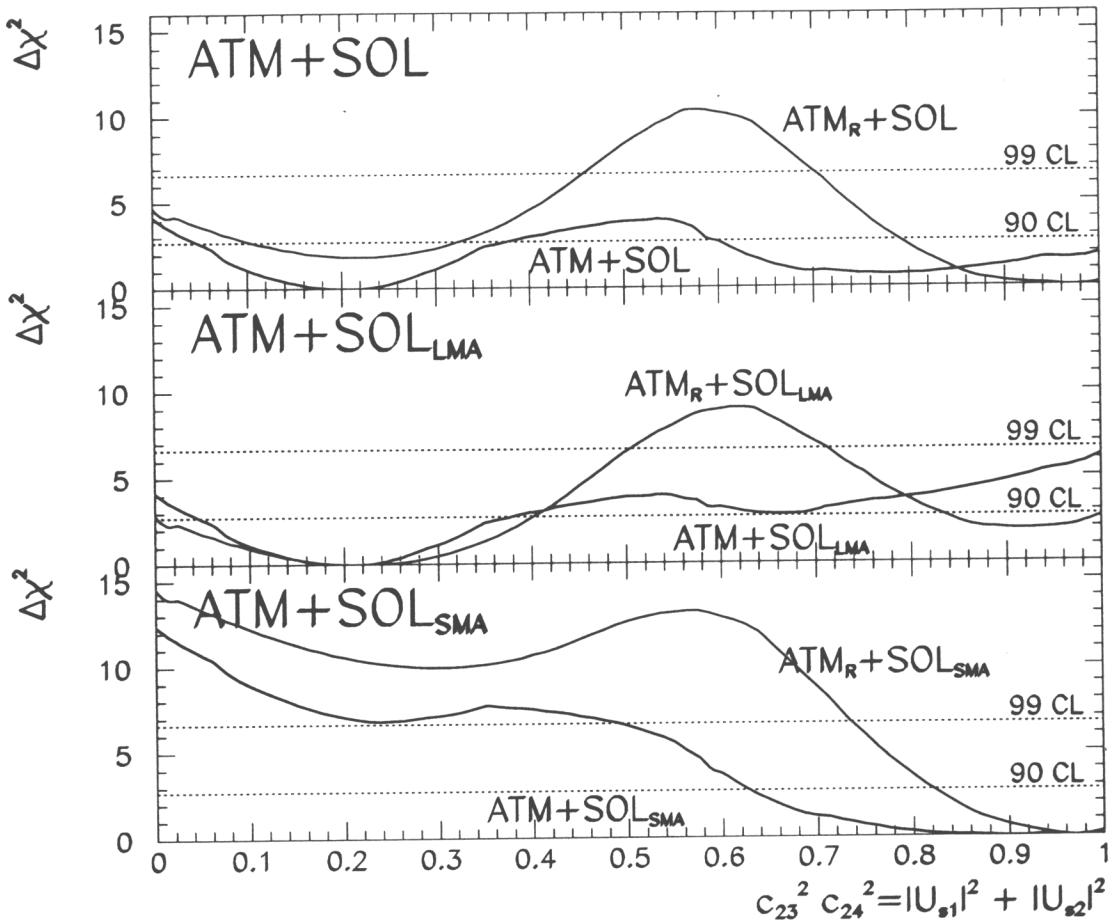


- NAIVELY :

- SOLAR : $c_{23}^2 c_{24}^2 \leq 0.52$ AT 99% C.L.
- ATM : $c_{23}^2 c_{24}^2 \geq 0.52$ AT 99% C.L.

Combined analysis

- Maximal active-sterile admixture is newer preferred:



- there are always two local minima;
- in the *unconstrained* and *LMA* cases, $c_{23}^2 c_{24}^2 \approx 0.2$ is preferred;
- in the *SMA* case, $c_{23}^2 c_{24}^2 \approx 1$ is preferred;
 - after SNO, the *SMA* solution is (slightly) disfavoured;
 - however, in the ATM_R case the *SMA* solution is still preferred.

Scenario	d.o.f.	s_{23}^2	$c_{23}^2 c_{24}^2$	χ^2_{\min}	GOF
$ATM + SOL_{unc}$	$85 - 6$	0.065	0.21	73.8	64%
$ATM_R + SOL_{unc}$	$85 - 5$	0.	0.98	75.5	62%
$ATM + SOL_{LMA}$	$85 - 6$	0.065	0.21	73.8	64%
$ATM_R + SOL_{LMA}$	$85 - 5$	0.	0.22	77.4	56%
$ATM + SOL_{SMA}$	$85 - 6$	0.030	0.91	75.4	59%
$ATM_R + SOL_{SMA}$	$85 - 5$	0.	0.98	75.5	62%

Conclusions

- We have performed a global and unified analysis of both solar and atmospheric neutrino data in the context:
 - of 3ν oscillations, using taking into account also the Chooz result;
 - of 4ν oscillations, in the framework of $2 + 2$ schemes.
- we included in our fit:
 - all the solar experiments, with SK-1258 data and SNO_{CC} rates;
 - all the atmospheric experiments for the 3ν analysis, and SK (1289 days) + MACRO for the 4ν analysis.

3ν results

- both solar and atmospheric data are in strong disagreement with the SM, however can be perfectly explained by the *oscillation hypothesis*;
- even without the reactor data $\theta_{13} \approx 0$ is preferred;
- there is *full agreement* between solar, atmospheric and reactor results.

⇒ M.C. Gonzalez-Garcia, M.M., C. Peña-Garay, J.W.F. Valle, *Global three-neutrino oscillation analysis of neutrino data*, Phys. Rev. D63 (2001) 033005, [hep-ph/0009350](#).

4ν results

- neither solar nor atm data favour oscillations into a sterile neutrino;
 - maximal active/sterile admixture is *always* disfavoured;
 - the best fit point has $|U_{s1}|^2 + |U_{s2}|^2 \approx 0.2$, is dominated by solar data and favours in the *LMA* solution;
 - however, another configuration with $|U_{s1}|^2 + |U_{s2}|^2 \approx 1$, dominated by atmospheric data and favoured by the *SMA* solution, is also possible.
- ⇒ M.C. Gonzalez-Garcia, M.M., C. Peña-Garay, *Solar and Atmospheric Four-Neutrino Oscillations*, [hep-ph/0105269](#) (to appear in PRD).