

*Extremely High Energy Cosmic Neutrinos  
and Relic Neutrinos*

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*Fermilab & CERN*

NO-VE · 9 February 2006

# I Neutrino Observatories: Expectations

Cosmic  $\nu$  flux may exceed atmospheric background at  $E_\nu \approx$  few TeV

*prospect for sources · characterize sources · study  $\nu$  properties*

Sources include AGN (at  $\sim 10^2$  Mpc)

1 Mpc  $\approx 3.1 \times 10^{22}$  m

*pp or p $\gamma$   $\Rightarrow$   $\approx$  numbers of  $\pi^+$   $\pi^0$   $\pi^-$*

*$\pi^+ + \pi^0 + \pi^- \Rightarrow 2\gamma + 2\nu_\mu + 2\bar{\nu}_\mu + 1\nu_e + 1\bar{\nu}_e$*

$$\Phi_{\text{std}}^0 = \left\{ \varphi_e^0 = \frac{1}{3}, \varphi_\mu^0 = \frac{2}{3}, \varphi_\tau^0 = 0 \right\} \quad (\nu = \bar{\nu})$$

Detection (in volumes  $\rightarrow 1 \text{ km}^3$ )

$$(\nu_\mu, \bar{\nu}_\mu)N \rightarrow (\mu^-, \mu^+) + \text{anything}$$

Can we achieve efficient, calibrated  $(\nu_e, \bar{\nu}_e)$  detection?

Good  $(\nu_\tau, \bar{\nu}_\tau)$  detection, NC capability desirable

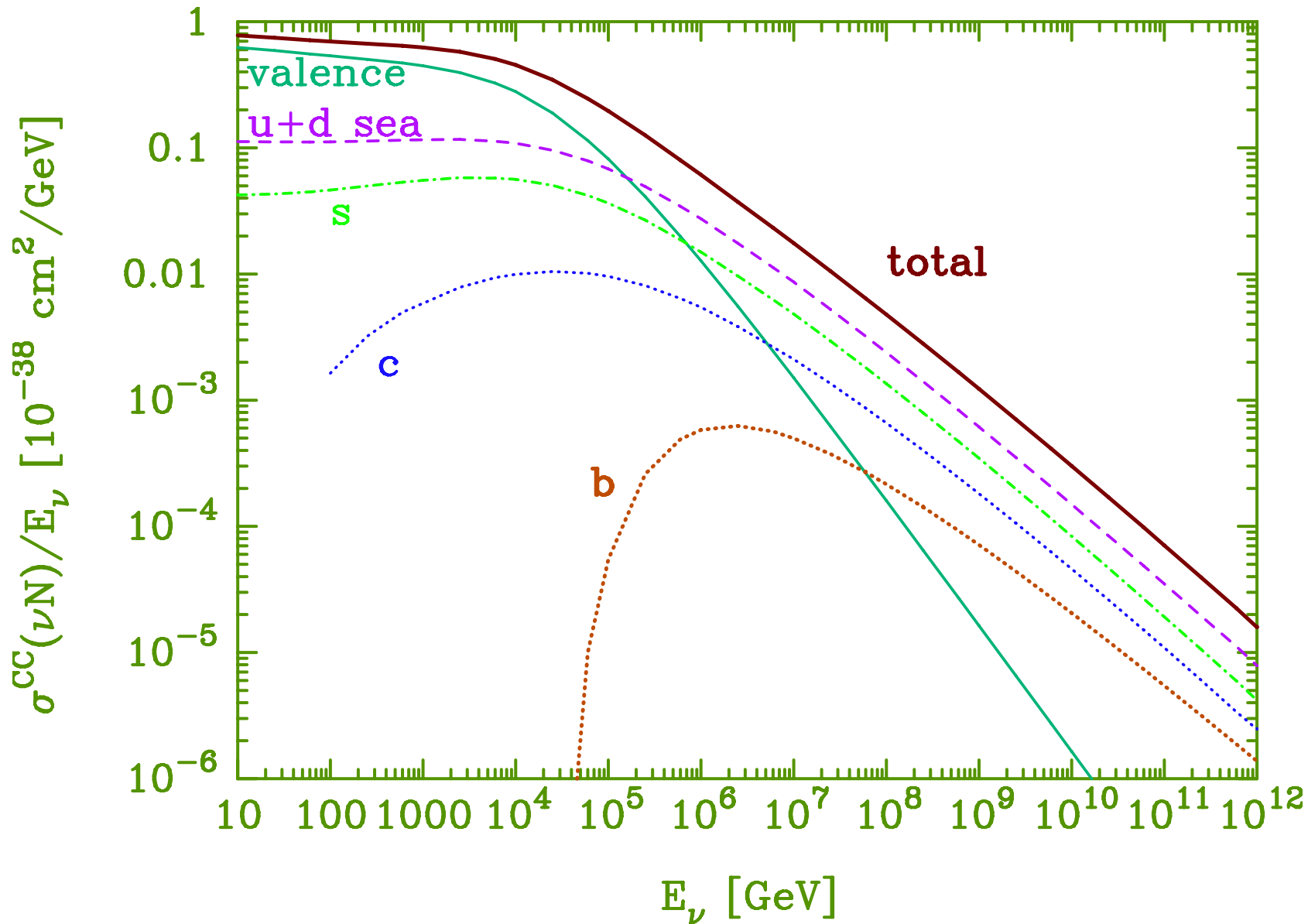
$$\nu_\mu N \rightarrow \mu^- + \text{anything}$$

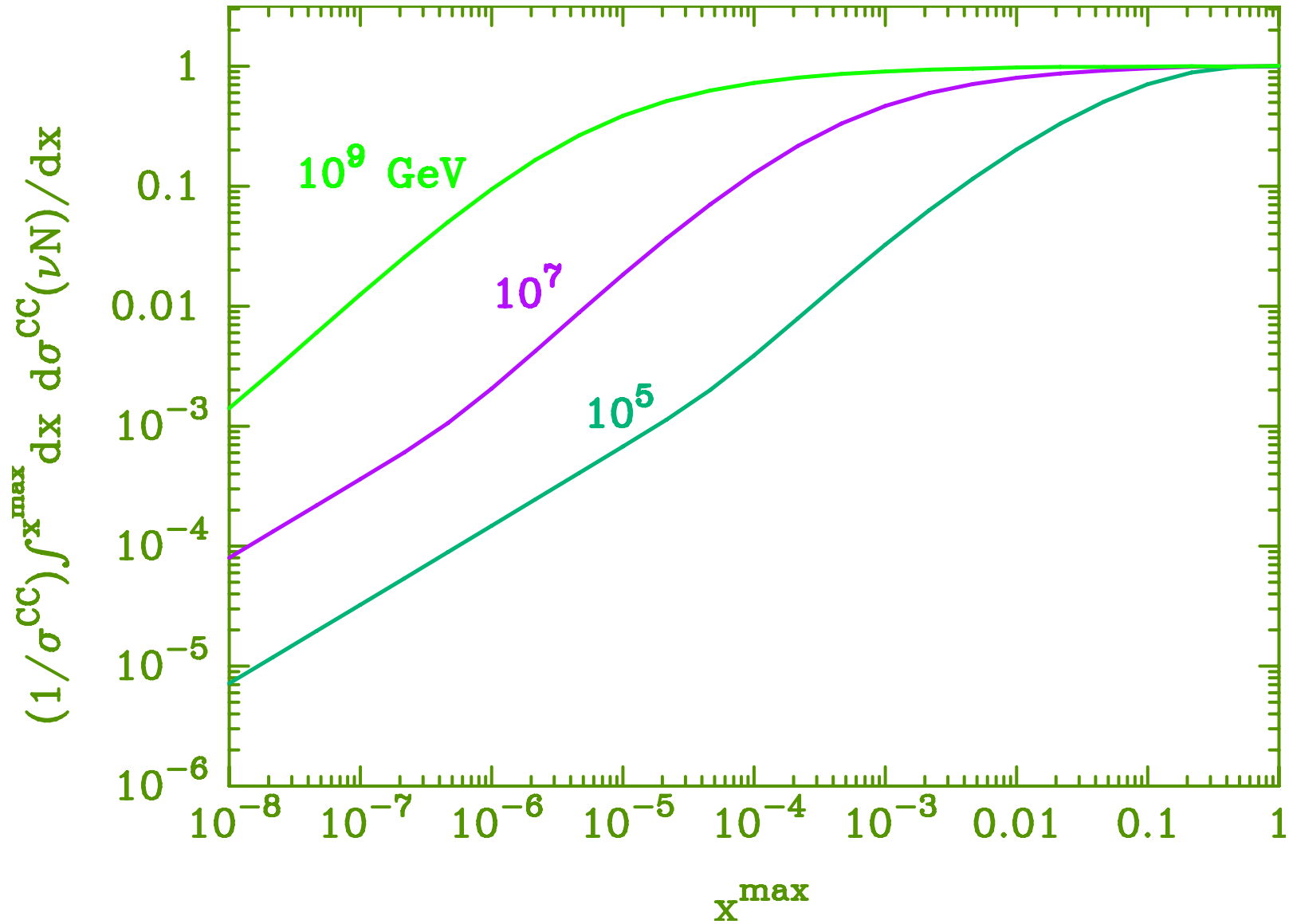
$$\frac{d^2\sigma}{dxdy} = \frac{2G_F^2 M E_\nu}{\pi} \left( \frac{M_W^2}{Q^2 + M_W^2} \right)^2 [xq(x, Q^2) + x\bar{q}(x, Q^2)(1-y)^2]$$

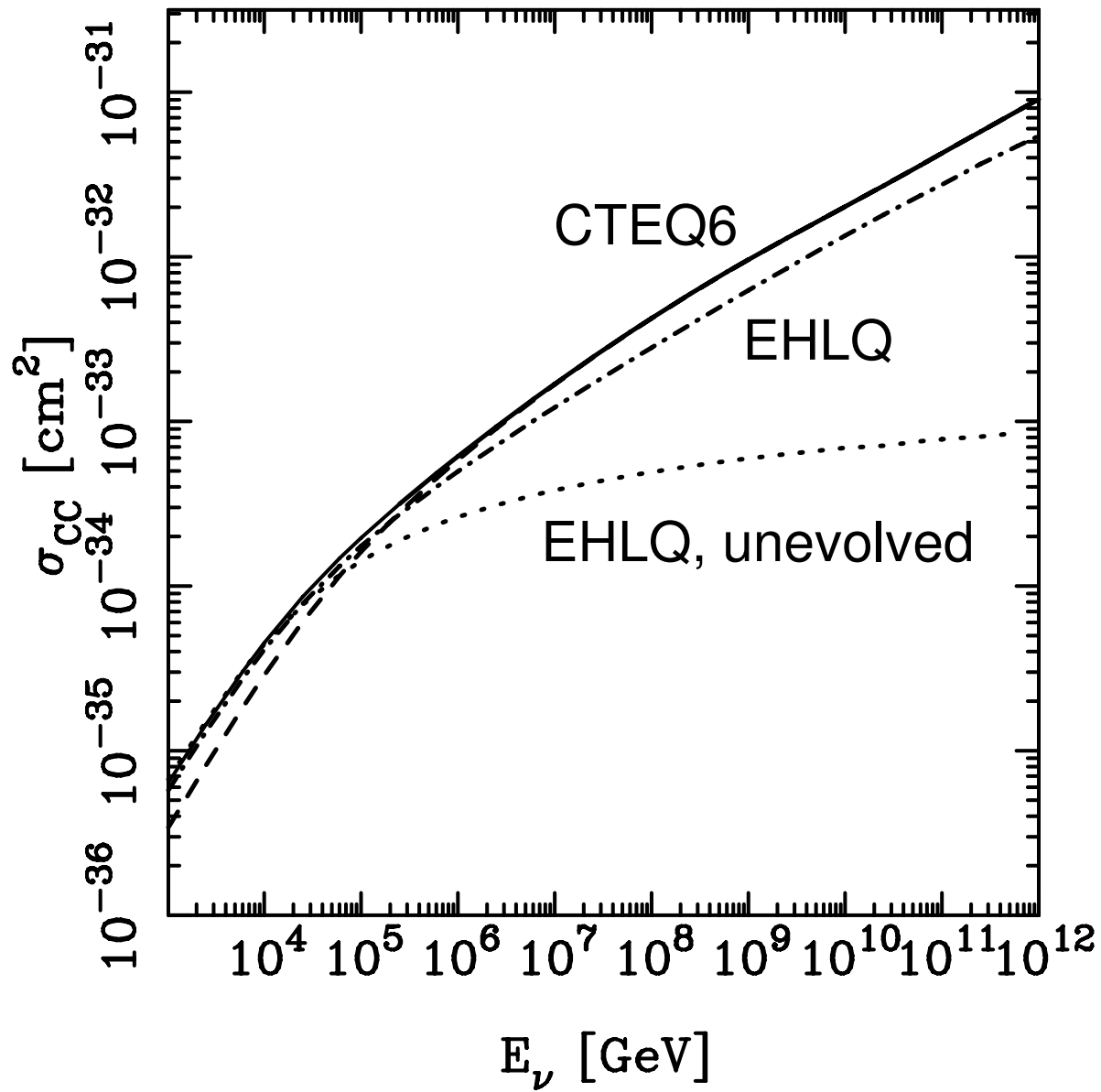
$$q(x, Q^2) = \frac{u_v(x, Q^2) + d_v(x, Q^2)}{2} + \frac{u_s(x, Q^2) + d_s(x, Q^2)}{2} + s_s(x, Q^2) + b_s(x, Q^2)$$

$$\bar{q}(x, Q^2) = \frac{u_s(x, Q^2) + d_s(x, Q^2)}{2} + c_s(x, Q^2) + t_s(x, Q^2),$$

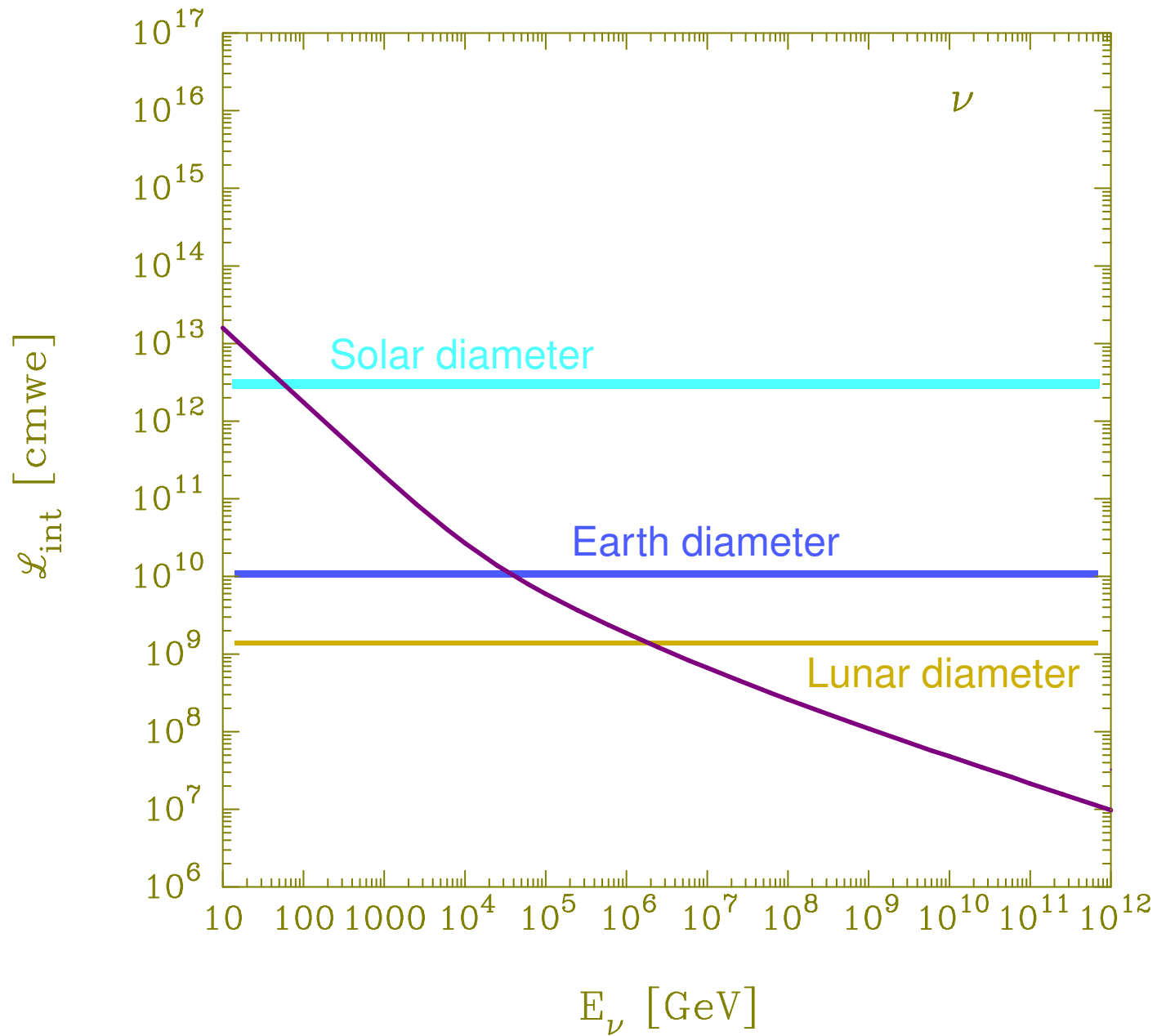
... isoscalar nucleon

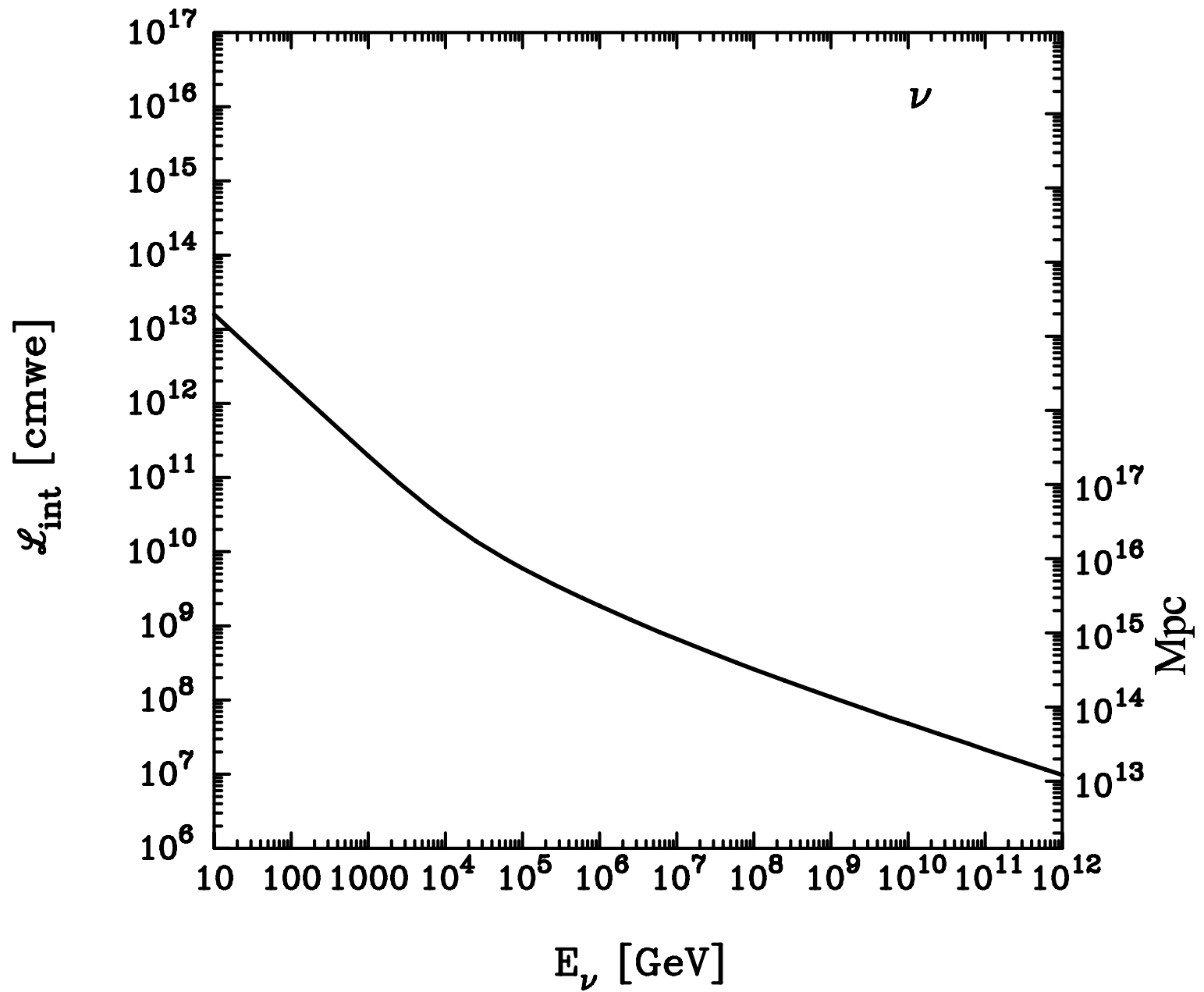




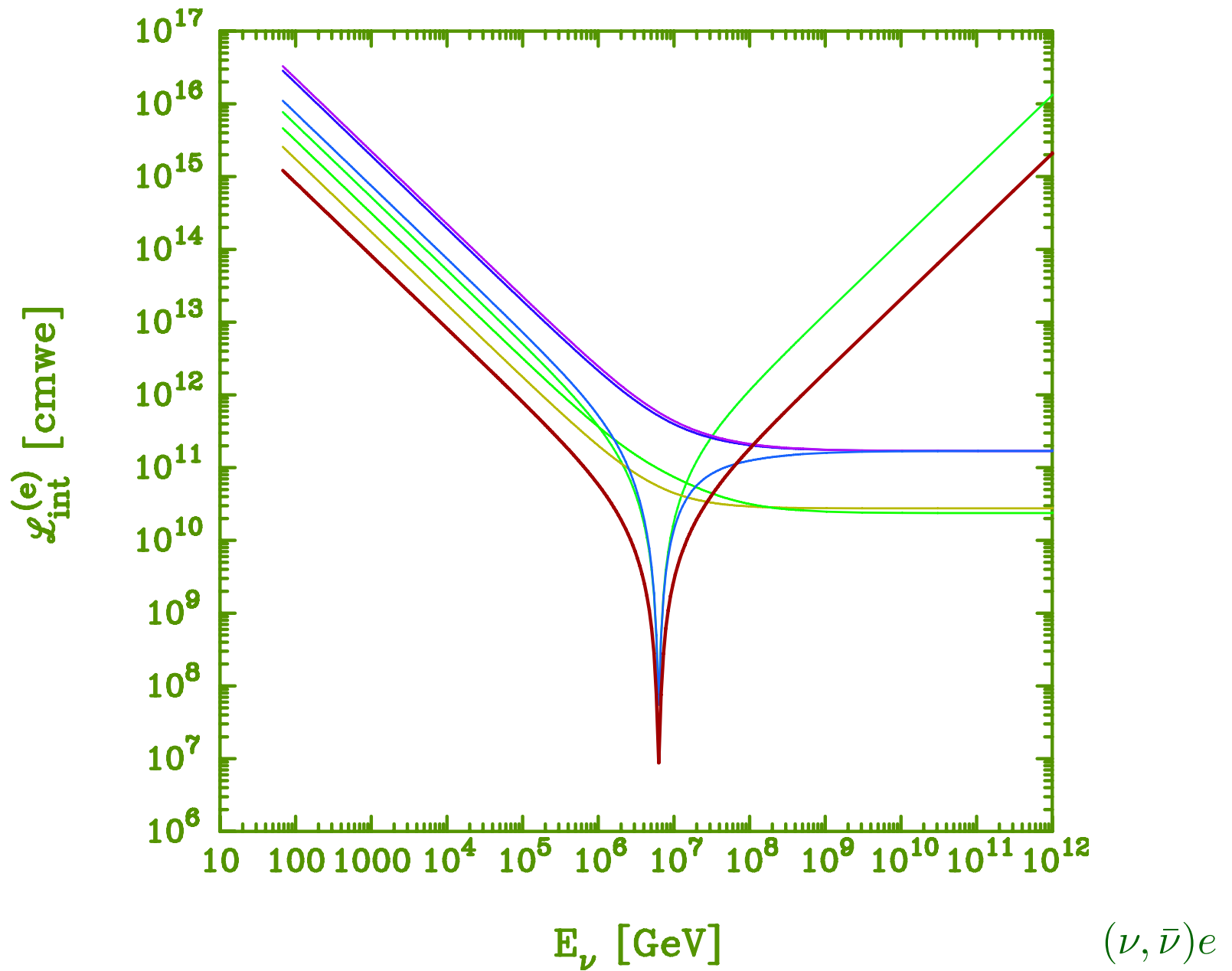


M. H. Reno





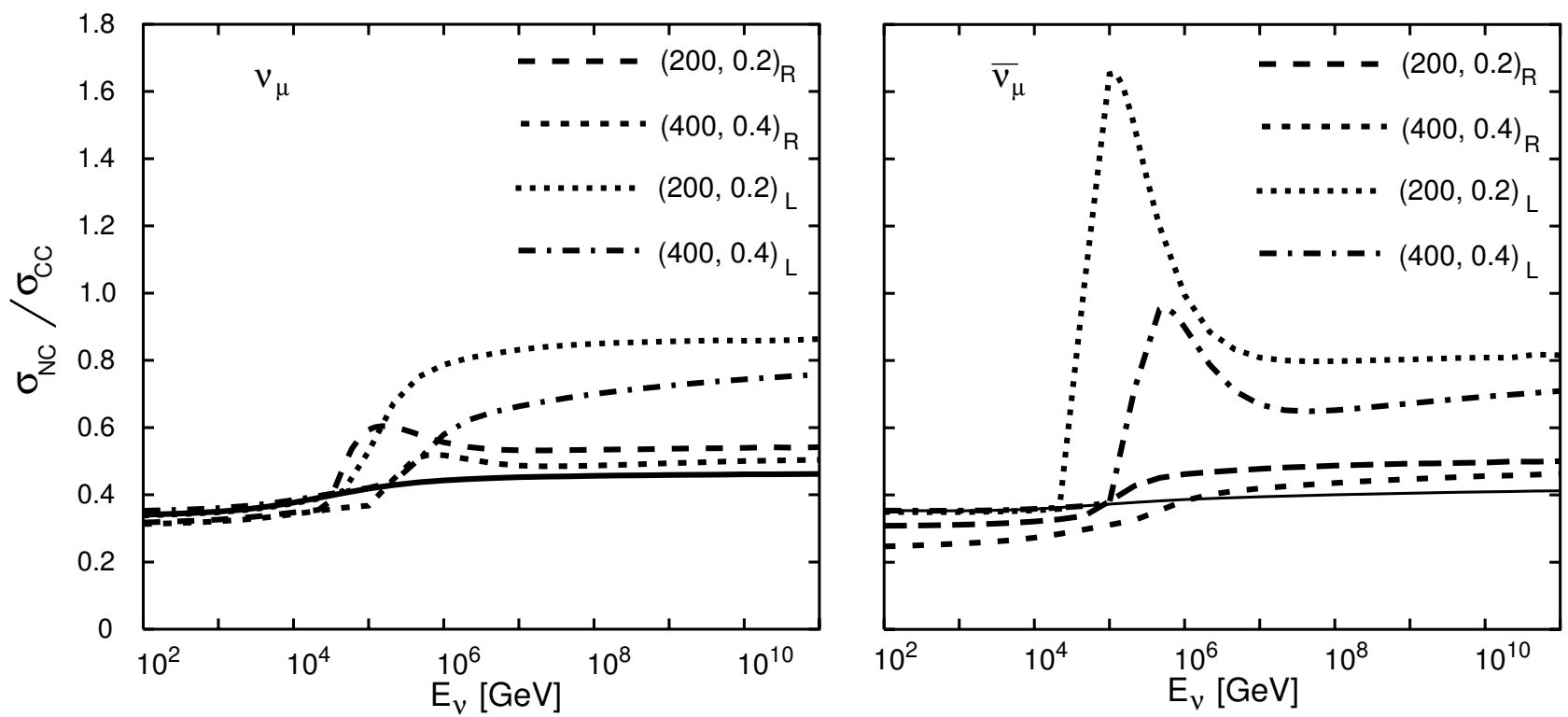




## II New Physics in $\nu N$ interactions?

*NC/CC an important diagnostic*

$\tilde{d}_{L,R}^k$  production through  $\mathcal{R}$  interactions:



$(\tilde{m}, \lambda')$

### III Influence of Neutrino Oscillations

Flux at Earth  $\Phi = \{\varphi_e, \varphi_\mu, \varphi_\tau\} \neq \Phi^0 = \{\varphi_e^0, \varphi_\mu^0, \varphi_\tau^0\}$  source fluxes

Vacuum oscillation length is short; for  $|\Delta m^2| = 10^{-5} \text{ eV}^2$ ,

$$L_{\text{osc}} = 4\pi E_\nu / |\Delta m^2| \approx 2.5 \times 10^{-24} \text{ Mpc} \cdot (E_\nu / 1 \text{ eV})$$

... a fraction of Mpc even for  $E_\nu = 10^{20} \text{ eV}$

*$\nu$  oscillate many times between cosmic source and terrestrial detector*

*Also, over long paths, cosmic neutrinos are vulnerable to decay processes that would not affect terrestrial or solar experiments.*

## ... Neutrino Oscillations

$$\text{(flavor)} \nu_\alpha = \sum_i U_{\beta i} \nu_i \text{ (mass)}$$

Idealize  $\sin \theta_{13} = 0$ ,  $\sin 2\theta_{23} = 1$ , write  $x = \sin^2 \theta_{12} \cos^2 \theta_{12}$ .

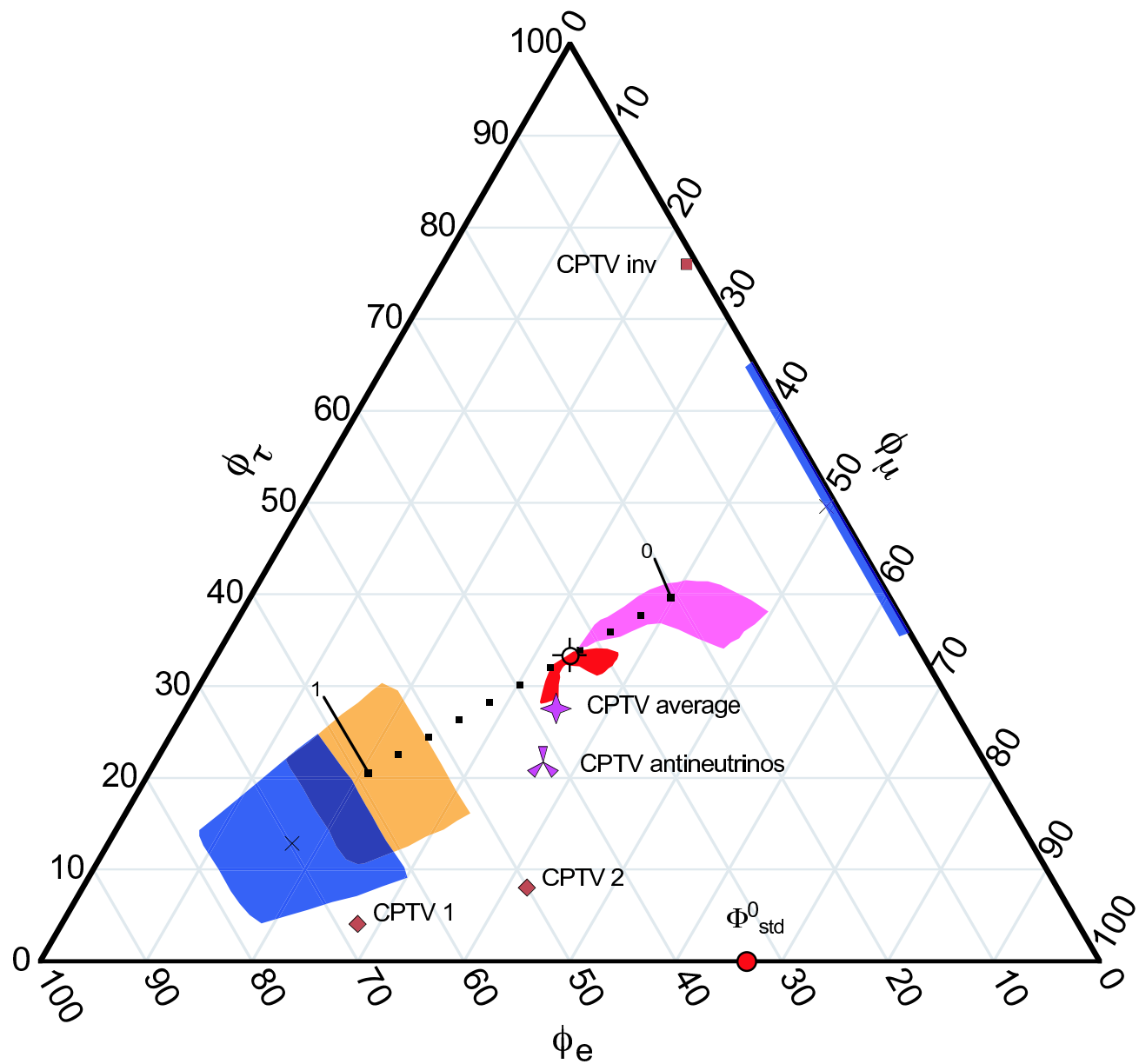
$$U_{\text{ideal}} = \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12}/\sqrt{2} & c_{12}/\sqrt{2} & 1/\sqrt{2} \\ s_{12}/\sqrt{2} & -c_{12}/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}$$

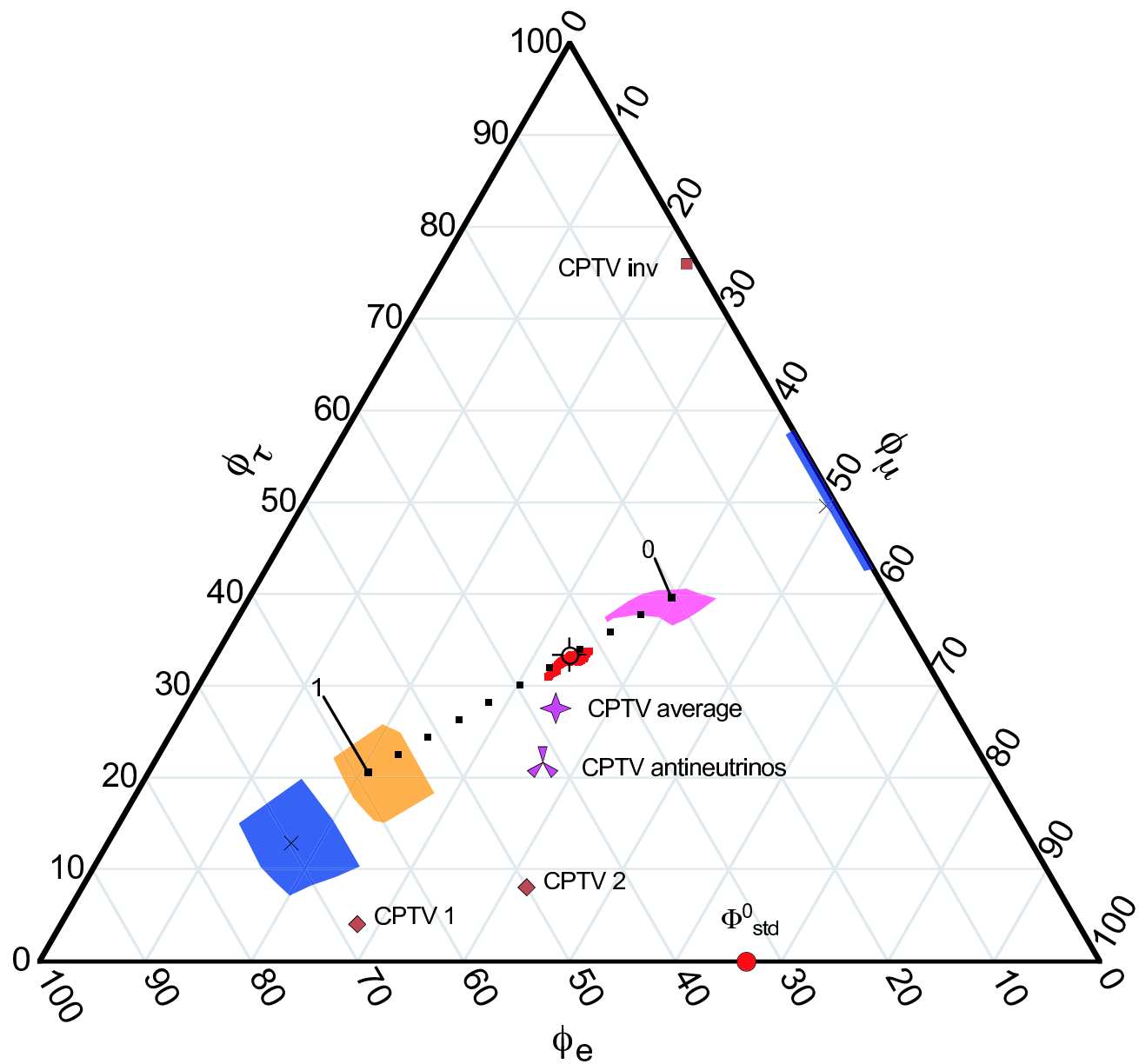
Transfer matrix  $\mathcal{X}$ :  $\Phi^0$  (source)  $\rightarrow$   $\Phi$  (detector); Over many oscillations,

$$\mathcal{X}_{\text{ideal}} = \begin{pmatrix} 1 - 2x & x & x \\ x & \frac{1}{2}(1 - x) & \frac{1}{2}(1 - x) \\ x & \frac{1}{2}(1 - x) & \frac{1}{2}(1 - x) \end{pmatrix}$$

Parke

$$\mathcal{X}_{\text{ideal}} : \Phi_{\text{std}}^0 \rightarrow \left\{ \varphi_e = \frac{1}{3}, \varphi_\mu = \frac{1}{3}, \varphi_\tau = \frac{1}{3} \right\}$$

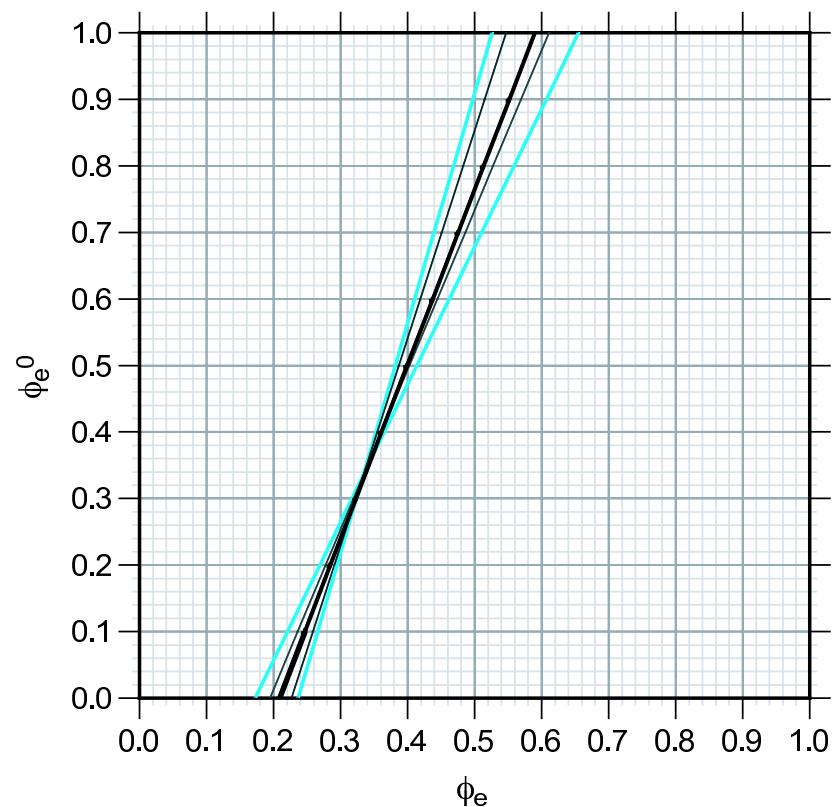




## IV Reconstructing the $\nu$ Mixture at the Source

$\nu_\mu, \nu_\tau$  fully mixed  $\Rightarrow$  can't fully characterize  $\Phi^0$

Reconstruct  $\nu_e$  fraction at source using  $\mathcal{X}_{\text{ideal}}$ :  $\varphi_e^0 = (\varphi_e - x)/(1 - 3x)$



Extreme  $\varphi_e$  implicates unconventional physics

## V Influence of Neutrino Decays

Nonradiative decays  $\nu_i \rightarrow (\nu_j, \bar{\nu}_j) + X$  not very constrained:

$$\tau/m \gtrsim 10^{-4} \text{ s/eV}$$

If only lightest neutrino survives, flavor mix at Earth is independent of composition at source

Normal hierarchy

$$m_1 < m_2 < m_3:$$

$$\varphi_\alpha = |U_{\alpha 1}|^2$$

$$\Phi_{\text{normal}} \approx \{0.70, 0.17, 0.13\}$$

Inverted hierarchy

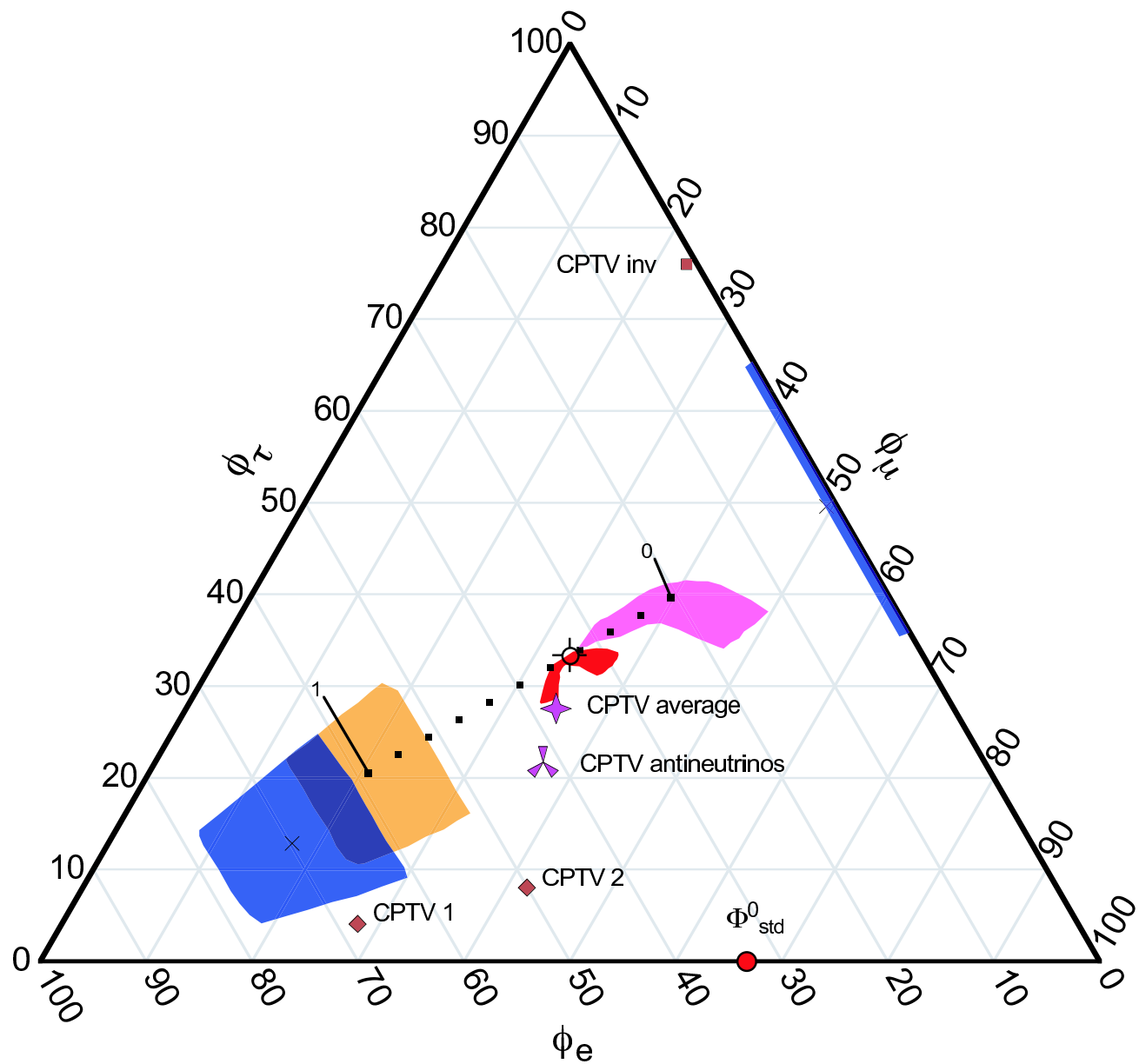
$$m_1 > m_2 > m_3:$$

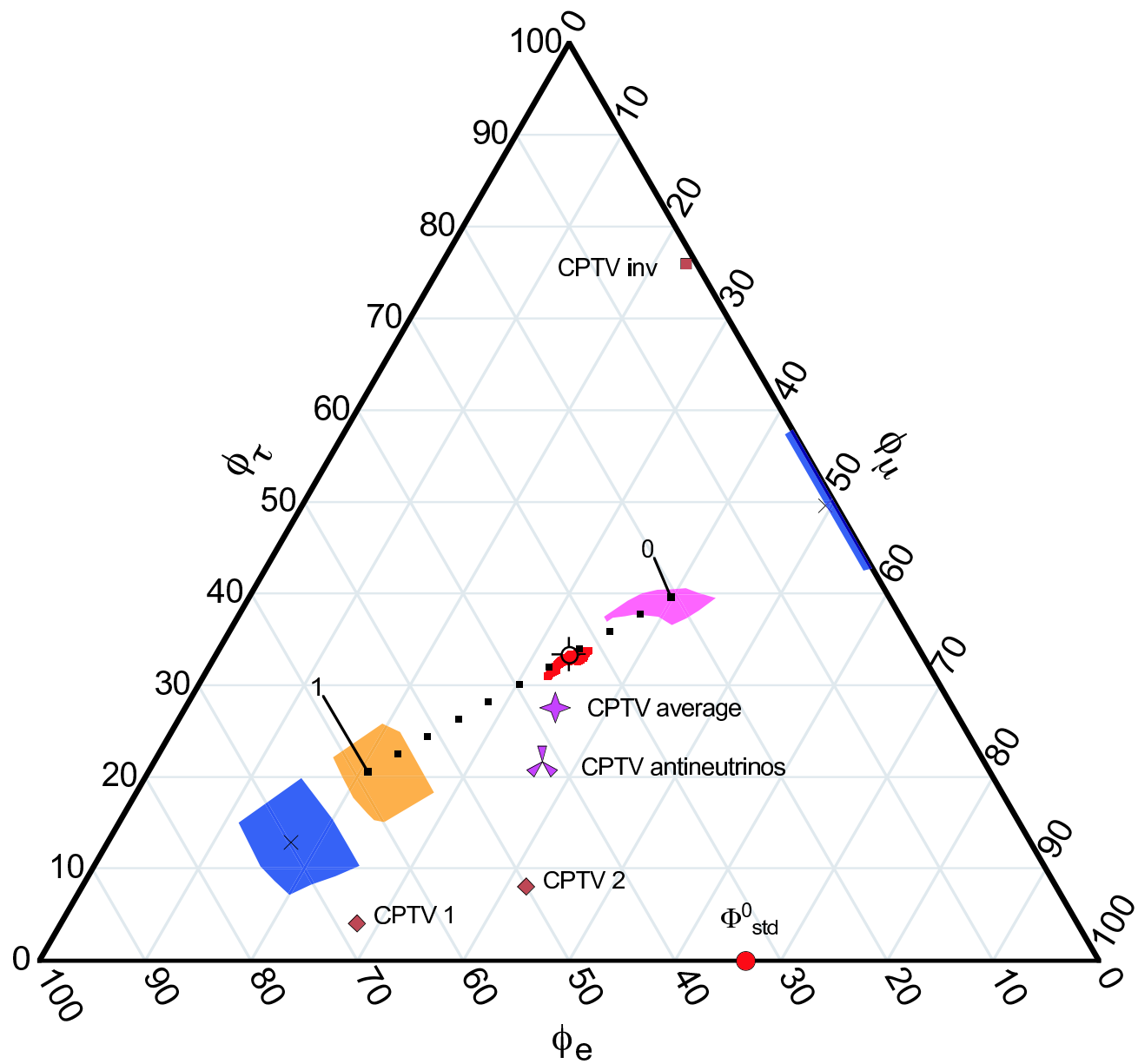
$$\varphi_\alpha = |U_{\alpha 3}|^2$$

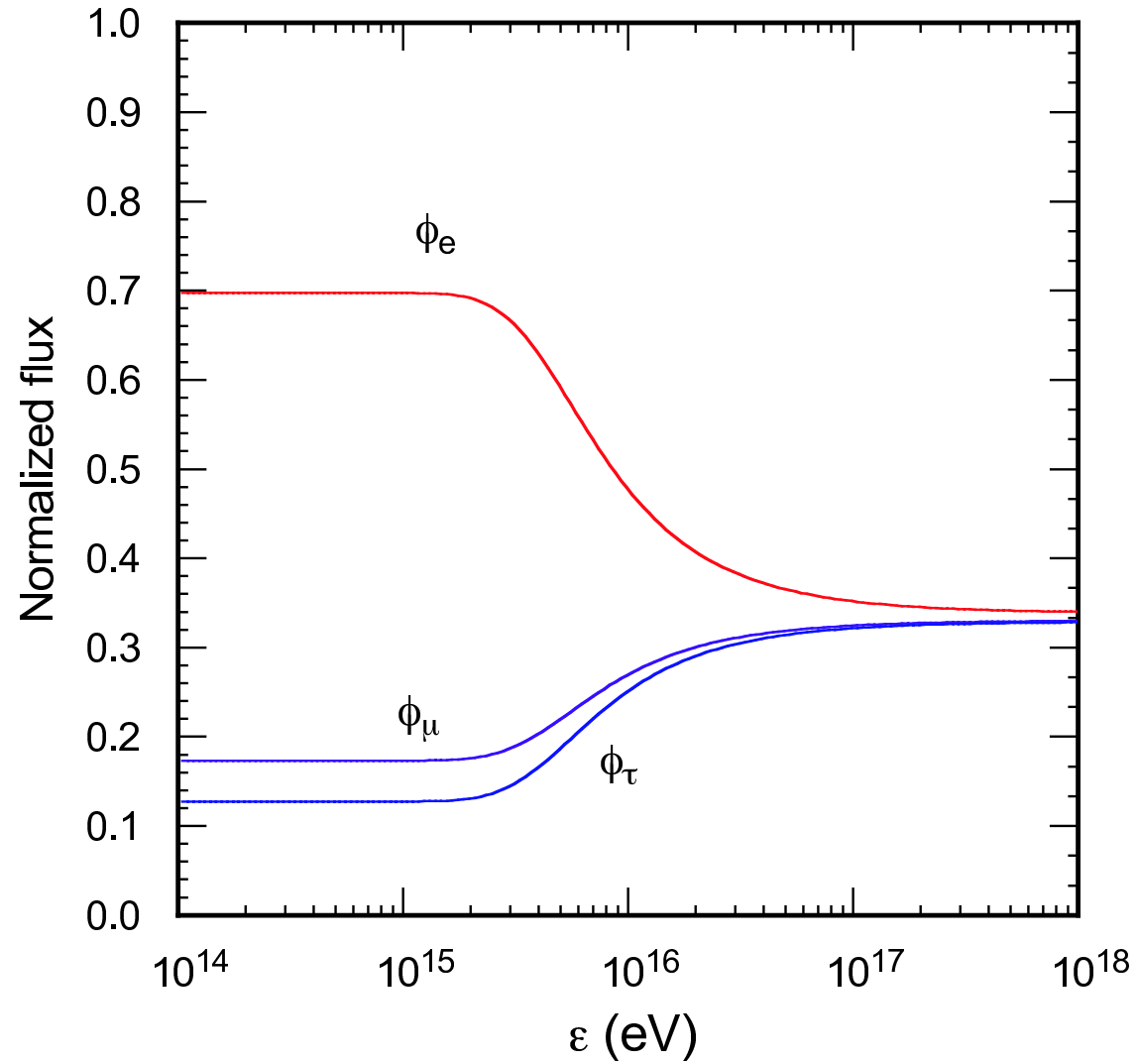
$$\Phi_{\text{inverted}} \approx \{0, 0.5, 0.5\}$$

far from  $\Phi_{\text{std}} = \{\frac{1}{3}, \frac{1}{3}, \frac{1}{3}\}$



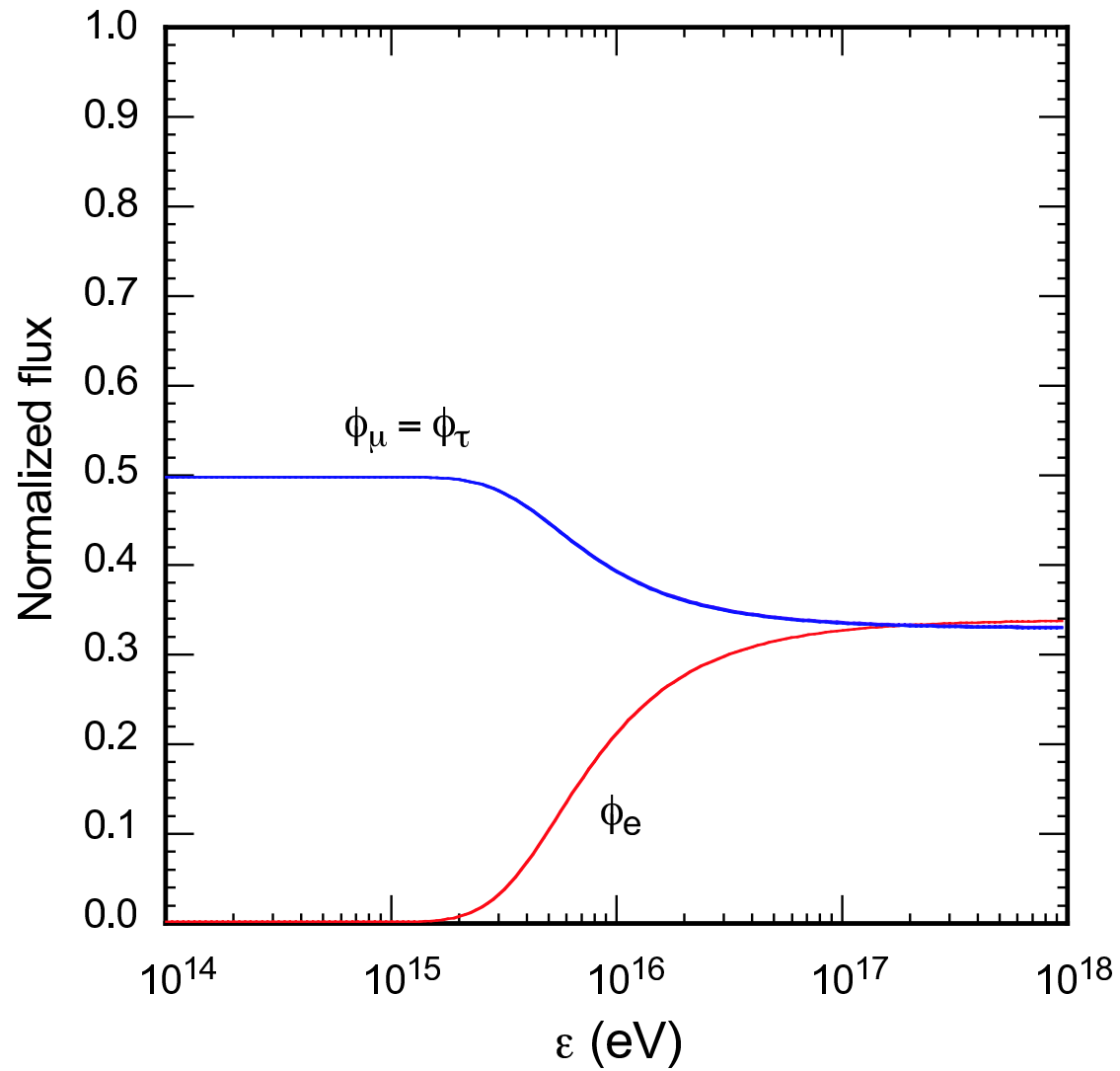






$$E_\nu = \epsilon(1 \text{ s/eV}) / (\tau_\nu / m_\nu) \cdot L / (100 \text{ Mpc})$$

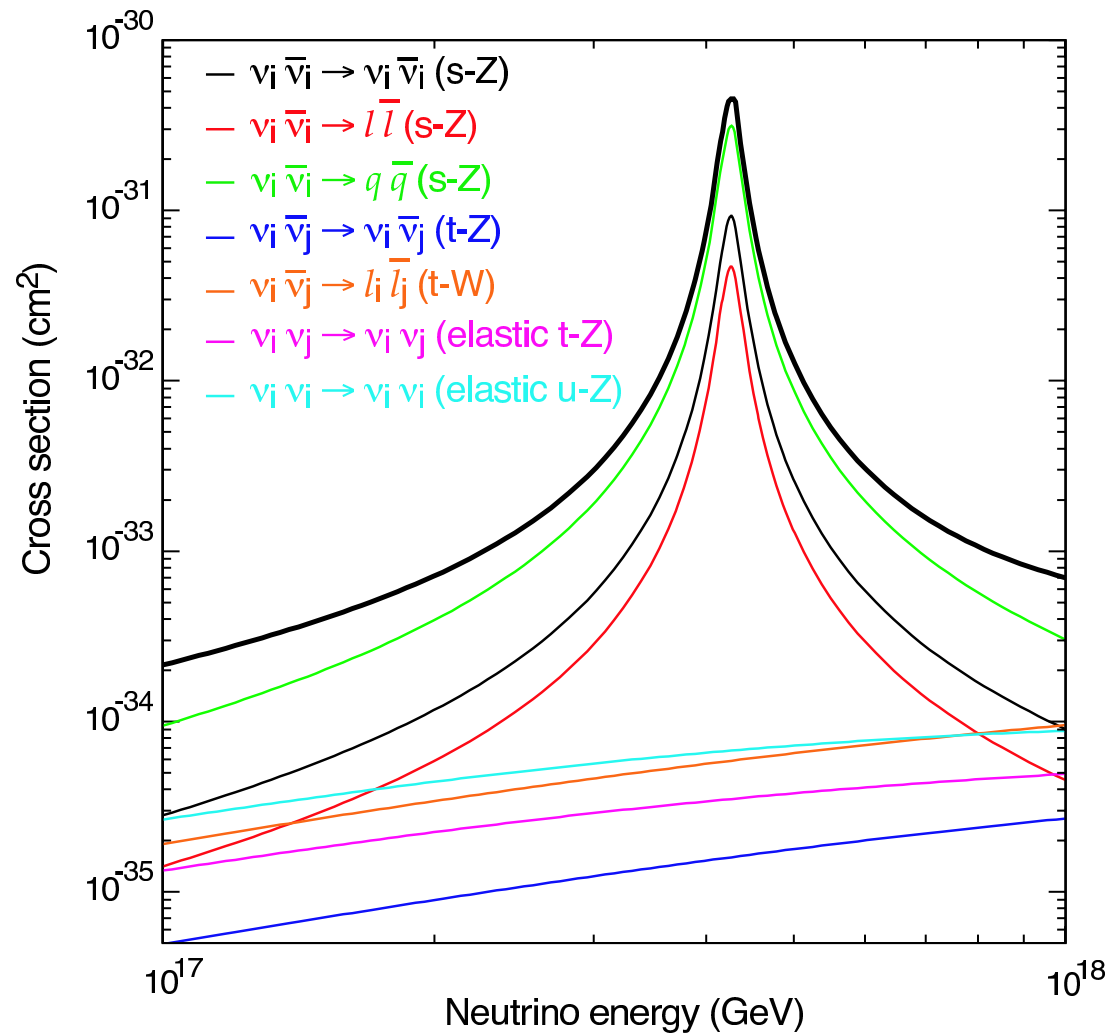
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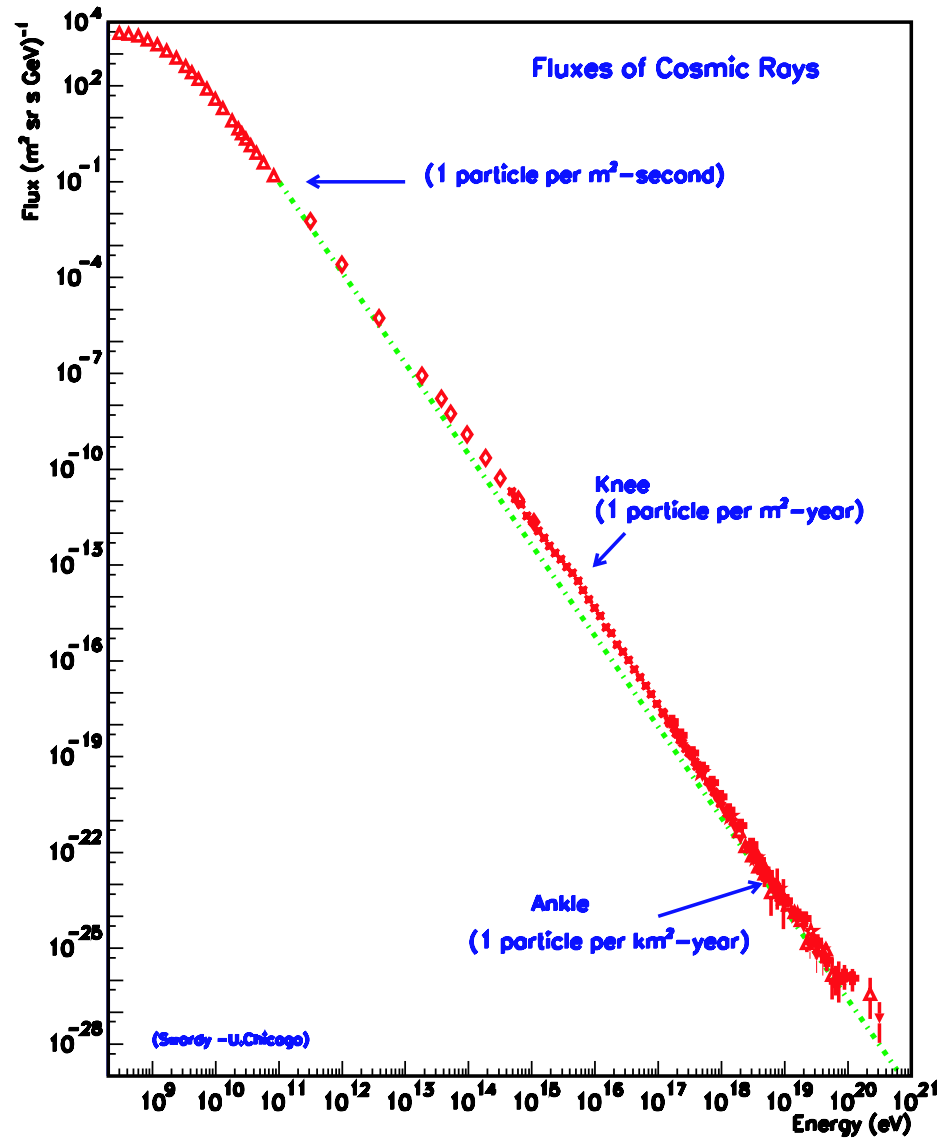
Inverted hierarchy

# VI UHE $\nu$ annihilation on $\nu$ relics

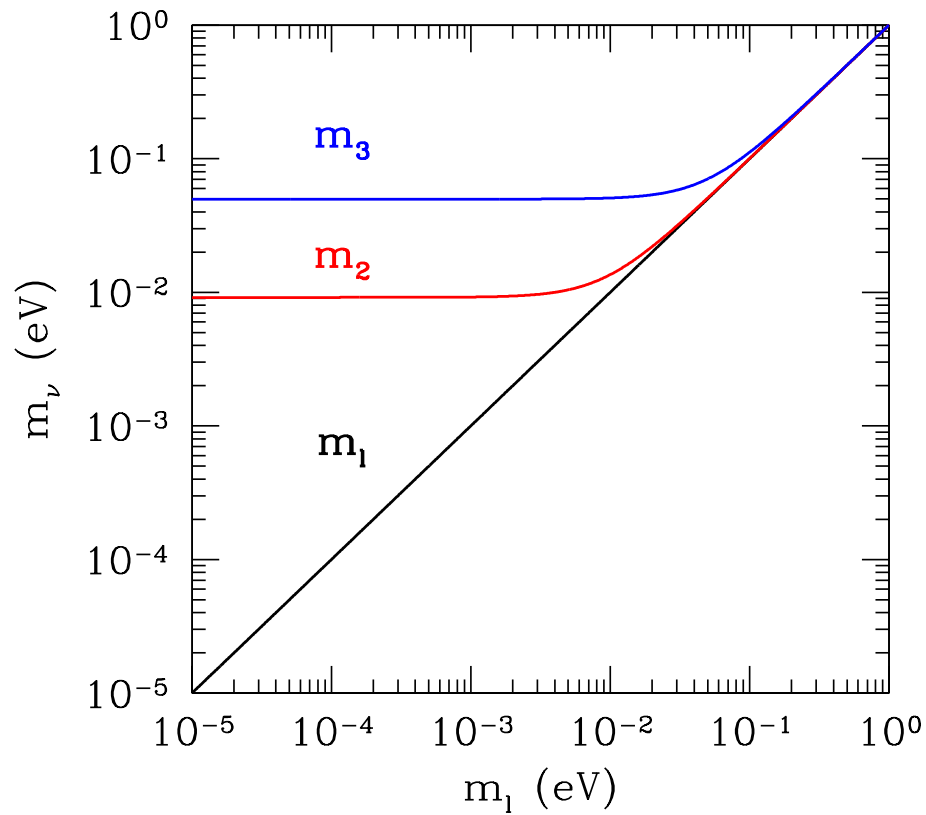


$$m_\nu = 10^{-5} \text{ eV}$$

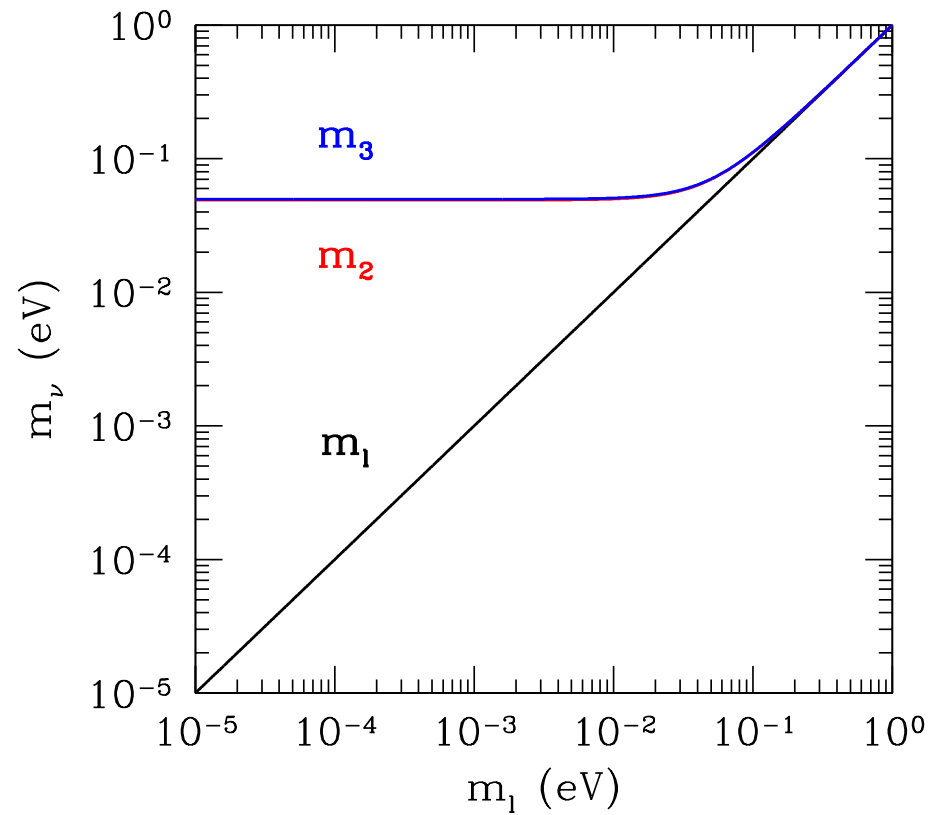
# Pierre Auger Observatory should clarify trans-GZK regime soon



## Normal hierarchy

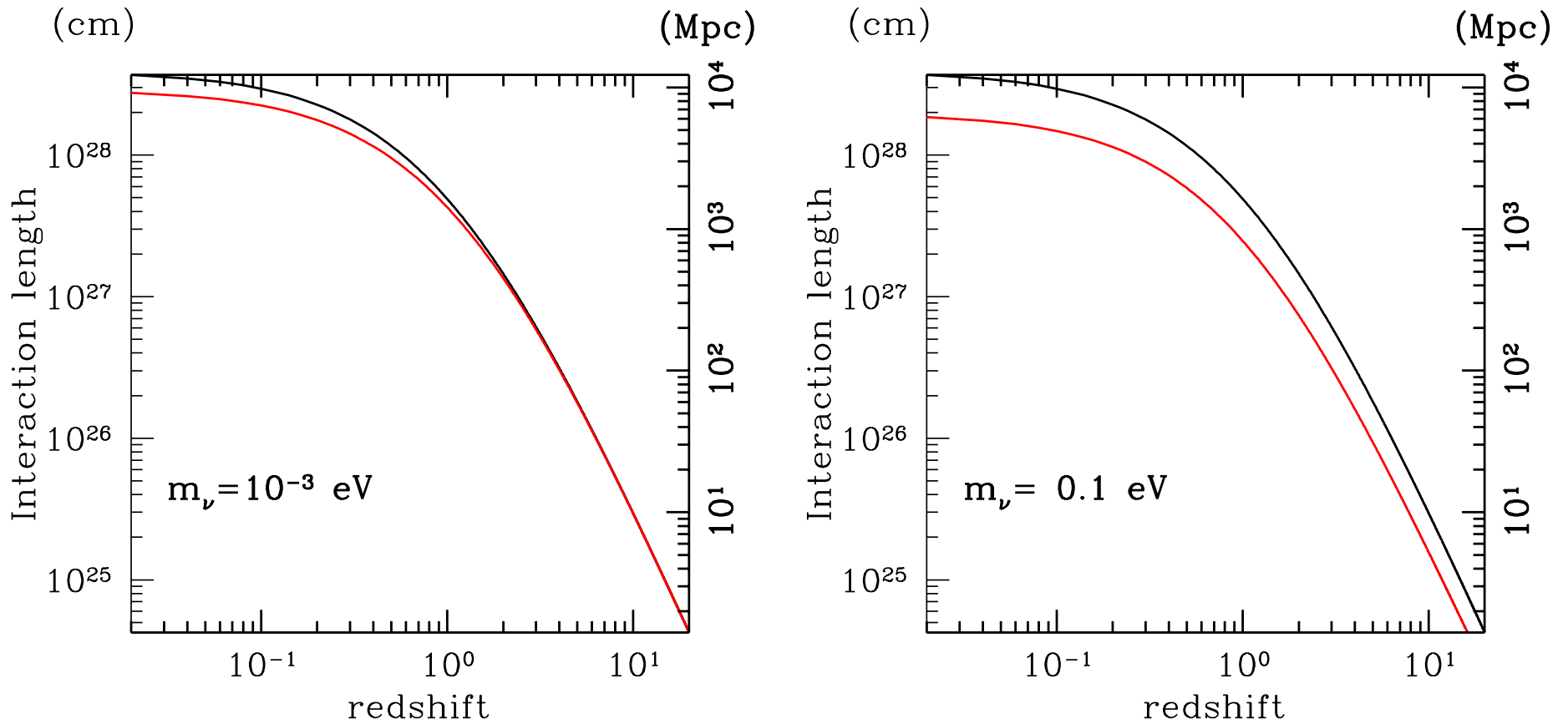


## Inverted hierarchy



Animation

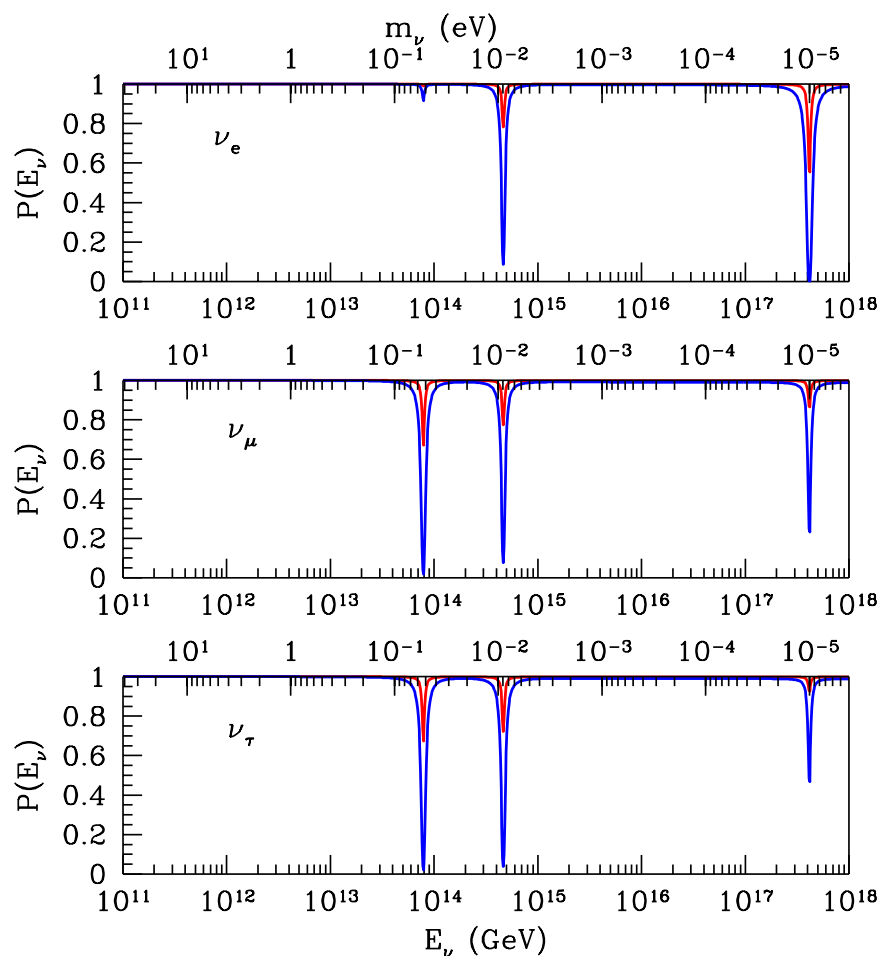
Interaction lengths on  $Z^0$  resonance: Dirac Majorana



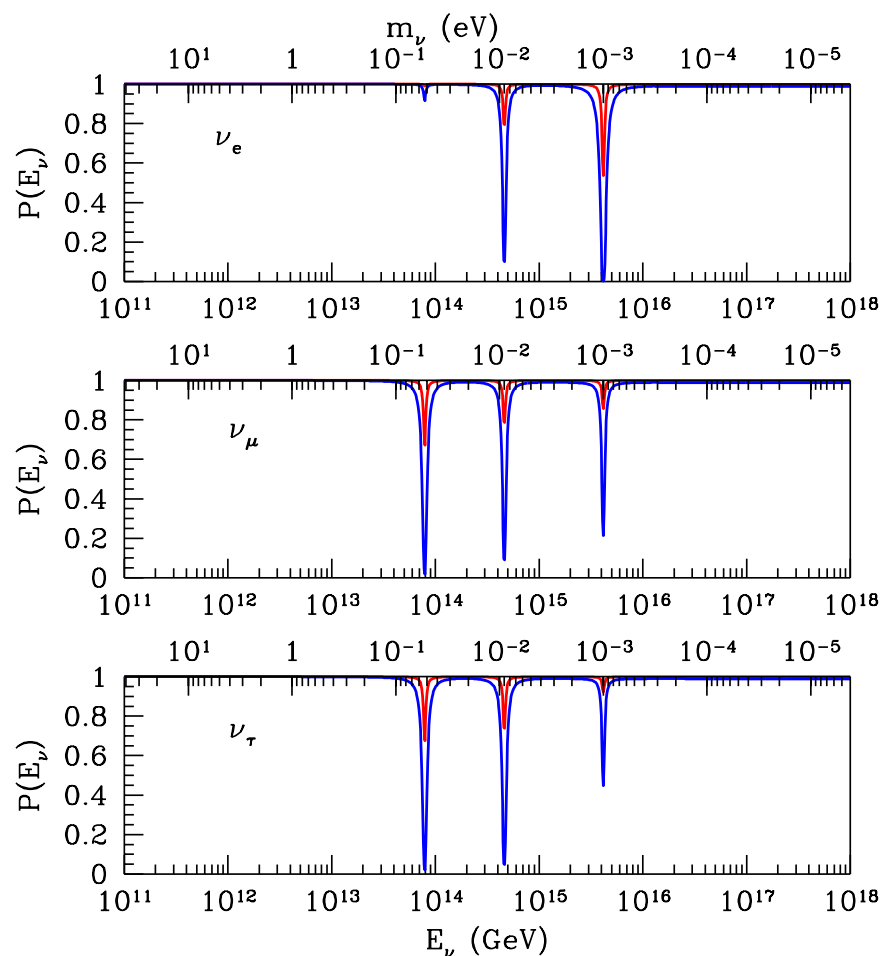
$\nu$  number density now:  $56 \text{ cm}^{-3}$ ,  $\propto (1+z)^3$



# Fable: $l-o-o-o-o-n-g$ path ( $10^4$ or $10^5$ Mpc) in current Universe

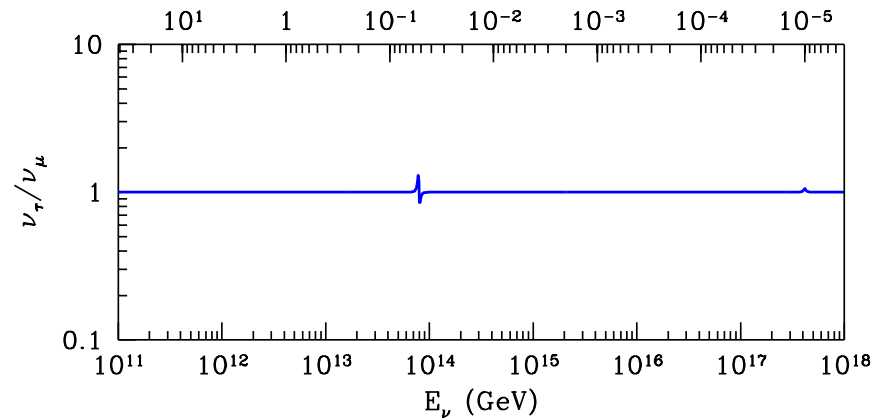
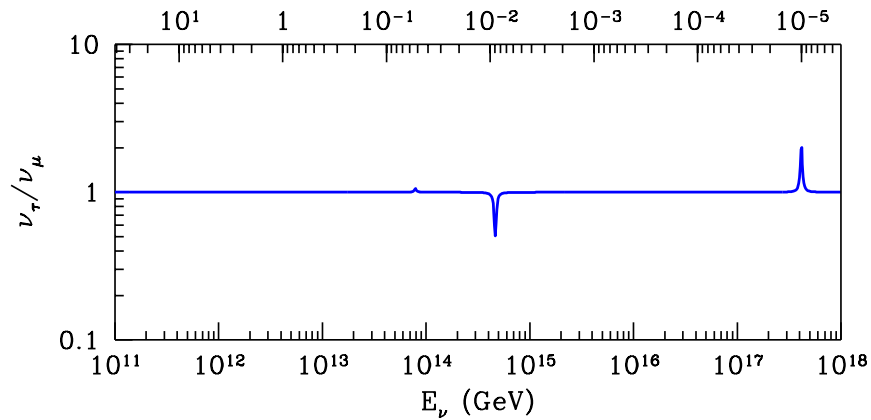
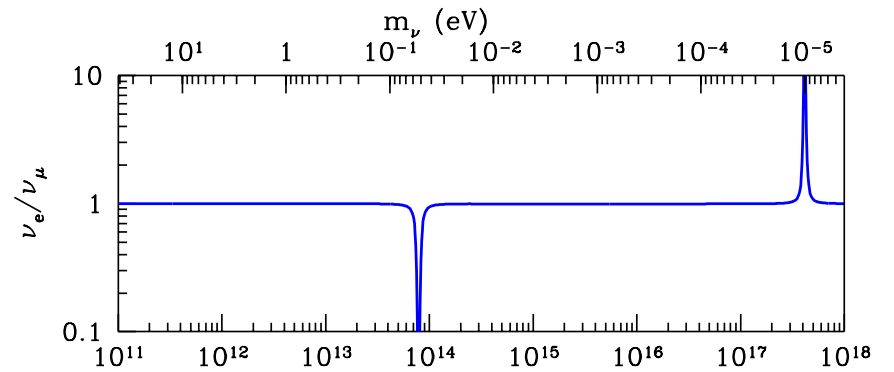
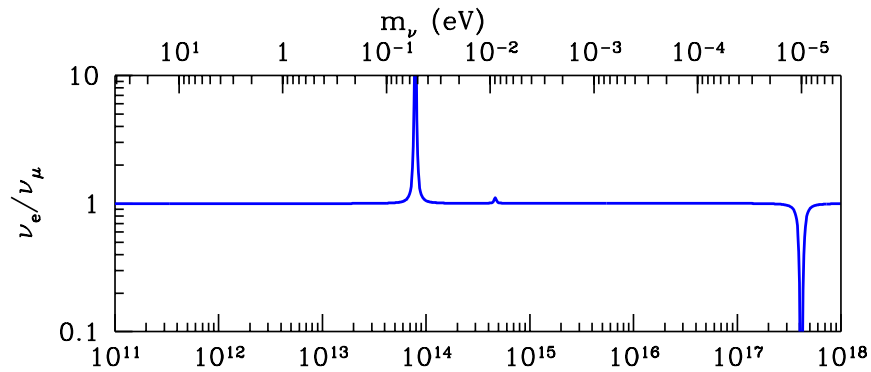


$$m_\ell = 10^{-5} \text{ eV}$$



$$m_\ell = 10^{-3} \text{ eV}$$

# Flavor ratios probe the mass hierarchy ...

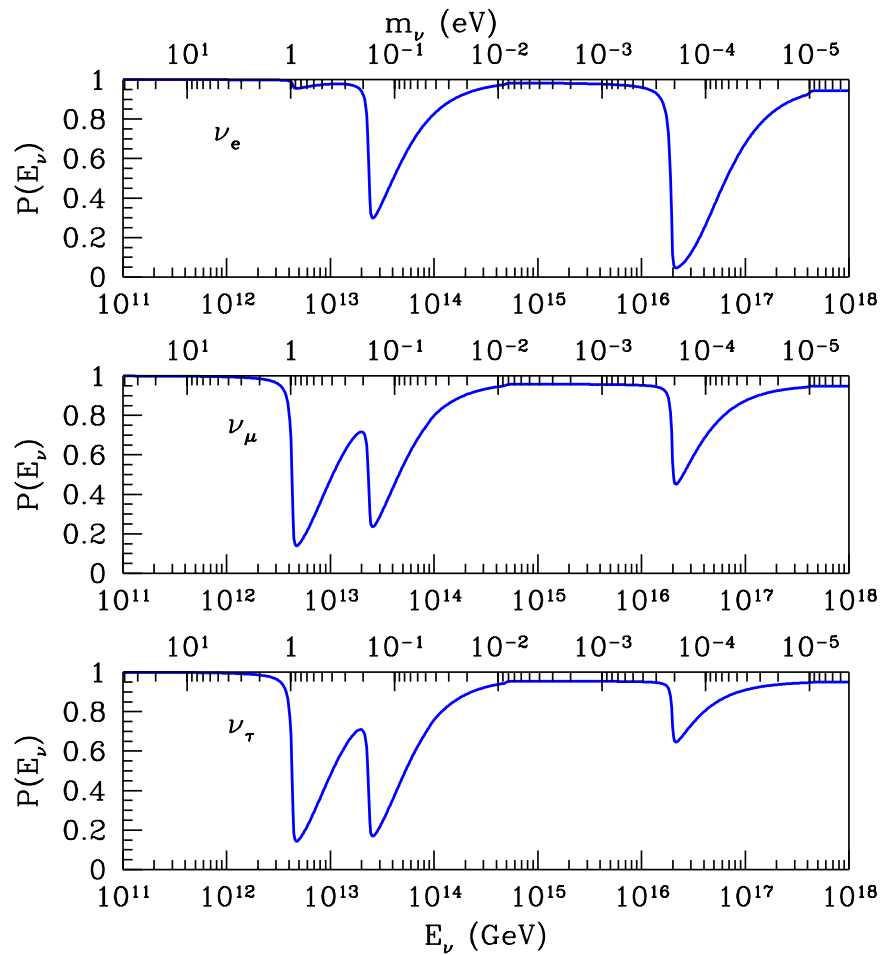


Normal

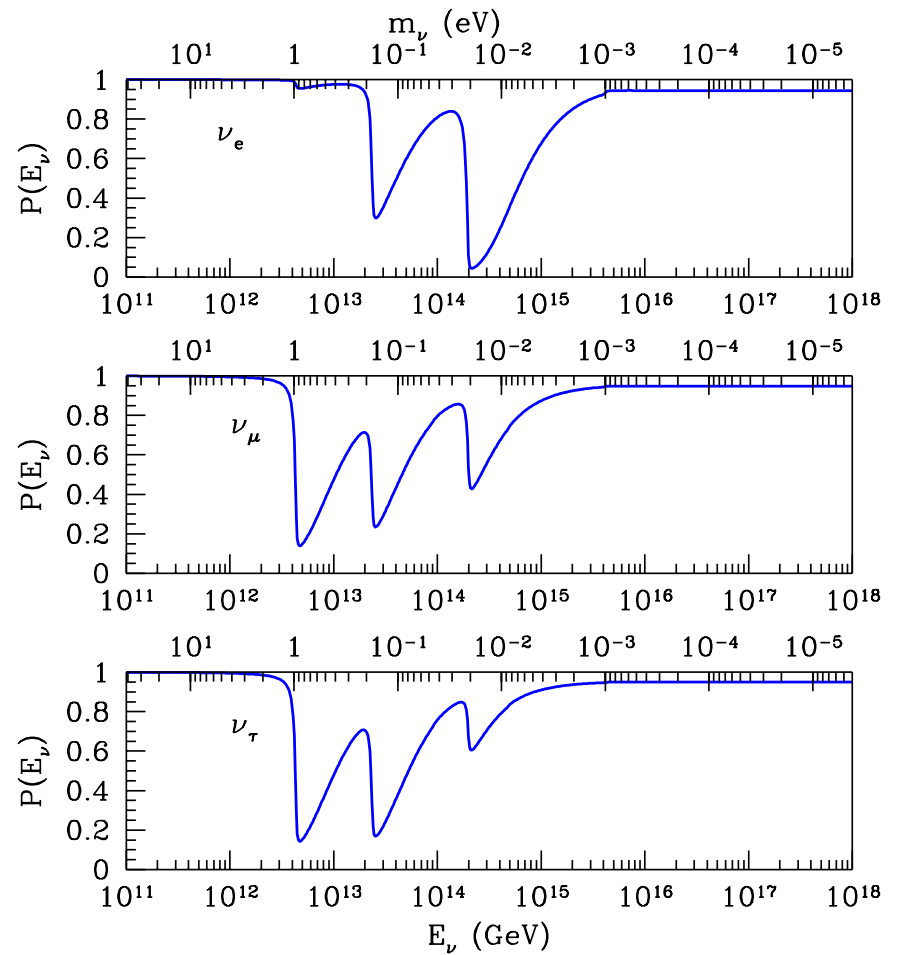
$$m_\ell = 10^{-5} \text{ eV}$$

Inverted

# Incorporate evolution of Universe back to $z = 20$

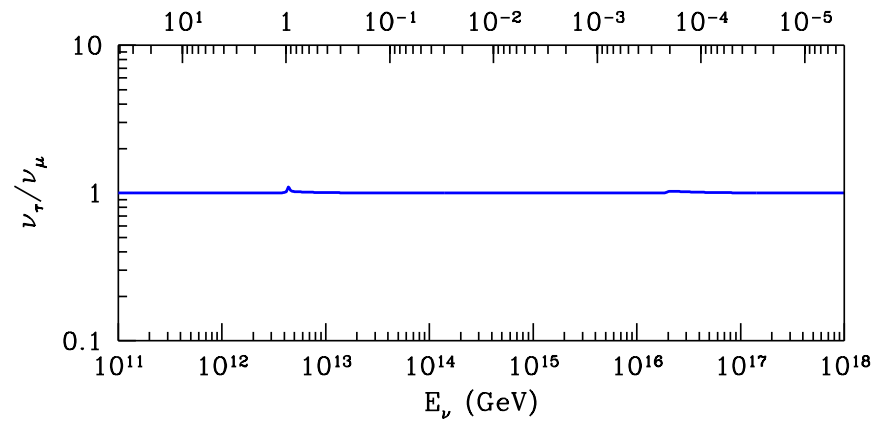
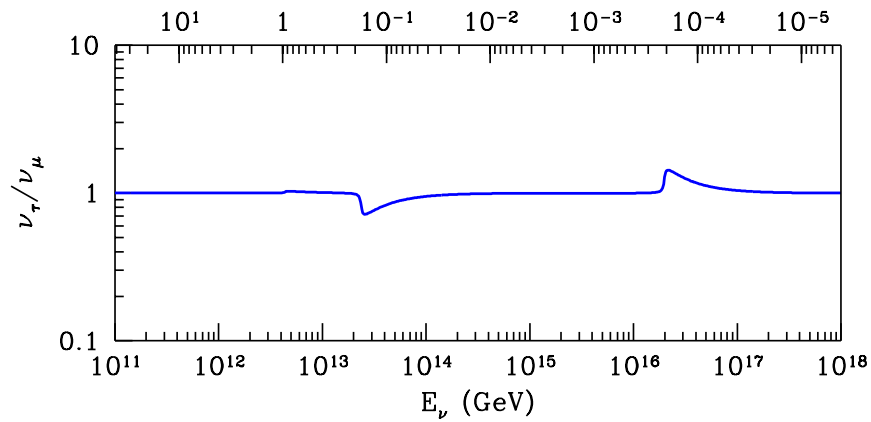
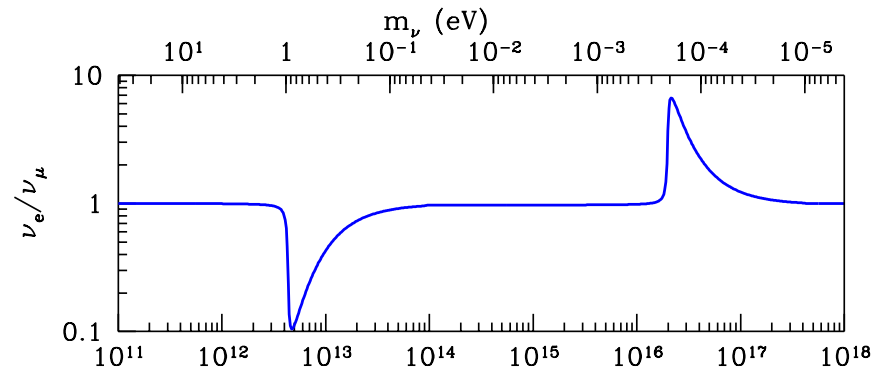
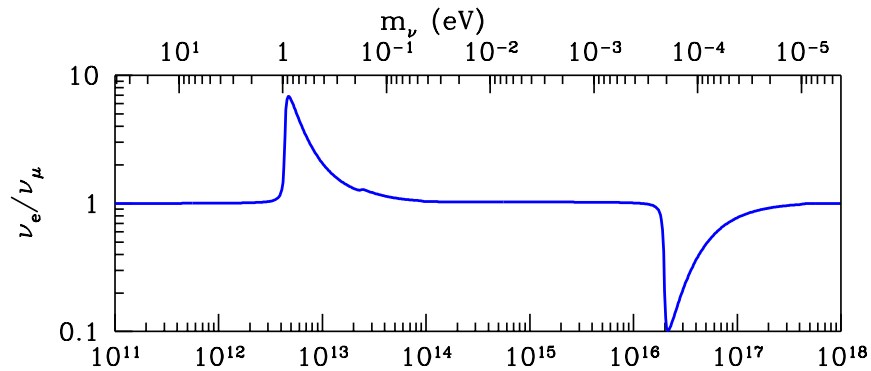


$$m_\ell = 10^{-5} \text{ eV}$$



$$m_\ell = 10^{-3} \text{ eV}$$

# Flavor ratios probe the mass hierarchy ( $z \lesssim 20$ )

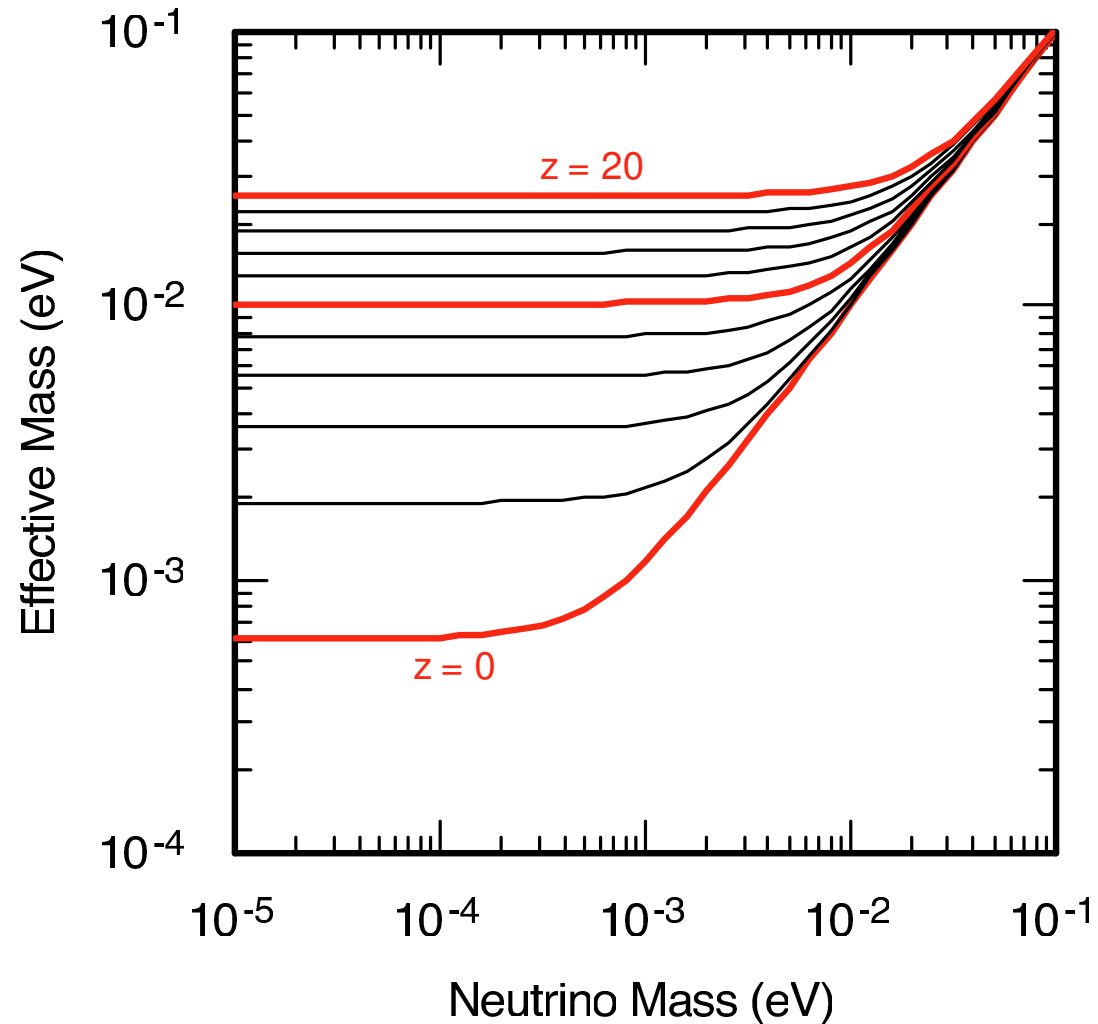


Normal

$$m_\ell = 10^{-5} \text{ eV}$$

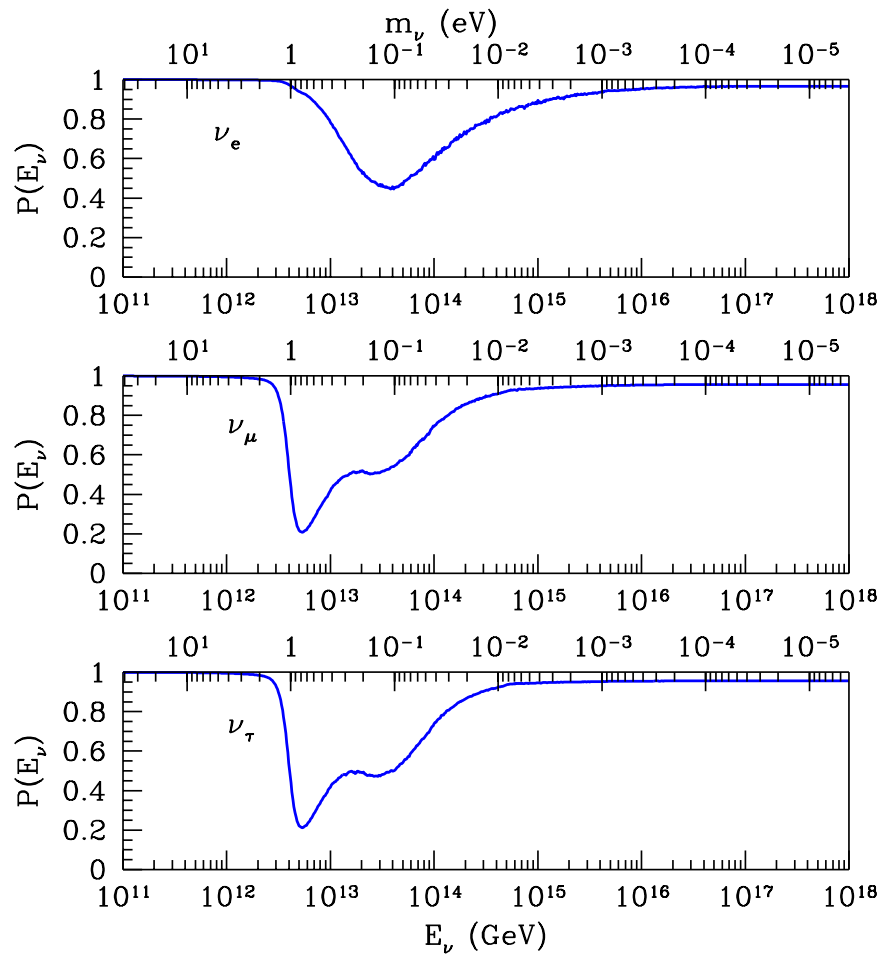
Inverted

# Neutrinos are moving targets ...

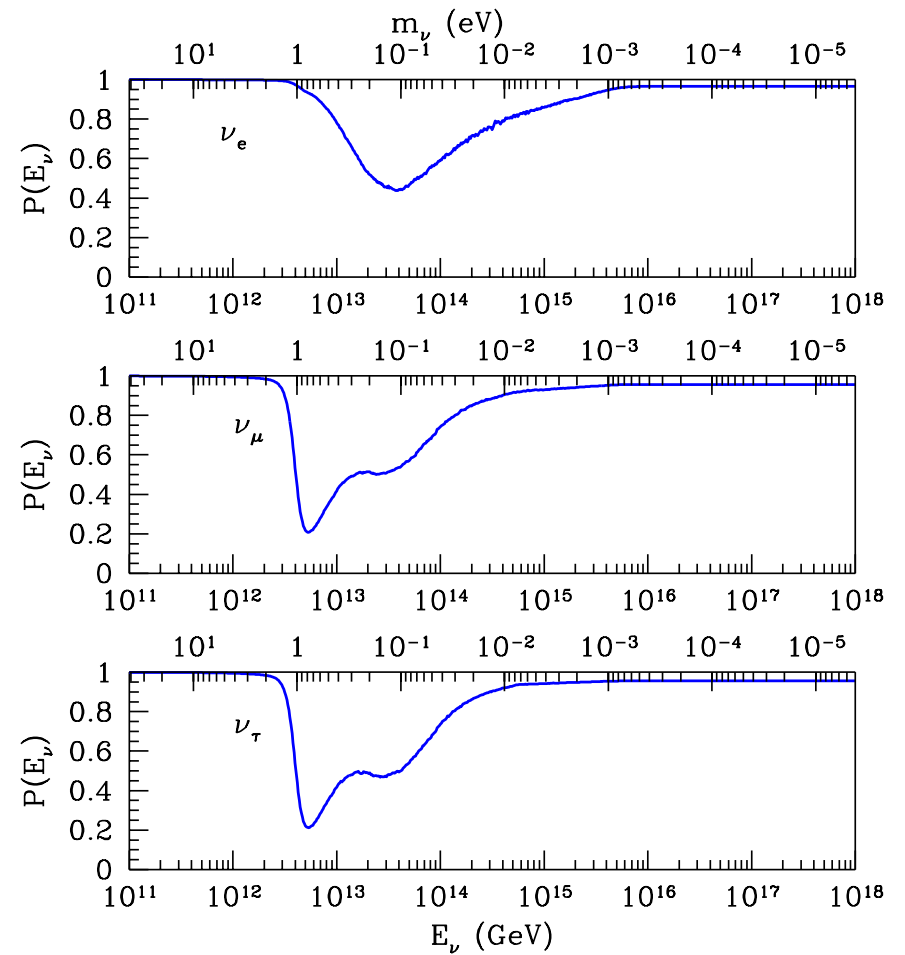


$$T_{\nu 0} = 1.945 \text{ K} = 1.697 \times 10^{-4} \text{ eV} \quad T_{\nu} \propto (1 + z)$$

# Incorporate evolution of Universe back to $z = 20$ , Fermi motion

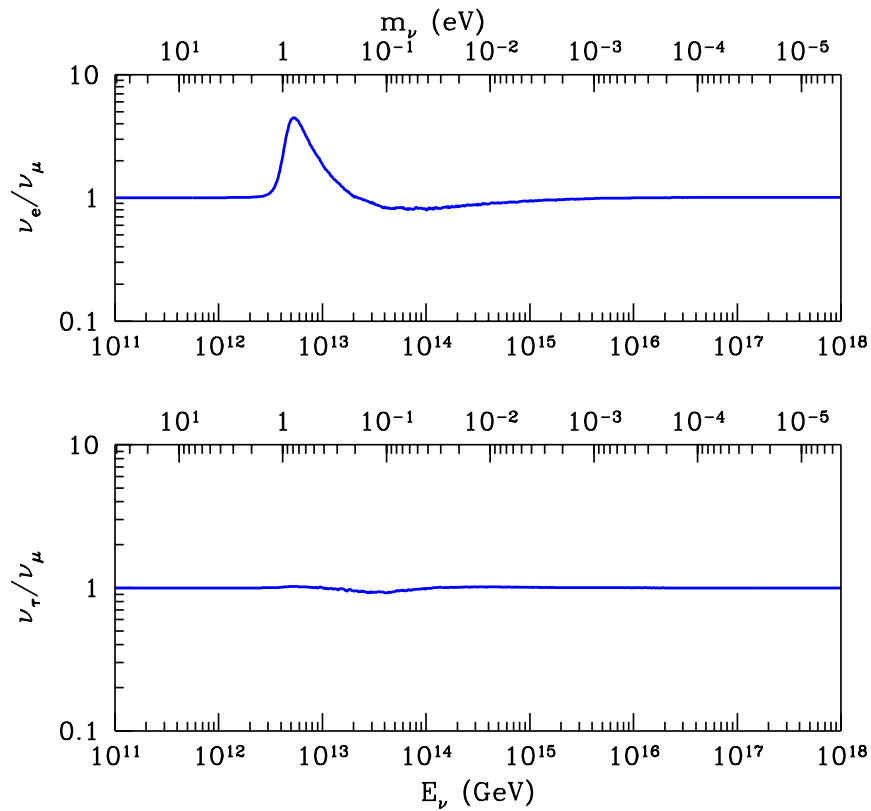


$$m_\ell = 10^{-5} \text{ eV}$$



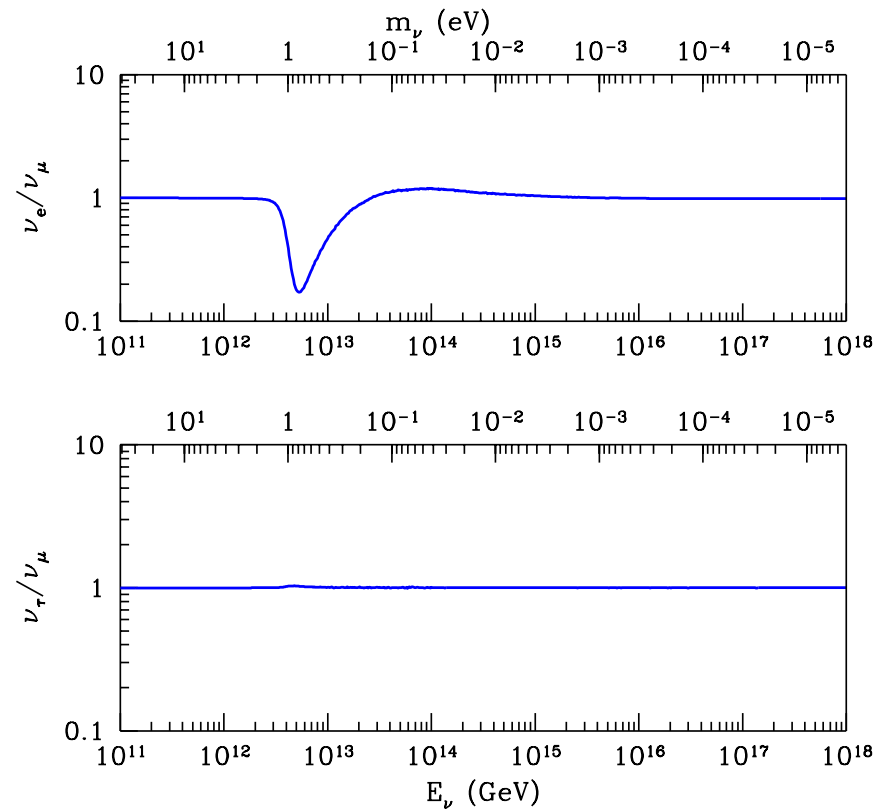
$$m_\ell = 10^{-3} \text{ eV}$$

# Flavor ratios probe the mass hierarchy ( $z \lesssim 20$ ), Fermi motion



Normal

$$m_\ell = 10^{-5} \text{ eV}$$



Inverted

## Cosmic-neutrino absorption spectroscopy ...

- ▷ Must establish  $\nu$  flux exists in GZK regime and beyond
- ▷ Will require vast effective volumes, long observation times
- ▷ To probe neutrino properties (beyond mass scale), need (at least)  $e/\mu$  comparison
- ▷ Earlier the sources (higher redshift), the lower the energy of absorption lines, the greater the sensitivity to thermal history of the Universe
- ▷ Nonacceleration sources at early times could plant dips at unexpectedly low energies



## VII Neutrino Coannihilation on Dark-Matter Relics?

Consider neutralino dark matter,  $M_{\chi_1^0} \approx 150$  GeV

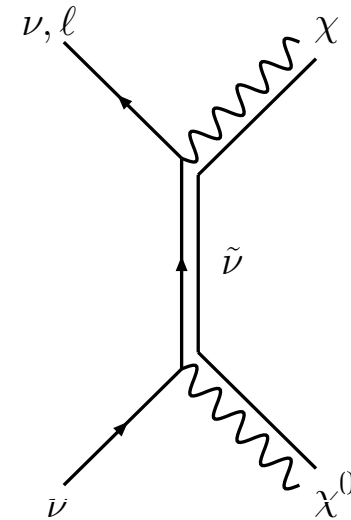
Good news:  $E_\nu^{\text{res}} \approx 400$  GeV ( $\tilde{\nu}$  formation);  
cross section 10% of  $\nu\bar{\nu} \rightarrow Z$

Bad news: relic  $\chi^0$  much rarer than relic  $\nu$

Universe at large:  $56 \nu \text{ cm}^{-3}$ ,  $\lesssim 10^{-8} \chi^0 \text{ cm}^{-3}$

Interaction length for  $\tilde{\nu}$  formation:  $10^{15}$  Mpc

Our location in galaxy [NFW]:  $\lesssim 10^{-3} \chi^0 \text{ cm}^{-3}$



Barenboim, Mena, CQ

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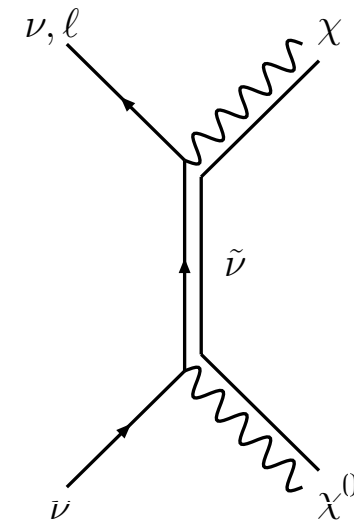
Solar system, inside Earth orbit [Khriplovich & Pitjeva]:  $< 10^3 \chi^0 \text{ cm}^{-3}$

$\rightsquigarrow < 10^{-6} \tilde{\nu} \text{ y}^{-1}$  in Earth's atmosphere (ATM  $\nu$ )

... but up to  $O(600) \tilde{\nu} \text{ y}^{-1}$  inside Earth's orbit (AGN  $\nu$ )

Barenboim, Mena, CQ

Datta, Fargion, Mele: UHE  $\chi^0$  on relic  $\nu$



$$\dots \nu \chi_1^0 \rightarrow \tilde{\nu}$$

Entire galaxy would contain  $\sim 10^{65}$  neutralinos (NFW profile)

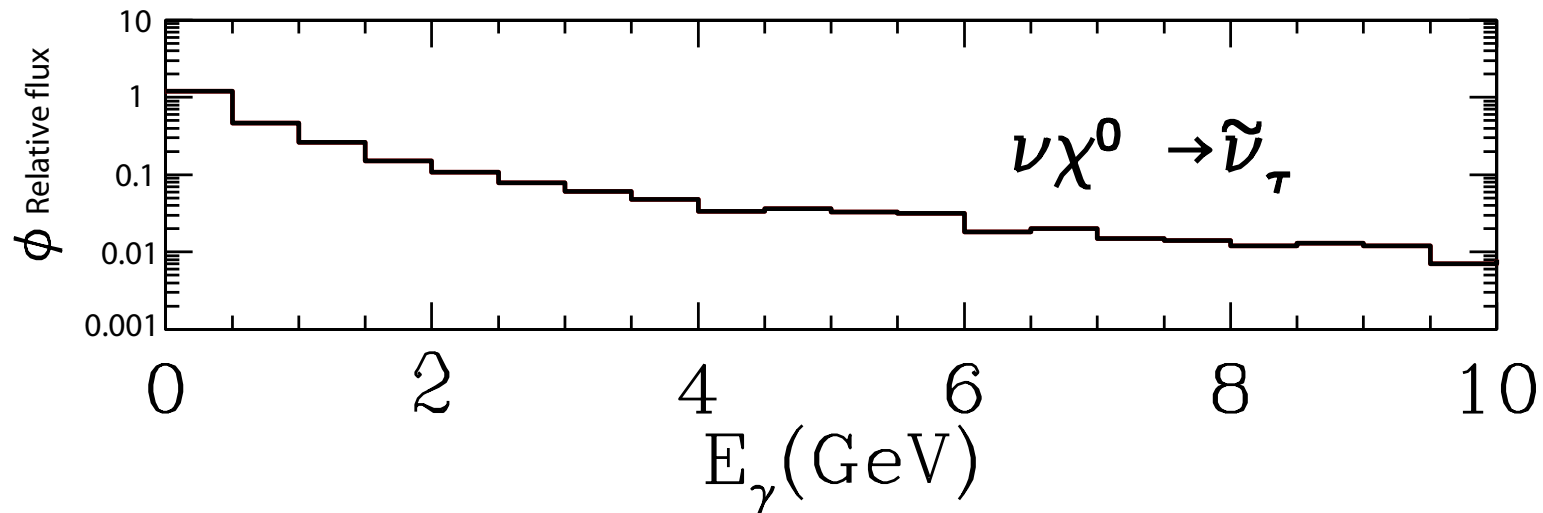
With reasonable  $\nu$  flux,  $dN_\nu/dE_\nu \approx 5 \times 10^{-18} [\text{GeV cm}^2 \text{ s sr}]^{-1}$ ,  
expect  $O(10^{24})$  coannihilations per year in the galaxy

$$\dots \nu \chi_1^0 \rightarrow \tilde{\nu}$$

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Few-GeV  $\gamma$  signals from inelastic decay channels, *most prominent for  $\nu_\tau$*   
 ... for the right kind of neutralino dark matter (GLAST regime)



## VIII Gravitational Lensing of Neutrinos?

*How demonstrate that neutrinos have normal gravitational interactions?*

Analogue of Pound–Rebka experiment exploiting Mössbauer effect?

Arrival time of SN1987A neutrinos, photons      Longo, Krauss & Tremaine

Lack steady sources, angular resolution to see deflection by the Sun

Lensing Supernova neutrinos by black hole at galactic center:  
significant amplification, time dispersion

Mena, Mocioiu, CQ

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“It is a part of probability that many improbable things will happen.”

George Eliot (after Aristotle), *Daniel Deronda*

Mena, Mocioiu, CQ

# From Neutrino Astronomy to Particle Physics

Prospects for probing particle physics in neutrino telescopes will be greatly enhanced by

- recording, characterizing energy of NC events
- neutrino flavor tagging, with energy measurement
- attention to surprises (e.g., misplaced absorption lines)
- sensitivity to TeV- $\gamma$  signals from  $\nu$  coannihilation ( $\gamma$ -ray telescopes)
- SN neutrino bursts from other side of our galaxy

## *Thanks to . . .*

Mary Hall Reno, Terry Walker,  
Raj Gandhi, Ina Sarcevic,  
Marcela Carena, Magda Lola,  
Debajyoti Choudhury, Vu Anh Tuan,  
Gabriela Barenboim, Olga Mena,  
Irina Mocioiu, Stephen Parke



$$\begin{aligned}
U &= \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \\
&= \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}
\end{aligned}$$

$s_{ij} = \sin \theta_{ij}$ ,  $c_{ij} = \cos \theta_{ij}$  and  $\delta$  is a CP-violating phase.

$$\begin{aligned}
\mathcal{X}_{\beta\alpha} &= \delta_{\alpha\beta} - 2\Re \sum_{i>j} U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^* \\
&= \sum_j |U_{\alpha j}|^2 |U_{\beta j}|^2,
\end{aligned}$$

(does not depend on phase  $\delta$ )

Idealized case:  $\theta_{12} = 0.57, x = 0.21$

Current knowledge (95% CL):

$$\begin{aligned} 0.49 < \theta_{12} < 0.67 \\ \frac{\pi}{4} \times 0.8 < \theta_{23} < \frac{\pi}{4} \times 1.2 \\ 0 < \theta_{13} < 0.1 \end{aligned}$$

After next round (95% CL):

$$\begin{aligned} 0.54 < \theta_{12} < 0.63 \\ \frac{\pi}{4} \times 0.9 < \theta_{23} < \frac{\pi}{4} \times 1.1 \\ 0 < \theta_{13} < 0.1 \end{aligned}$$