

Physics Beyond the Standard Model

First sign - Neutrino Mass

Possibilities:

1. Add $\nu_R \rightarrow \nu_L \nu_R \Phi$

\rightarrow Usual Dirac masses

Problem: Largest $m_\nu < 10^{-6} m_e$

2. New physics at large scale $M \rightarrow$

$$\nu_L \nu_L \Phi \Phi / M$$

\rightarrow Majorana masses $\sim \frac{v^2}{M}$

3. Add ν_R with a large Majorana mass $M_R \rightarrow$

$$\left(\begin{array}{c|c} m_D & \\ \hline m_D & M_R \end{array} \right) \rightarrow$$

Majorana mass $\sim \frac{m_D^2}{M_R}$

See-saw formula

THEORETICAL MOTIVATION

QUARK-LEPTON SYMMETRY

$$\begin{pmatrix} u \\ d \end{pmatrix} \quad \begin{pmatrix} c \\ s \end{pmatrix} \quad \begin{pmatrix} t \\ b \end{pmatrix}$$

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix} \quad \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix} \quad \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$$

1. Three generations
2. Mass hierarchy
3. Same weak interactions

If symmetry becomes exact
 ν_{Ri} must exist $\rightarrow \nu$ mass

GM-R-S solution: when
 symmetry is broken ν gets mass!

$$m_\nu \sim \frac{m_D^2}{M}$$

$$L \begin{pmatrix} 0 & m_D \\ m_D & M \end{pmatrix} R$$

SO(10) GUT

(14)

$$\Psi_{16} = \begin{pmatrix} u_{iL} & d_{iL} & N_L & e_L \\ u^c_{iL} & d^c_{iL} & N^c_L & e^c_L \end{pmatrix}$$

one generation

$i = \text{color}$

$$\Psi_{16} \sim \underline{16} \quad \overline{\Psi_{16}} \sim \overline{16} \text{ Majorana}$$

$$\Psi^c_{16} \sim \overline{16}$$

$$Y \sim \overline{\Psi^c_{16}} \Psi_{16} \sim \underline{16} \times \underline{16}$$

$$= \underline{10} + \underline{120} + \underline{126}$$

$$Y = F_{10} [\overline{\Psi^c_{16}} \Psi_{16}]_{10} \phi_{10} + F_{120} [\overline{\Psi^c_{16}} \Psi_{16}]_{120} \phi_{120}$$

$$+ F_{126} [\overline{\Psi^c_{16}} \Psi_{16}]_{126} \phi_{126}$$

This \rightarrow both Dirac & Majorana mass terms

6 Light Neutrino Model

Add a $U(1)$ for which

$$\nu_R \quad R=1$$

$$\text{Scalar } \gamma \quad R=-1$$

Violate L

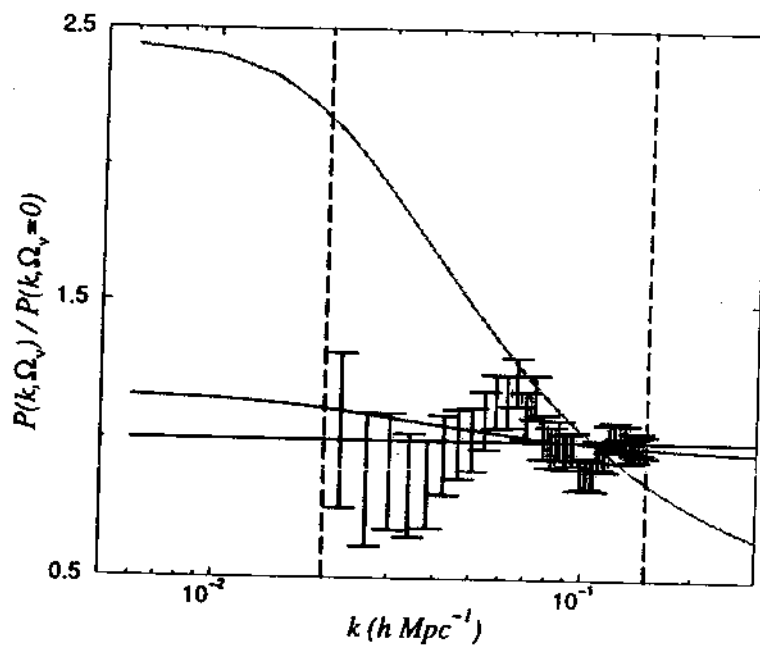
$$\begin{aligned} & \nu_L \nu_L \phi \phi / M_1 + \nu_R \nu_R \gamma \gamma / M_2 \\ & + \nu_L \nu_R \phi \gamma / M_3 \end{aligned}$$

3 Sterile ν mixed in

LSND

Elgorty
astro-ph/0303089
 $\Sigma m_\nu < 1 \text{ eV}$
 $m_1 < \frac{1}{3} \text{ eV}$

fits on neutrino masses from the 2dFGRS and WMAP: the role of priors



$\Sigma m_\nu \sim 2.1$

↑

Figure 3. Ratio of power spectra for $\Omega_\nu = 0.01$ (bottom line) and $\Omega_\nu = 0.05$ (top line) to the one for $\Omega_\nu = 0$ (horizontal line) with amplitudes fitted to the 2dFGRS power spectrum data (vertical bars) in redshift space. We have fixed $\Omega_m = 0.3$, $h = 0.7$, and $\Omega_b h^2 = 0.02$. The vertical dashed lines limit the range in k used in the fits.

power spectrum is not affected by redshift space distortions

Astrophysics

1. ν from the Sun

2. Type II Supernovae

> 99% of energy in

ν of all types in ~ 10 sec

19 $\bar{\nu}_e$ from SN 1987a

10^{58} were emitted

ν oscillations can change the spectrum

3. Very high E ν from

γ ray bursts? AGN?

Solar Neutrinos

1. Verifying the theory of solar energy

2. Prototypical problem of astrophysics:

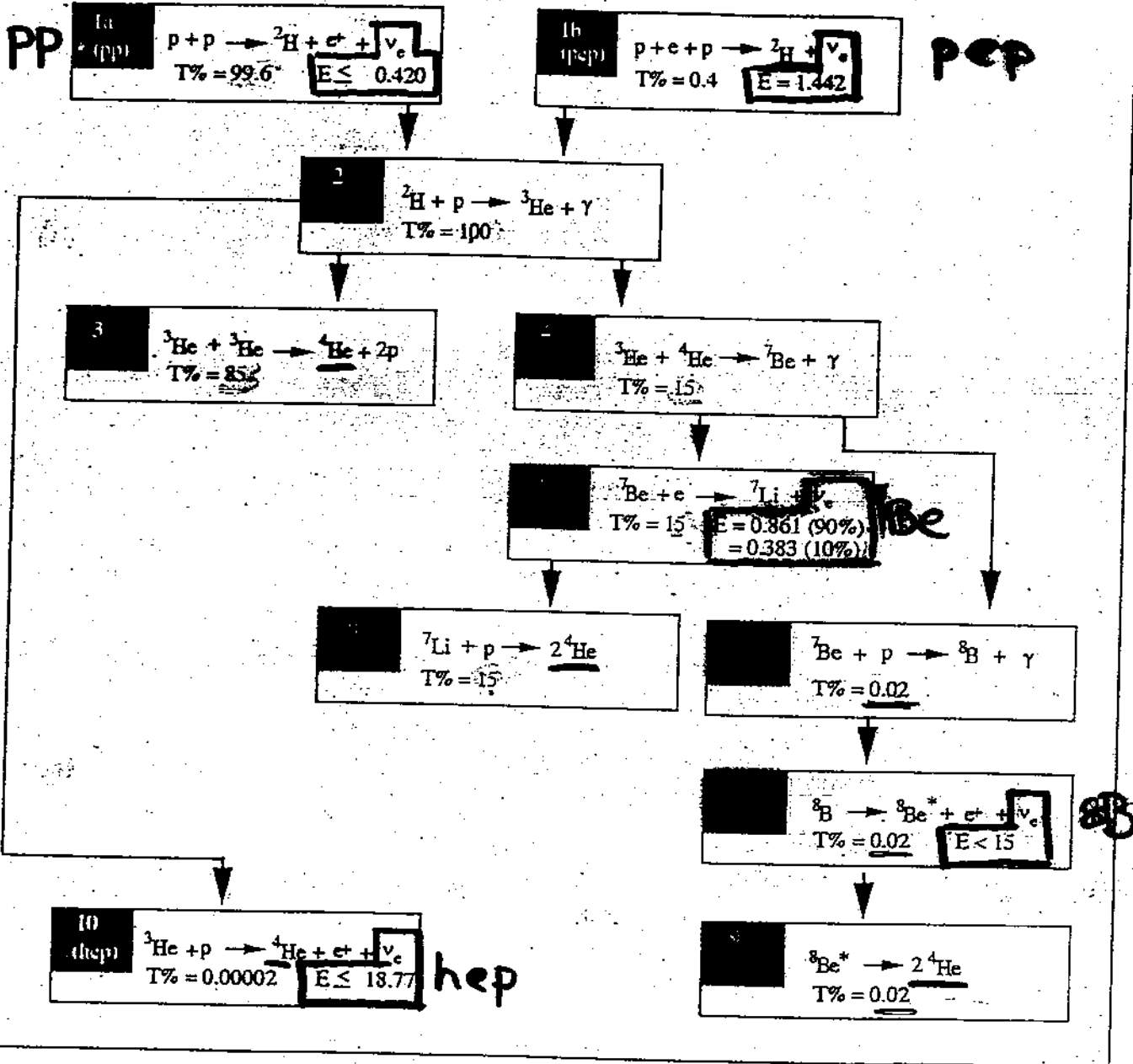
So the problem the ν on the Sun

The wonderful solution
SNO (Herb Chen)

$$\frac{\nu_e}{\nu_e + \nu_\mu + \nu_\tau} \approx \frac{1}{3}$$

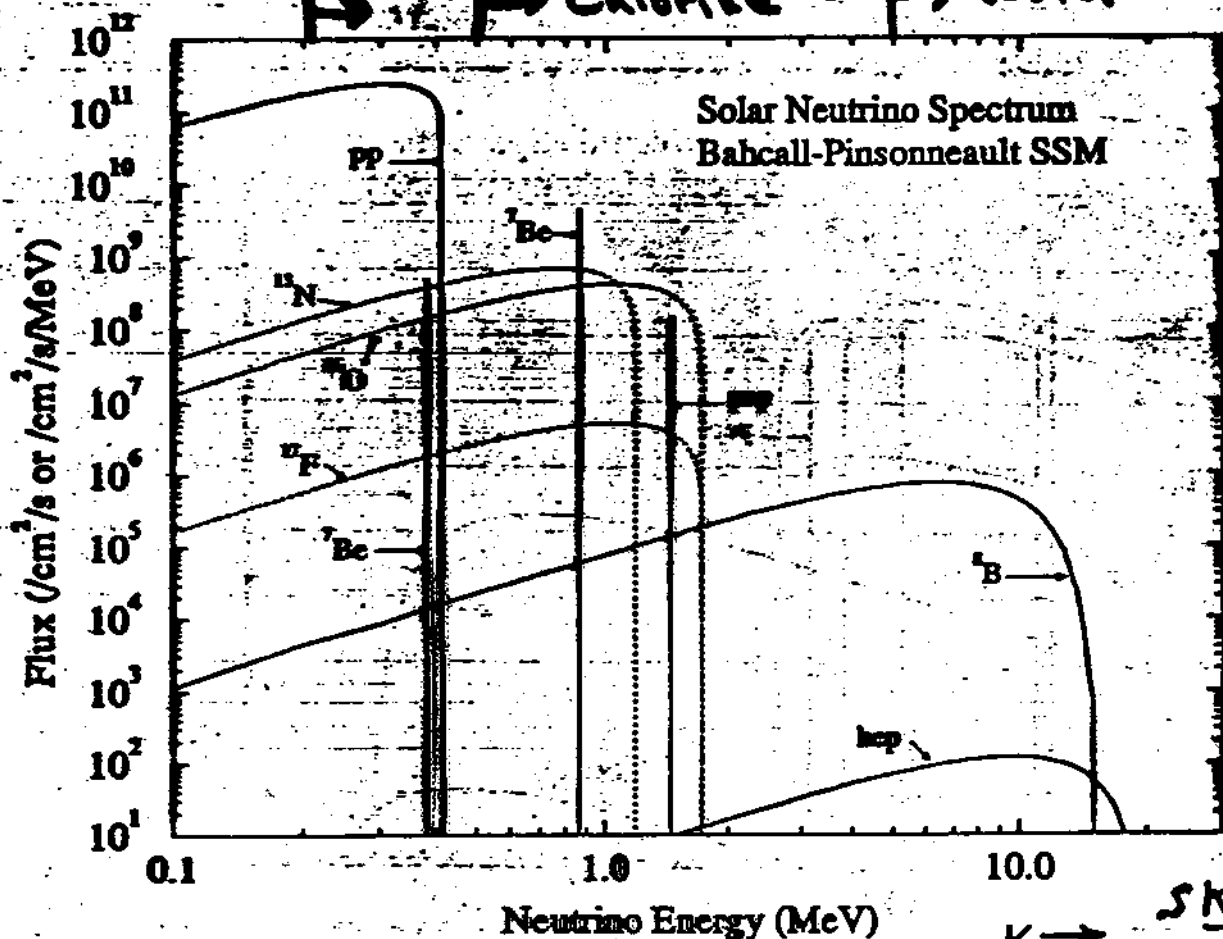
Solar Energy Production

The Proton-Proton (pp) Chain in the Sun



Bahca

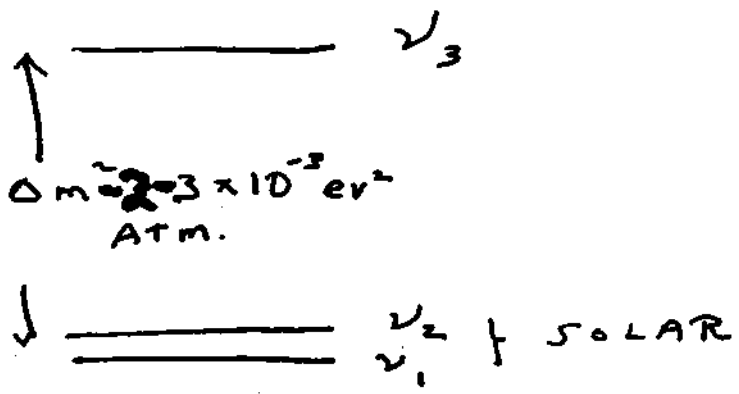
Gallium → Chlorine → Water



← K → $\frac{SKAM}{SSM} = .47 \pm .02$

← DAVIS → $\frac{DAVIS}{SSM} = .33 \pm .0$

← GALLIUM → $\frac{GA}{SSM} = .56 \pm .01$



LMA-MSW
 $\theta \sim 45^\circ$
 $\Delta m_{12}^2 \sim 10^{-5} \text{ eV}^2$

$$\nu_3 = (\nu_\mu + \nu_\tau) / \sqrt{2} + s_{13} \nu_e$$

$$\nu_2 = \sin \theta_\odot \nu_e + \cos \theta_\odot (\nu_\mu - \nu_\tau) / \sqrt{2}$$

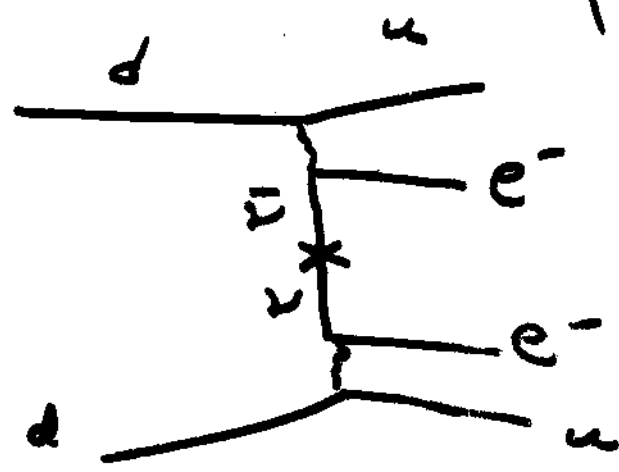
$$\nu_1 = -\cos \theta_\odot \nu_e + \sin \theta_\odot (\nu_\mu - \nu_\tau) / \sqrt{2}$$

MAJOR QUESTIONS

1. $s_{13} = |s_{13}| e^{i\delta}$ What is $|s_{13}|, \delta$?
2. Inverse hierarchy?
3. Solar solution: $\Delta m_{12}^2, \theta_\odot$
4. Non standard: $\nu_{sterile}, \text{FCNC}, \dots$
5. What is m_1 ?
6. Majorana or Dirac?
7. 2 Majorana phases?

Possible signal for a Majorana ν is Neutrinoless Double β -Decay

$$(Z, A) \rightarrow (Z+2, A) + 2e^-$$



" $m(\nu_e)$ " $\leq 0.5\text{eV}$ from ${}^{76}\text{Ge}$ depends on nuclear calculations

$$\text{really } "m(\nu_e)" = \sum_{\alpha} \eta_{\alpha} |U_{e\alpha}|^2 m_{\alpha}$$

$$\eta_2 \text{ and } \eta_3 = \pm 1$$

are CP eigenvalues of Majorana ν
or $\eta_2 = e^{i\theta}$ $\eta_3 = e^{i\phi}$

CP Violation in ν Oscillation (Detecting the phase δ)

$$P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$$

1. Rate is proportional to S_{13}^2
2. Difference depends not only on Δm_{32}^2 , but also Δm_{21}^2

Requires long baseline and/or low

3. In matter the difference is not a direct sign of CP.

Fit data to S_{13} and S_{red} hierro

4. T violation ("no matter effect")

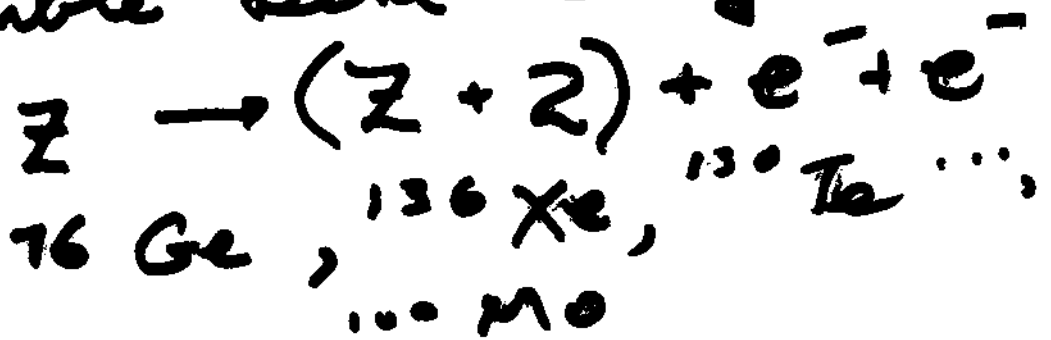
$$\text{of } \nu_\mu \rightarrow \nu_e \text{ with } \nu_e \rightarrow \nu_\mu$$

Neutrinos (Steering Committee, APS Study)

1. Solar neutrinos

- ${}^7\text{Be} \nu$ - Borexino
- ${}^8\text{B} \nu$ - R+D

2. Double beta decay



3. Mixing matrix

$$\begin{pmatrix}
 \sqrt{\frac{2}{3}} & \sqrt{\frac{1}{3}} & \theta_{13} e^{i\delta} \\
 \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\
 -\frac{1}{\sqrt{6}} & -\frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}}
 \end{pmatrix}$$

- Detect θ_{13} - (1) Reactor
 (2) Off-axis Formula
 (3) SPARK to SK Korea

Are there questions with
no answers?

1. Why this cast of character

e, u, T, v_1, v_2, v_3

a, d, s, t, b

2. Why baryons (not anti-b)

Ω_b

Lessons from Kepler:

1. Why only 6 planets?

Past 20 Years

I. Neutrino Astronomy

1. Solar neutrinos
2. Supernova 1987a

II. Particle Physics

1. Neutrino mass - the first signal of physics beyond the standard model
2. Neutrino mass is the first component of dark matter identified

Next 20 Years

I. Neutrino Astronomy

1. Complete solar neutrino detection
Be and pp neutrinos
2. Supernova watch
3. Extra-galactic neutrino search

II. Particle Physics

1. Dirac or Majorana
2. S_{13} and CP Violation
3. Sterile neutrinos?