

---

# BENE workshop

*Resolving parameter degeneracies in long-baseline experiments with atmospheric neutrino data*

Thomas Schwetz

SISSA, Trieste

based on:

P. Huber, M. Maltoni, TS, hep-ph/0501037

# *Outline*

---

- Introduction
- Parameter degeneracies in LBL experiments
- Three-flavour effects in ATM experiments
- Resolving the degeneracies by a combined LBL and ATM analysis
  - simulation of the T2K-II experiment
  - preliminary analysis of CERN-Frejus experiments
- Concluding remarks

# *Introduction*

---

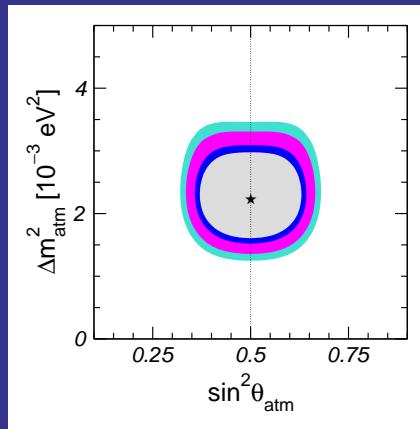
3-flavour neutrino oscillation parameters:

$$\Delta m_{31}^2 \qquad \qquad \qquad \Delta m_{21}^2$$
$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

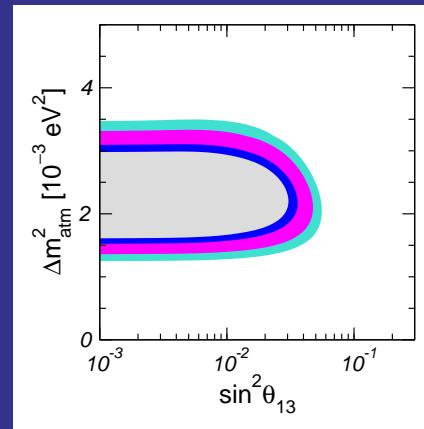
# Introduction

3-flavour neutrino oscillation parameters:

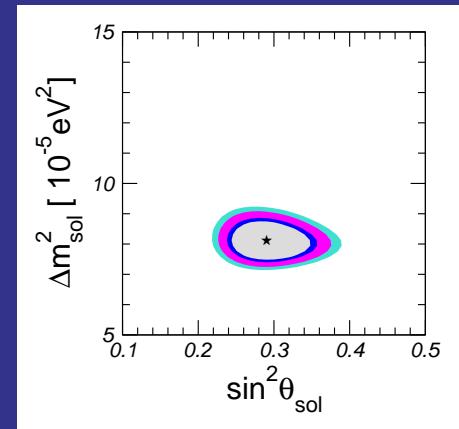
$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
$$|\Delta m_{31}^2| \quad \quad \quad \Delta m_{21}^2$$



atmospheric + K2K



CHOOZ



solar + KamLAND

Maltoni, Schwetz, Tortola, Valle, hep-ph/0405172

# Introduction

3-flavour neutrino oscillation parameters:

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{-i\delta} s_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\frac{|\Delta m_{31}^2|}{10^{-3} \text{ eV}^2} = 2.2^{+0.37}_{-0.27} \quad (14\%)$$

$$\sin^2 \theta_{23} = 0.50^{+0.06}_{-0.05} \quad (11\%)$$

atmospheric + K2K

$$\sin^2 \theta_{13} < 0.05 \text{ } (3\sigma)$$

CHOOZ

$$\frac{|\Delta m_{21}^2|}{10^{-5} \text{ eV}^2} = 7.9 \pm 0.3 \quad (4\%)$$

$$\sin^2 \theta_{12} = 0.30^{+0.03}_{-0.02} \quad (9\%)$$

solar + KamLAND

Maltoni, Schwetz, Tortola, Valle, hep-ph/0405172

# *Introduction*

---

Open questions:

# *Introduction*

---

Open questions:

- How small is  $\theta_{13}$ ?

# *Introduction*

---

## Open questions:

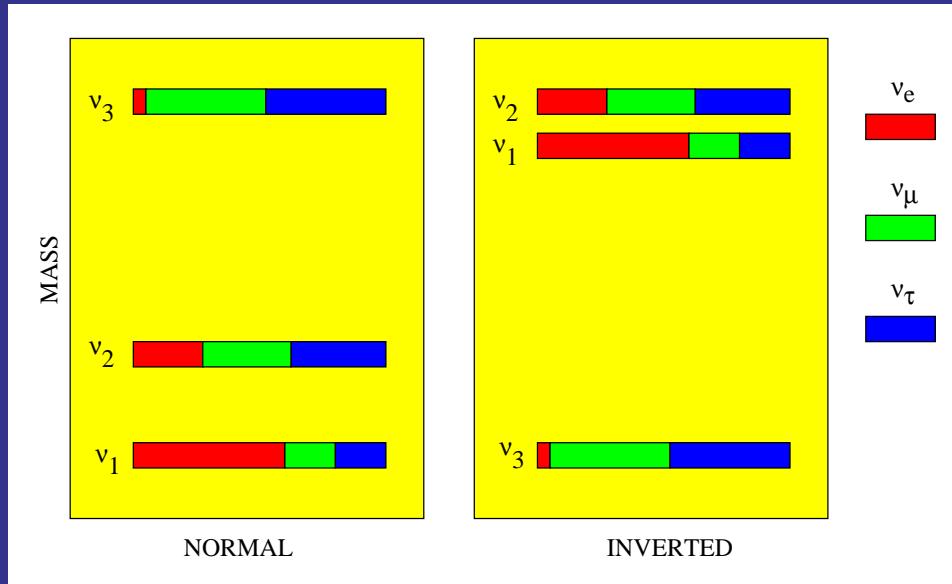
- How small is  $\theta_{13}$ ?
- What is the value of the CP phase  $\delta_{\text{CP}}$ ?

# *Introduction*

---

## Open questions:

- How small is  $\theta_{13}$ ?
- What is the value of the CP phase  $\delta_{\text{CP}}$ ?
- Type of the neutrino mass ordering (sign of  $\Delta m_{31}^2$ )



---

# Parameter degeneracies in LBL experiments

- M. Koike, T. Ota, J. Sato, Phys. Rev. D65 (2002) 053015  
J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301  
H. Minakata, H. Nunokawa, JHEP 10 (2001) 001  
G.L. Fogli, E. Lisi, Phys. Rev. D54 (1996) 3667  
V.Barger, D.Marfatia, K.Whisnant, Phys. Rev. D65 (2002) 073023; D66 (2002) 053007  
P.Huber, M.Lindner, W.Winter, Nucl. Phys. B645 (2002) 3; Nucl. Phys. B654 (2003) 3  
J. Burguet-Castell et al., Nucl.Phys. B646 (2002) 301  
A.Donini, D.Meloni, S.Rigolin, JHEP 0406 (2004) 011

and many more (I appologize for omissions)

# *The $\nu_\mu \rightarrow \nu_e$ oscillation probability*

---

$P_{\mu e}$  in vacuum to leading order in  $\sin^2 2\theta_{13}$  and  $\alpha$

$$\begin{aligned} P_{\mu e} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta_{31} \\ &+ \alpha \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \Delta_{31} \sin \Delta_{31} \cos(\Delta_{31} \pm \delta_{\text{CP}}) \\ &+ \alpha^2 \sin^2 2\theta_{12} \cos^2 \theta_{23} \Delta_{31}^2 \end{aligned}$$

with

$$\alpha \equiv \frac{\Delta m_{21}^2}{\Delta m_{31}^2}, \quad \Delta_{31} \equiv \frac{\Delta m_{31}^2 L}{4E_\nu}$$

# *The 8-fold degeneracy*

---

- The **intrinsic** or  $(\delta_{\text{CP}}, \theta_{13})$  degeneracy

M. Koike, T. Ota, J. Sato, Phys. Rev. D65 (2002) 053015

J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301

several solutions in the  $(\delta_{\text{CP}}, \theta_{13})$  plane

$$\begin{aligned} P_{\mu e} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta_{31} + \alpha^2 \sin^2 2\theta_{12} \cos^2 \theta_{23} \Delta_{31}^2 \\ &+ \alpha \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \Delta_{31} \sin \Delta_{31} \cos(\Delta_{31} \pm \delta_{\text{CP}}) \end{aligned}$$

# *The 8-fold degeneracy*

---

- The **intrinsic** or  $(\delta_{CP}, \theta_{13})$  degeneracy

M. Koike, T. Ota, J. Sato, Phys. Rev. D65 (2002) 053015

J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301

several solutions in the  $(\delta_{CP}, \theta_{13})$  plane

- The **hierarchy** or  $\text{sgn}(\Delta m_{31}^2)$  degeneracy

H. Minakata, H. Nunokawa, JHEP 10 (2001) 001

solutions for both signs of  $\Delta m_{31}^2$  (affects mainly  $\delta_{CP}$ )

$$\begin{aligned} P_{\mu e} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta_{31} + \alpha^2 \sin^2 2\theta_{12} \cos^2 \theta_{23} \Delta_{31}^2 \\ &+ \alpha \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \Delta_{31} \sin \Delta_{31} \cos(\Delta_{31} \pm \delta_{CP}) \end{aligned}$$

# *The 8-fold degeneracy*

---

- The **intrinsic** or  $(\delta_{CP}, \theta_{13})$  degeneracy

M. Koike, T. Ota, J. Sato, Phys. Rev. D65 (2002) 053015

J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301

several solutions in the  $(\delta_{CP}, \theta_{13})$  plane

- The **hierarchy** or  $\text{sgn}(\Delta m_{31}^2)$  degeneracy

H. Minakata, H. Nunokawa, JHEP 10 (2001) 001

solutions for both signs of  $\Delta m_{31}^2$  (affects mainly  $\delta_{CP}$ )

- The **octant** or  $\theta_{23}$  degeneracy

G.L. Fogli, E. Lisi, Phys. Rev. D54 (1996) 3667

$\nu_\mu$ -disappearance channel gives only  $\sin^2 2\theta_{23}$

solutions for  $\theta_{23}$  and  $\pi/2 - \theta_{23}$  (affects mainly  $\sin^2 2\theta_{13}$ )

$$\begin{aligned} P_{\mu e} &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta_{31} + \alpha^2 \sin^2 2\theta_{12} \cos^2 \theta_{23} \Delta_{31}^2 \\ &+ \alpha \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \Delta_{31} \sin \Delta_{31} \cos(\Delta_{31} \pm \delta_{CP}) \end{aligned}$$

# *The 8-fold degeneracy*

---

- The **intrinsic** or  $(\delta_{CP}, \theta_{13})$  degeneracy

M. Koike, T. Ota, J. Sato, Phys. Rev. D65 (2002) 053015

J. Burguet-Castell et al., Nucl. Phys. B608 (2001) 301

several solutions in the  $(\delta_{CP}, \theta_{13})$  plane

- The **hierarchy** or  $\text{sgn}(\Delta m_{31}^2)$  degeneracy

H. Minakata, H. Nunokawa, JHEP 10 (2001) 001

solutions for both signs of  $\Delta m_{31}^2$  (affects mainly  $\delta_{CP}$ )

- The **octant** or  $\theta_{23}$  degeneracy

G.L. Fogli, E. Lisi, Phys. Rev. D54 (1996) 3667

$\nu_\mu$ -disappearance channel gives only  $\sin^2 2\theta_{23}$

solutions for  $\theta_{23}$  and  $\pi/2 - \theta_{23}$  (affects mainly  $\sin^2 2\theta_{13}$ )

overall an **8-fold degeneracy**

V.Barger, D.Marfatia, K.Whisnant, Phys. Rev. D65 (2002) 073023

# *The T2K-II long-baseline experiment*

---

4 MW superbeam at JPARC  
mean neutrino energy: 0.76 GeV (2° OA)  
1 Mt Cherenkov detector at Kamioka  
baseline: 295 km

	$\nu$ (2 Mt yrs)	$\bar{\nu}$ (6 Mt yrs)
$\nu_\mu \rightarrow \nu_e$ signal	21 300	16 000
$\nu_\mu \rightarrow \nu_e$ background	2 140	3 260
$\nu_\mu \rightarrow \nu_\mu$ signal	73 200	75 600
$\nu_\mu \rightarrow \nu_\mu$ background	340	320

$$\sin^2 2\theta_{13} = 0.05, \sin^2 \theta_{23} = 0.5, \sin^2 \theta_{12} = 0.3, \delta_{\text{CP}} = 0,$$
$$\Delta m_{21}^2 = 8.1 \times 10^{-5} \text{ eV}^2, \Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

# *Analysis method*

---

Calculation of event rates for given experiment:

$$N_i(\alpha) = \Phi \cdot \sigma \cdot R \cdot \epsilon \cdot P(\hat{\theta})$$

$\Phi$ : neutrino flux

$\sigma$ : detection cross section

$R$ : energy resolution

$\epsilon$ : efficiencies

$P(\hat{\theta})$ : 3-flavour osc. prob.,  $\hat{\theta} = (\Delta m_{21}^2, \Delta m_{31}^2, \theta_{12}, \theta_{23}, \theta_{13}, \delta)$

# *Analysis method*

---

Calculation of event rates for given experiment:

$$N_i(\alpha) = \Phi \cdot \sigma \cdot R \cdot \epsilon \cdot P(\hat{\theta})$$

$\Phi$ : neutrino flux

$\sigma$ : detection cross section

$R$ : energy resolution

$\epsilon$ : efficiencies

$P(\hat{\theta})$ : 3-flavour osc. prob.,  $\hat{\theta} = (\Delta m_{21}^2, \Delta m_{31}^2, \theta_{12}, \theta_{23}, \theta_{13}, \delta)$

simulate data for “true values”  $\hat{\theta}^{\text{true}}$ :  $N_i(\hat{\theta}^{\text{true}})$

$\chi^2(\hat{\theta}; \hat{\theta}^{\text{true}})$  → allowed regions for  $\hat{\theta}$

including systematical errors, correlations, degeneracies

# *Analysis method*

---

Calculation of event rates for given experiment:

$$N_i(\alpha) = \Phi \cdot \sigma \cdot R \cdot \epsilon \cdot P(\hat{\theta})$$

$\Phi$ : neutrino flux

$\sigma$ : detection cross section

$R$ : energy resolution

$\epsilon$ : efficiencies

$P(\hat{\theta})$ : 3-flavour osc. prob.,  $\hat{\theta} = (\Delta m_{21}^2, \Delta m_{31}^2, \theta_{12}, \theta_{23}, \theta_{13}, \delta)$

simulate data for “true values”  $\hat{\theta}^{\text{true}}$ :  $N_i(\hat{\theta}^{\text{true}})$

$\chi^2(\hat{\theta}; \hat{\theta}^{\text{true}})$  → allowed regions for  $\hat{\theta}$

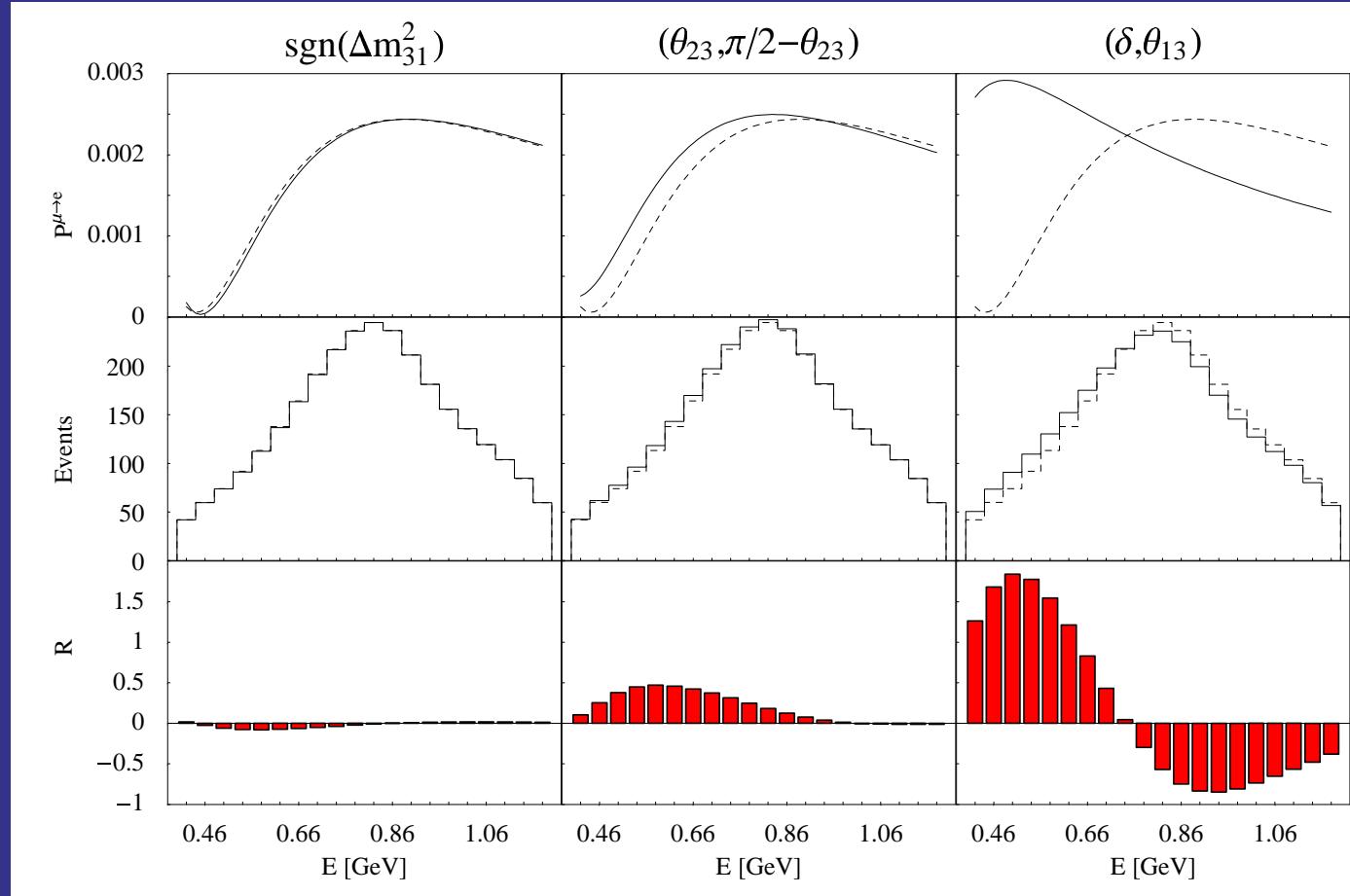
including systematical errors, correlations, degeneracies

**GLoBES software**

P. Huber, M. Lindner, W. Winter, hep-ph/0407333

<http://www.ph.tum.de/~globes/>

# Degeneracies and T2K-II



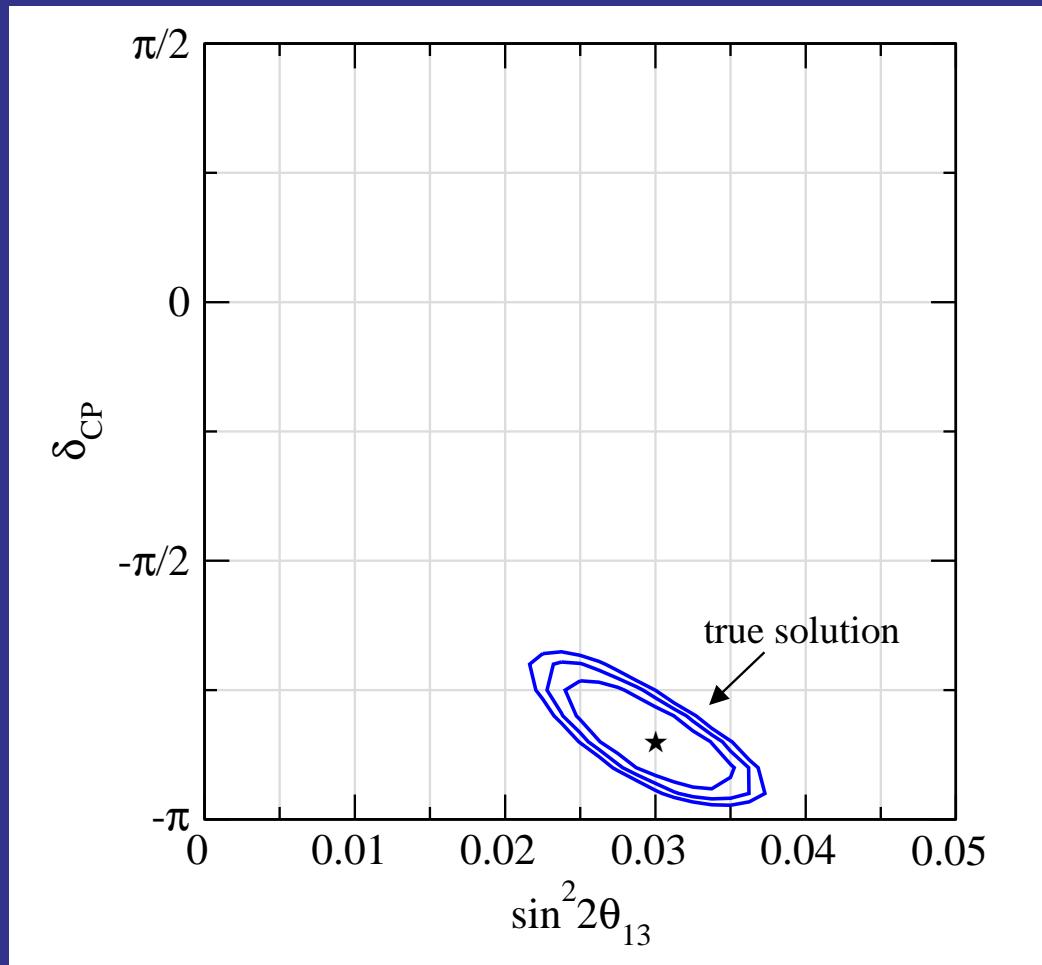
$$\begin{aligned}\sin^2 2\theta_{13} &= 0.01 \\ \delta_{\text{CP}} &= \pi/4 \\ \sin^2 \theta_{23} &= 0.3\end{aligned}$$

$$R = \frac{N_i^{\text{tr}} - N_i^{\text{deg}}}{\sqrt{(N_i^{\text{tr}} + N_i^{\text{deg}})/2}}$$

P.Huber, M.Lindner, W.Winter, Nucl. Phys. B645 (2002) 3

The intrinsic degeneracy is absent for T2K-II

# Degeneracies and T2K-II



True values:

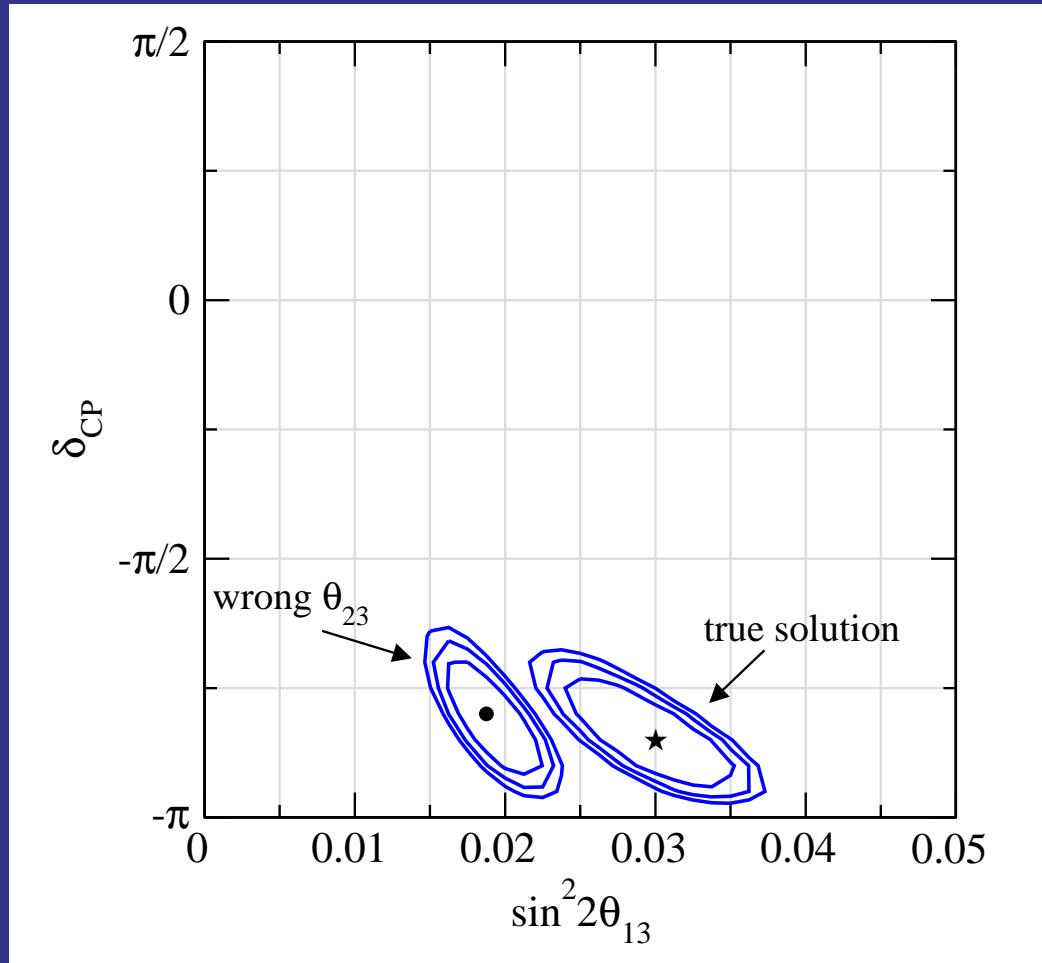
$$\sin^2 2\theta_{13} = 0.03$$

$$\delta_{CP} = -0.85\pi$$

$$\sin^2 \theta_{23} = 0.4$$

$$\Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

# Degeneracies and T2K-II



True values:

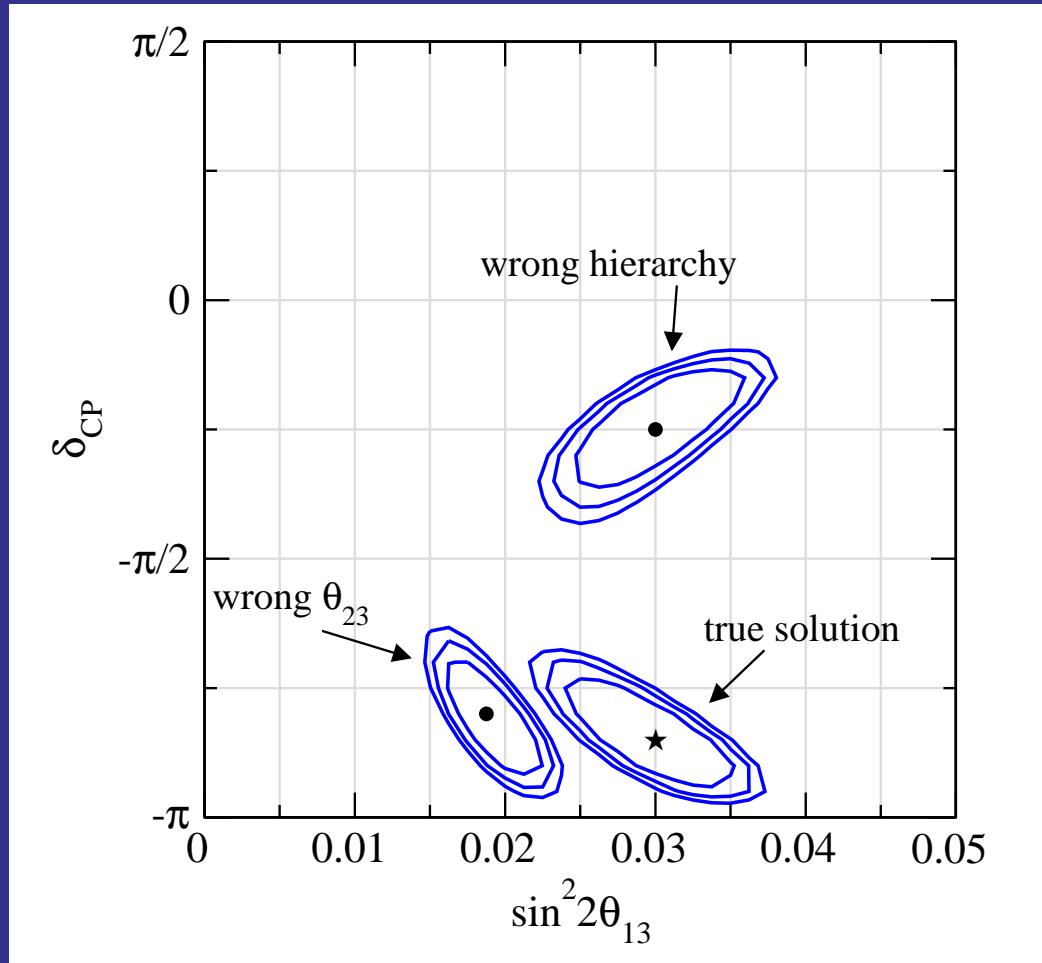
$$\sin^2 2\theta_{13} = 0.03$$

$$\delta_{CP} = -0.85\pi$$

$$\sin^2 \theta_{23} = 0.4$$

$$\Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

# Degeneracies and T2K-II



True values:

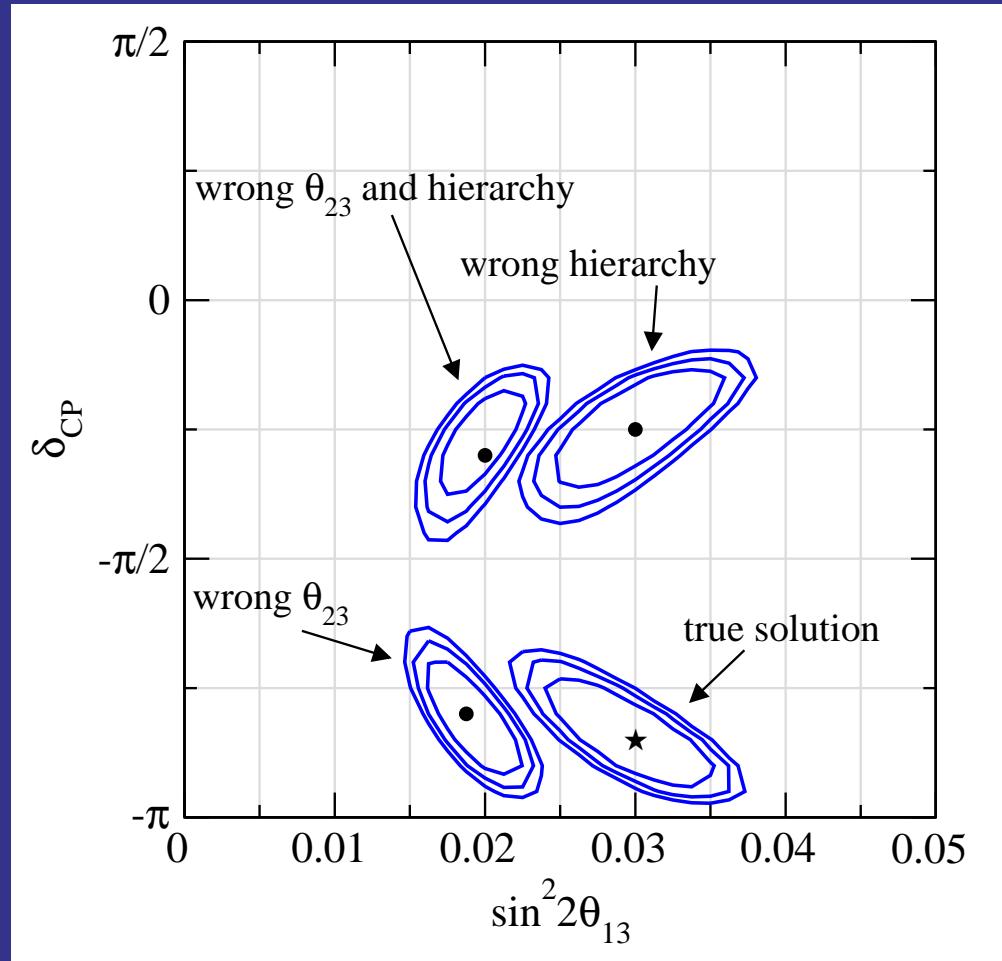
$$\sin^2 2\theta_{13} = 0.03$$

$$\delta_{CP} = -0.85\pi$$

$$\sin^2 \theta_{23} = 0.4$$

$$\Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

# Degeneracies and T2K-II



True values:

$$\sin^2 2\theta_{13} = 0.03$$

$$\delta_{CP} = -0.85\pi$$

$$\sin^2 \theta_{23} = 0.4$$

$$\Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

ambiguities in  $\theta_{13}$  and  $\delta_{CP}$   
no information on the hierarchy

---

## 3-flavour effects in atmospheric neutrinos

Petcov, Phys. Lett. B434, 321 (1998), hep-ph/9805262

Akhmedov, Nucl. Phys. B538, 25 (1999), hep-ph/9805272

Akhmedov, Dighe, Lipari, Smirnov, Nucl. Phys. B542, 3 (1999), hep-ph/9808270

Kim, Lee, Phys. Lett. B444, 204 (1998), hep-ph/9809491

Bernabeu, Palomares-Ruiz, Perez, Petcov, Phys. Lett. B531, 90 (2002), hep-ph/0110071

Bernabeu, Palomares-Ruiz, Petcov, Nucl. Phys. B669, 255 (2003), hep-ph/0305152

Peres, Smirnov, Phys. Lett. B456, 204 (1999), hep-ph/9902312

Peres, Smirnov, Nucl. Phys. B680, 479 (2004), hep-ph/0309312

Gonzalez-Garcia, Maltoni, Eur. Phys. J. C26, 417 (2003), hep-ph/0202218

Gonzalez-Garcia, Maltoni, Smirnov, Phys. Rev. D70, 093005 (2004), hep-ph/0408170

# *3-flavour effects in atmospheric neutrinos*

---

excess of electron-like events:

$$\begin{aligned}\frac{N_e}{N_e^0} - 1 \simeq & (r s_{23}^2 - 1) P_{2\nu}(\Delta m_{31}^2, \theta_{13}) & \theta_{13}\text{-effects} \\ & + (r c_{23}^2 - 1) P_{2\nu}(\Delta m_{21}^2, \theta_{12}) & \Delta m_{21}^2\text{-effects} \\ & - 2 s_{13} s_{23} c_{23} r \operatorname{Re}(A_{ee}^* A_{\mu e}) & \text{interference: } \delta_{\text{CP}}\end{aligned}$$

$$r = r(E_\nu) \equiv \frac{F_\mu^0(E_\nu)}{F_e^0(E_\nu)}$$

$r \approx 2$  (sub-GeV)  
 $r \approx 2.6 - 4.5$  (multi-GeV)

# $\theta_{13}$ -effects

---

$$\frac{N_e}{N_e^0} - 1 \simeq (r s_{23}^2 - 1) P_{2\nu}(\Delta m_{31}^2, \theta_{13})$$

resonant matter effect in  $P_{2\nu}(\Delta m_{31}^2, \theta_{13})$   
for multi-GeV events ( $r \approx 2.6 - 4.5$ )

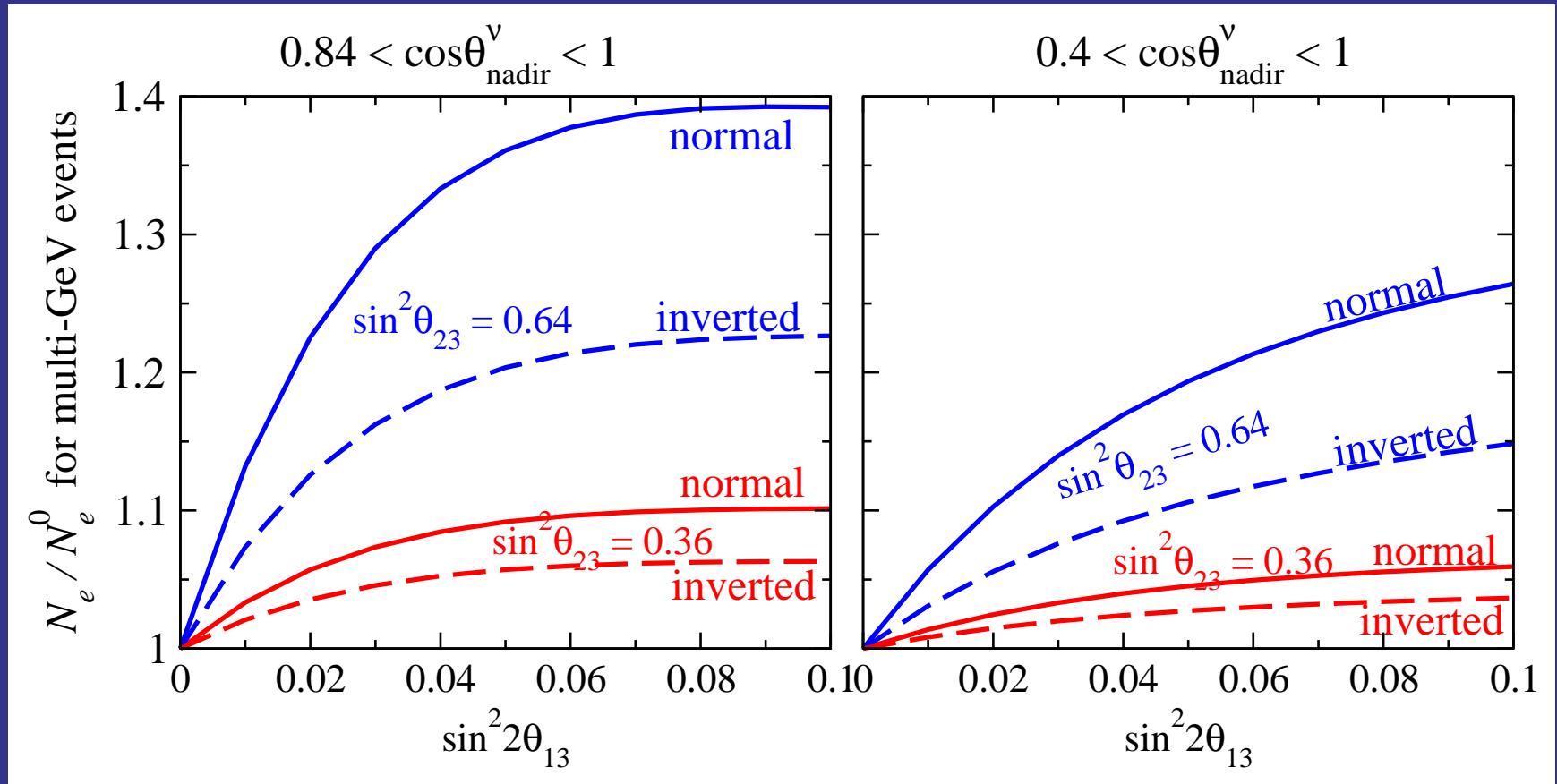
normal hierarchy: enhancement for neutrinos  
inverted hierarchy: enhancement for anti-neutrinos

detection cross sections are different for neutrinos  
and anti-neutrinos

sensitivity to the neutrino mass hierarchy

# $\theta_{13}$ -effects

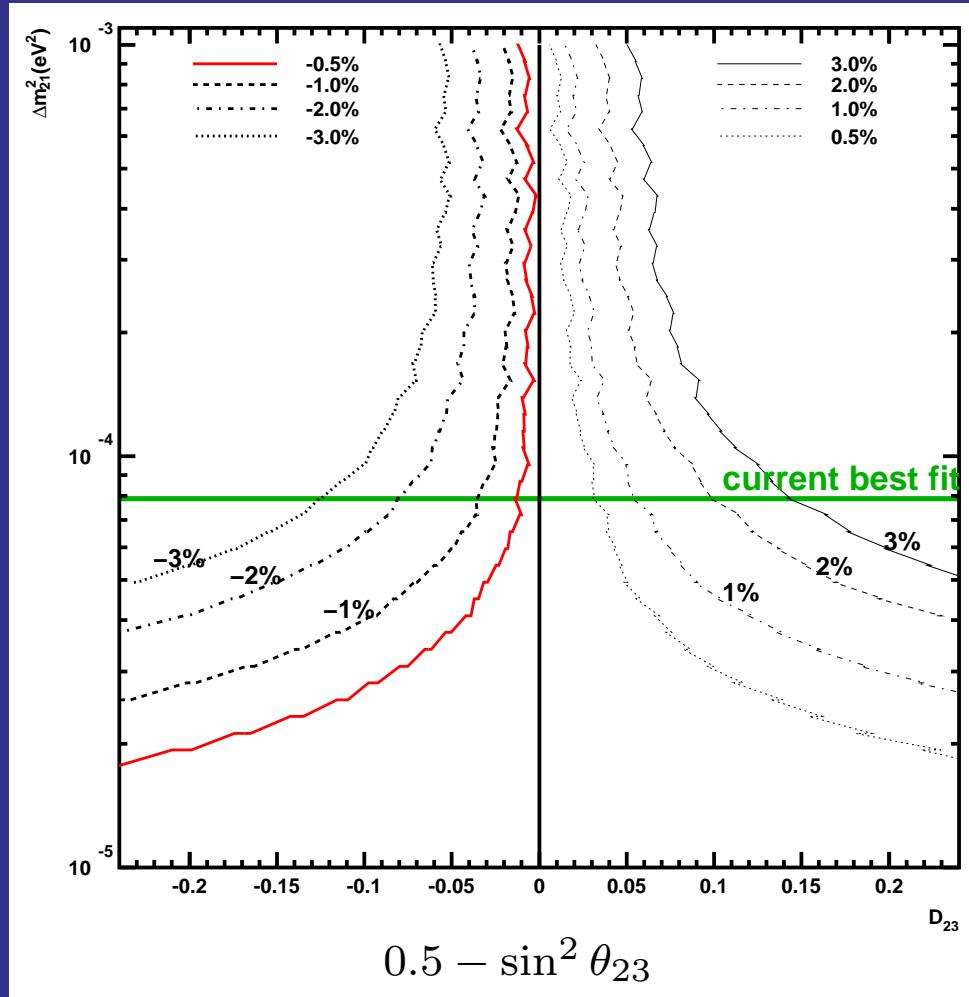
$$\frac{N_e}{N_e^0} - 1 \simeq (r s_{23}^2 - 1) P_{2\nu}(\Delta m_{31}^2, \theta_{13})$$



Bernabeu, Palomares-Ruiz, Petcov, Nucl. Phys. B669, 255 (2003), hep-ph/0305152

# $\Delta m_{21}^2$ -effects

$$\frac{N_e}{N_e^0} - 1 \simeq (r c_{23}^2 - 1) P_{2\nu}(\Delta m_{21}^2, \theta_{12})$$



Peres, Smirnov, hep-ph/0309312

contours of  $\frac{N_e}{N_e^0} - 1$

relevant for sub-GeV events

sensitivity to the octant of  $\theta_{23}$

# *Mega ton atmospheric neutrino experiments*

---

projects for Mt water Cherenkov detectors  
(SK: 22.5 kt)

UNO (US), Hyper-K (Japan), Frejus (Europe)

# *Mega ton atmospheric neutrino experiments*

---

projects for Mt water Cherenkov detectors  
(SK: 22.5 kt)

UNO (US), Hyper-K (Japan), Frejus (Europe)

multi-purpose experiments:

- far-detector for LBL experiments
- solar and atmospheric neutrinos
- supernova neutrinos
- proton decay
- ...

# The HK atmospheric neutrino experiment

---

assume 9 Mt yrs ATM data ( $100 \times$  SK-I data)

	zenith angle	$\nu$	$\bar{\nu}$
$e$ -like sub-GeV	10 bins	239 000	58 000
$e$ -like multi-GeV	10 bins	52 700	18 100
$\mu$ -like sub-GeV	10 bins	232 000	66 200
$\mu$ -like multi-GeV	10 bins	108 000	49 100
upward going $\mu$	$10_{\text{thr}} + 5_{\text{st}}$	127 000	65 400

$$\begin{aligned}\sin^2 2\theta_{13} &= 0.05, \sin^2 \theta_{23} = 0.5, \sin^2 \theta_{12} = 0.3, \delta_{\text{CP}} = 0, \\ \Delta m_{21}^2 &= 8.1 \times 10^{-5} \text{ eV}^2, \Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2\end{aligned}$$

# *The HK atmospheric neutrino experiment*

---

assume 9 Mt yrs ATM data ( $100 \times$  SK-I data)

	zenith angle	$\nu$	$\bar{\nu}$
$e$ -like sub-GeV	10 bins	239 000	58 000
$e$ -like multi-GeV	10 bins	52 700	18 100
$\mu$ -like sub-GeV	10 bins	232 000	66 200
$\mu$ -like multi-GeV	10 bins	108 000	49 100
upward going $\mu$	$10_{\text{thr}} + 5_{\text{st}}$	127 000	65 400

## WARNING:

- same systematics as SK-I

# The HK atmospheric neutrino experiment

---

assume 9 Mt yrs ATM data ( $100 \times$  SK-I data)

	zenith angle	$\nu$	$\bar{\nu}$
$e$ -like sub-GeV	10 bins	239 000	58 000
$e$ -like multi-GeV	10 bins	52 700	18 100
$\mu$ -like sub-GeV	10 bins	232 000	66 200
$\mu$ -like multi-GeV	10 bins	108 000	49 100
upward going $\mu$	$10_{\text{thr}} + 5_{\text{st}}$	127 000	65 400

## WARNING:

- same systematics as SK-I
- same binning (zenith angle, energy) as SK-I

# *The ATM analysis*

---

- Full numerical three-flavour analysis
  - both  $\Delta m_{31}^2$  and  $\Delta m_{21}^2$  taken into account
  - realistic treatment of earth matter effects

based on:

Gonzalez-Garcia, Maltoni, Pena-Garay, Valle, Phys. Rev. D **63** (2001) 033005

Gonzalez-Garcia, Maltoni, Eur. Phys. J. C **26** (2003) 417 [hep-ph/0202218]

Maltoni, TS, Tortola, Valle, Phys. Rev. D **67** (2003) 013011 [hep-ph/0207227]

Gonzalez-Garcia, Maltoni, Smirnov, Phys. Rev. D **70** (2004) 093005 [hep-ph/0408170]

# *The ATM analysis*

---

- Full numerical three-flavour analysis
  - both  $\Delta m_{31}^2$  and  $\Delta m_{21}^2$  taken into account
  - realistic treatment of earth matter effects

based on:

Gonzalez-Garcia, Maltoni, Pena-Garay, Valle, Phys. Rev. D **63** (2001) 033005

Gonzalez-Garcia, Maltoni, Eur. Phys. J. C **26** (2003) 417 [hep-ph/0202218]

Maltoni, TS, Tortola, Valle, Phys. Rev. D **67** (2003) 013011 [hep-ph/0207227]

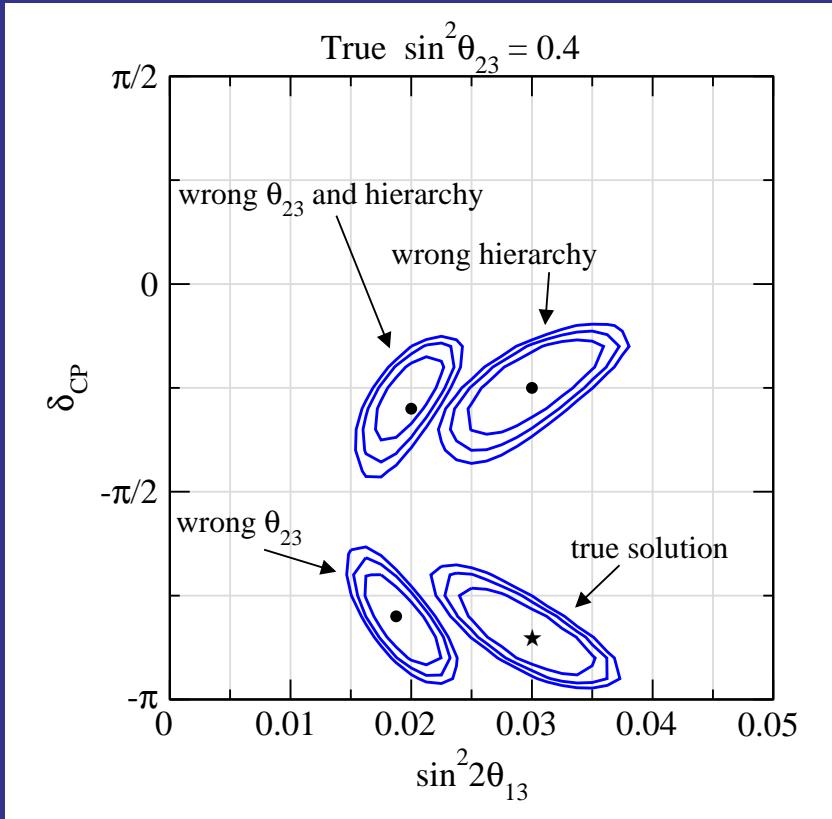
Gonzalez-Garcia, Maltoni, Smirnov, Phys. Rev. D **70** (2004) 093005 [hep-ph/0408170]

- Combined with LBL data by using a generalized version of the GLoBES software

---

# Resolving the degeneracies

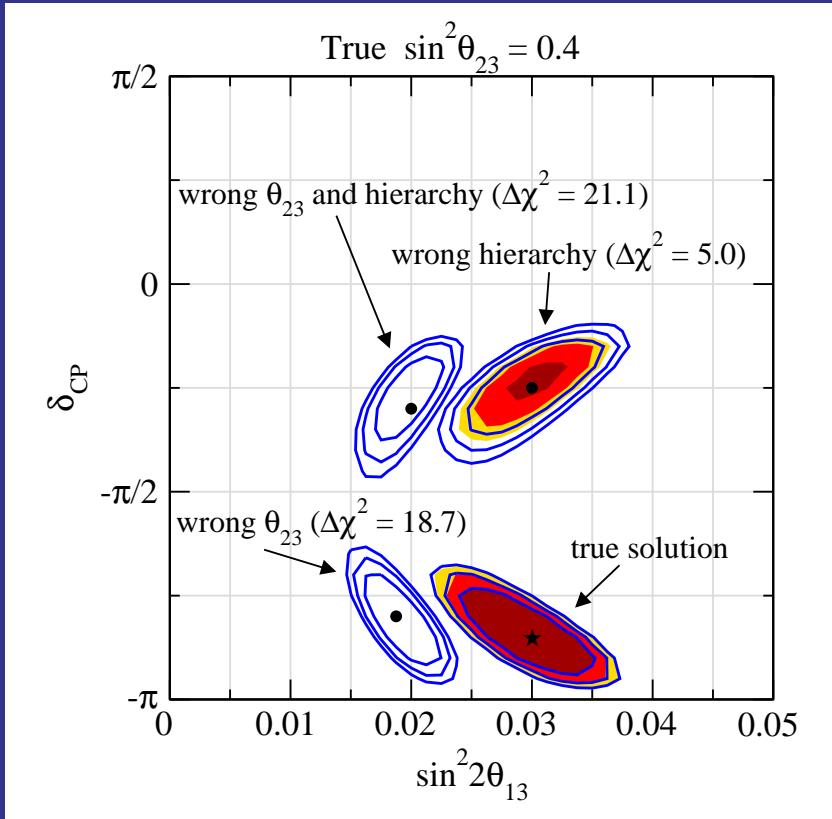
# *Resolving the degeneracies*



True values:

$$\sin^2 2\theta_{13} = 0.03, \delta_{\text{CP}} = -0.85\pi, \Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

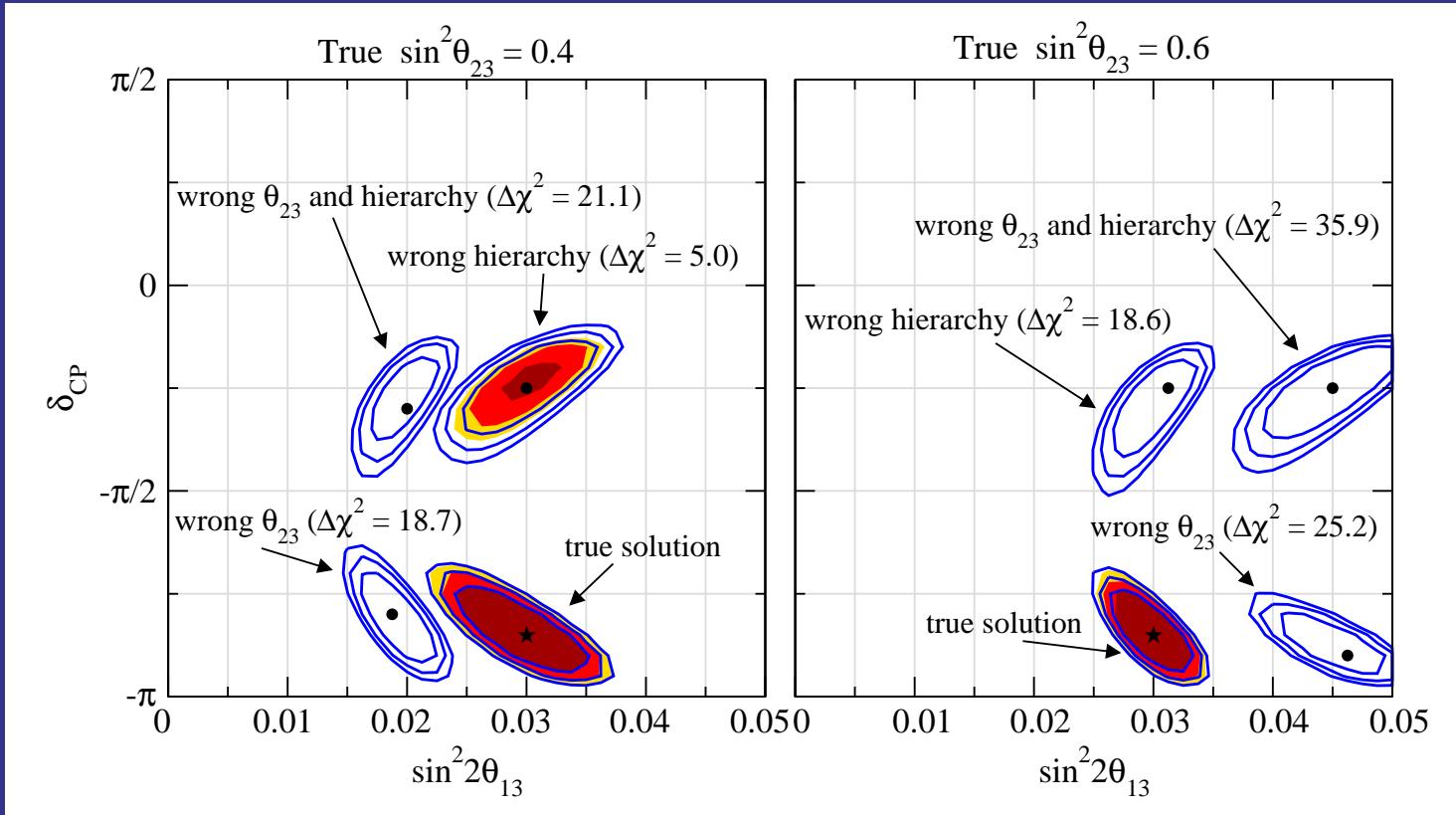
# *Resolving the degeneracies*



True values:

$$\sin^2 2\theta_{13} = 0.03, \delta_{\text{CP}} = -0.85\pi, \Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

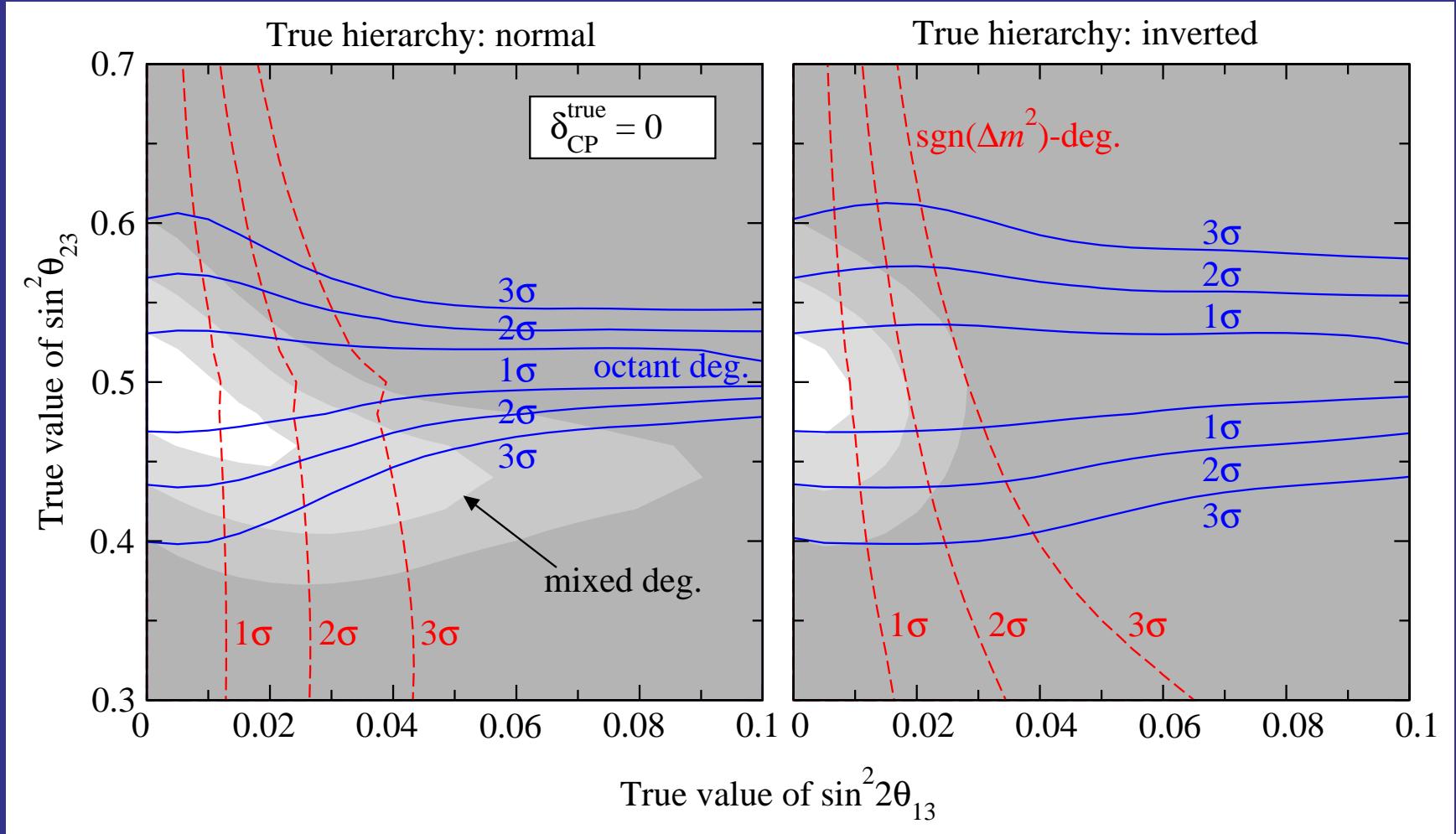
# Resolving the degeneracies



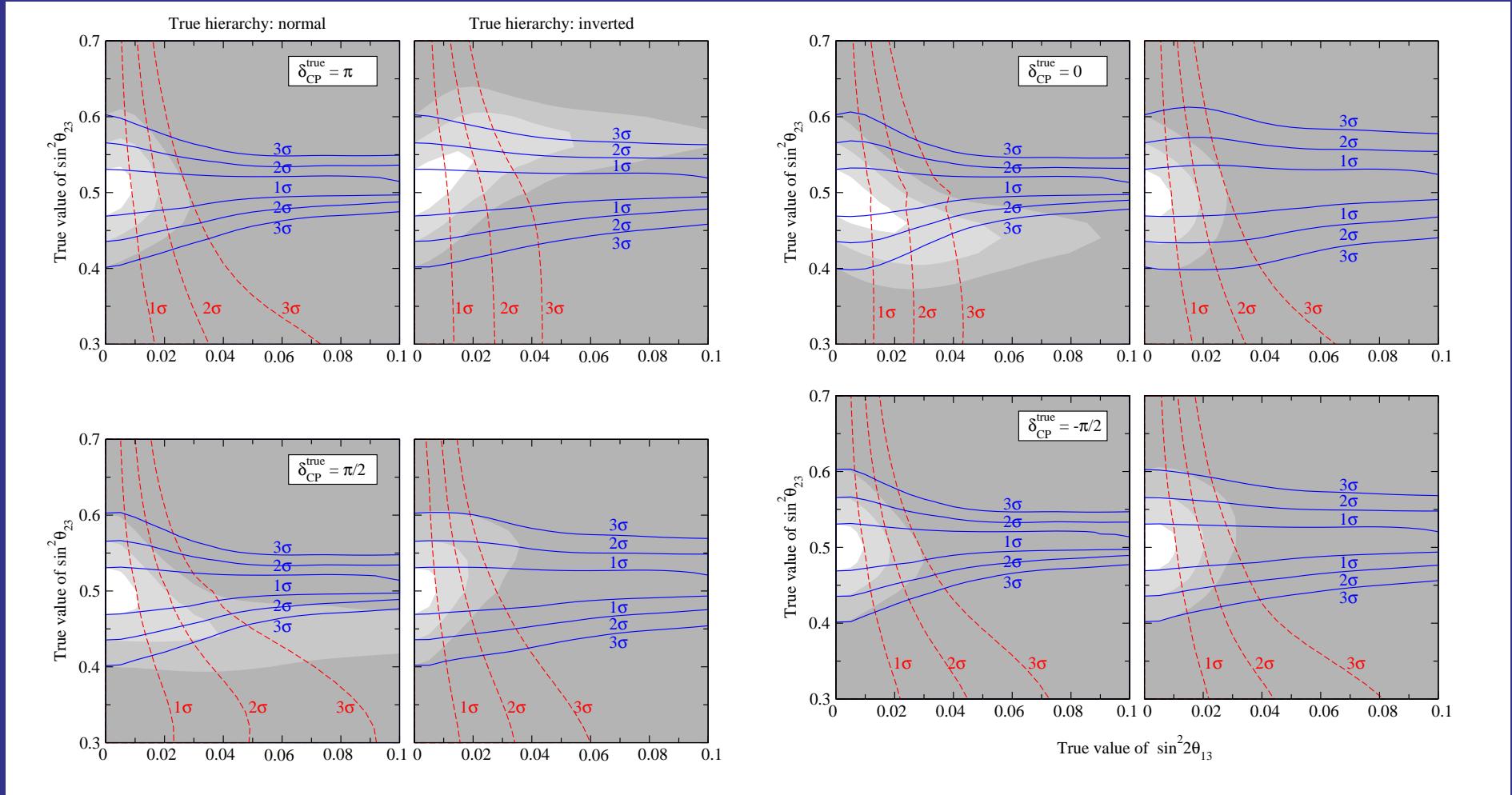
True values:

$$\sin^2 2\theta_{13} = 0.03, \delta_{\text{CP}} = -0.85\pi, \Delta m_{31}^2 = 2.2 \times 10^{-3} \text{ eV}^2$$

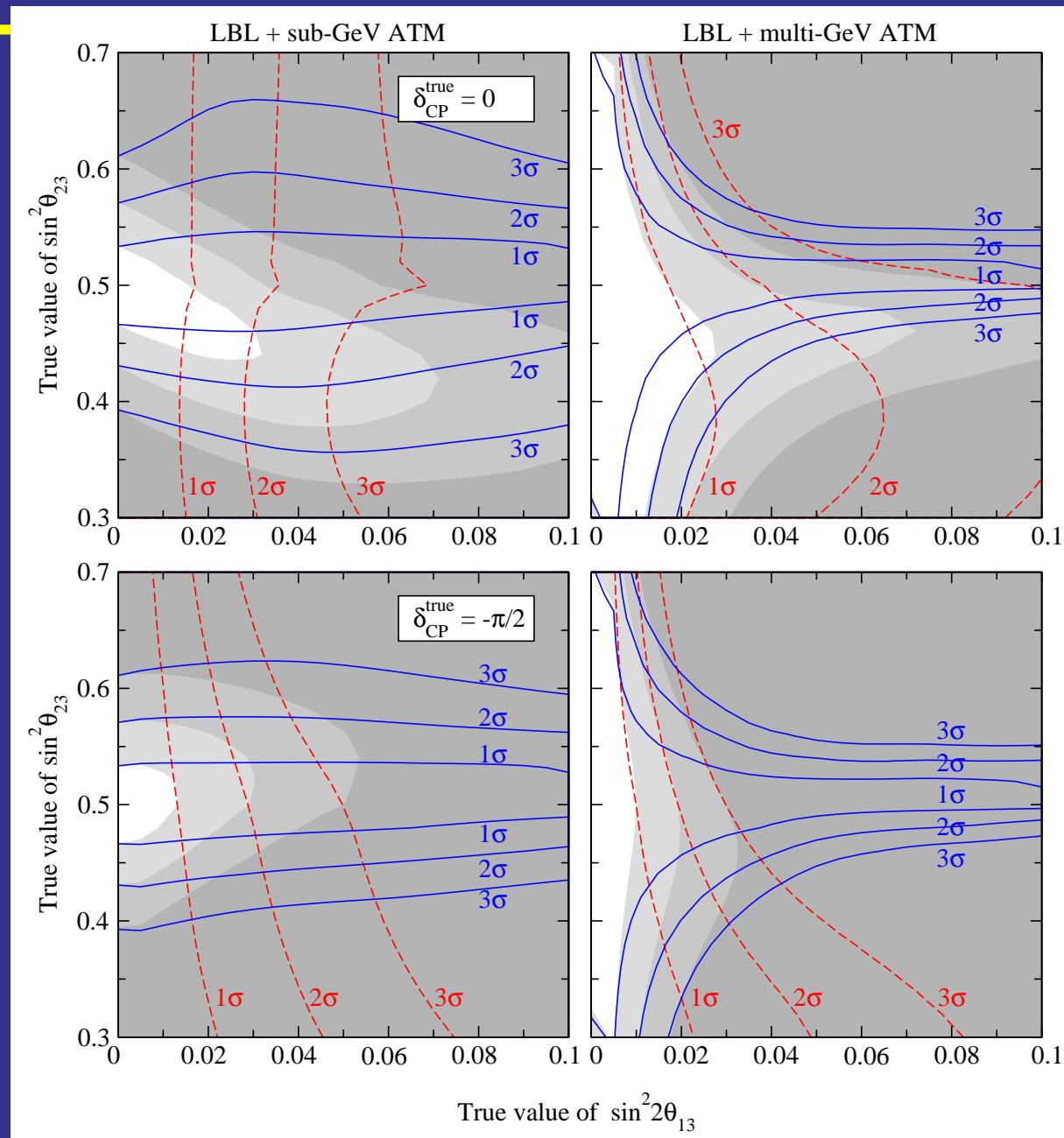
# *Resolving the degeneracies*



# Resolving the degeneracies



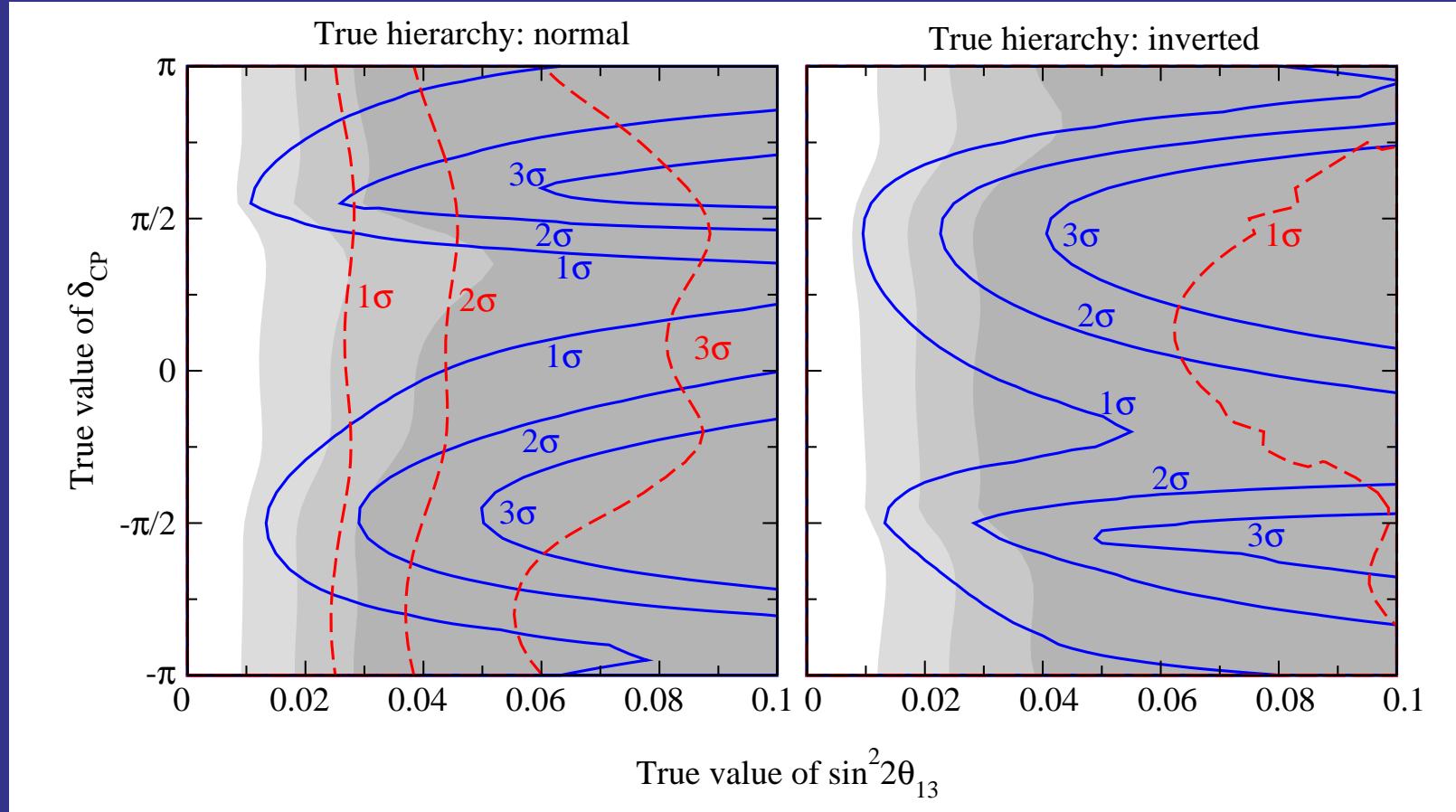
# Which are the relevant ATM data samples?



---

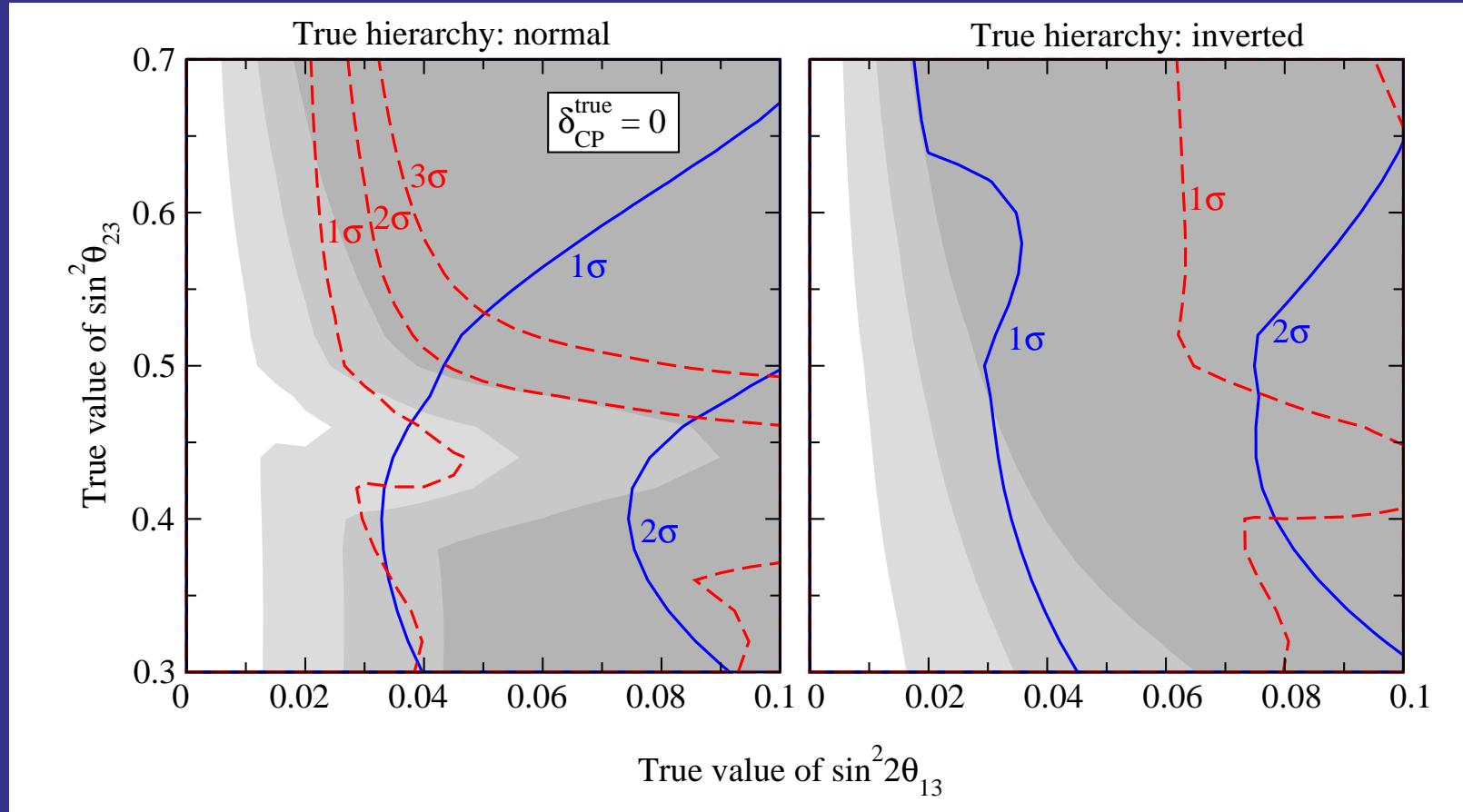
# **Identifying the mass hierarchy**

# *Identifying the mass hierarchy*



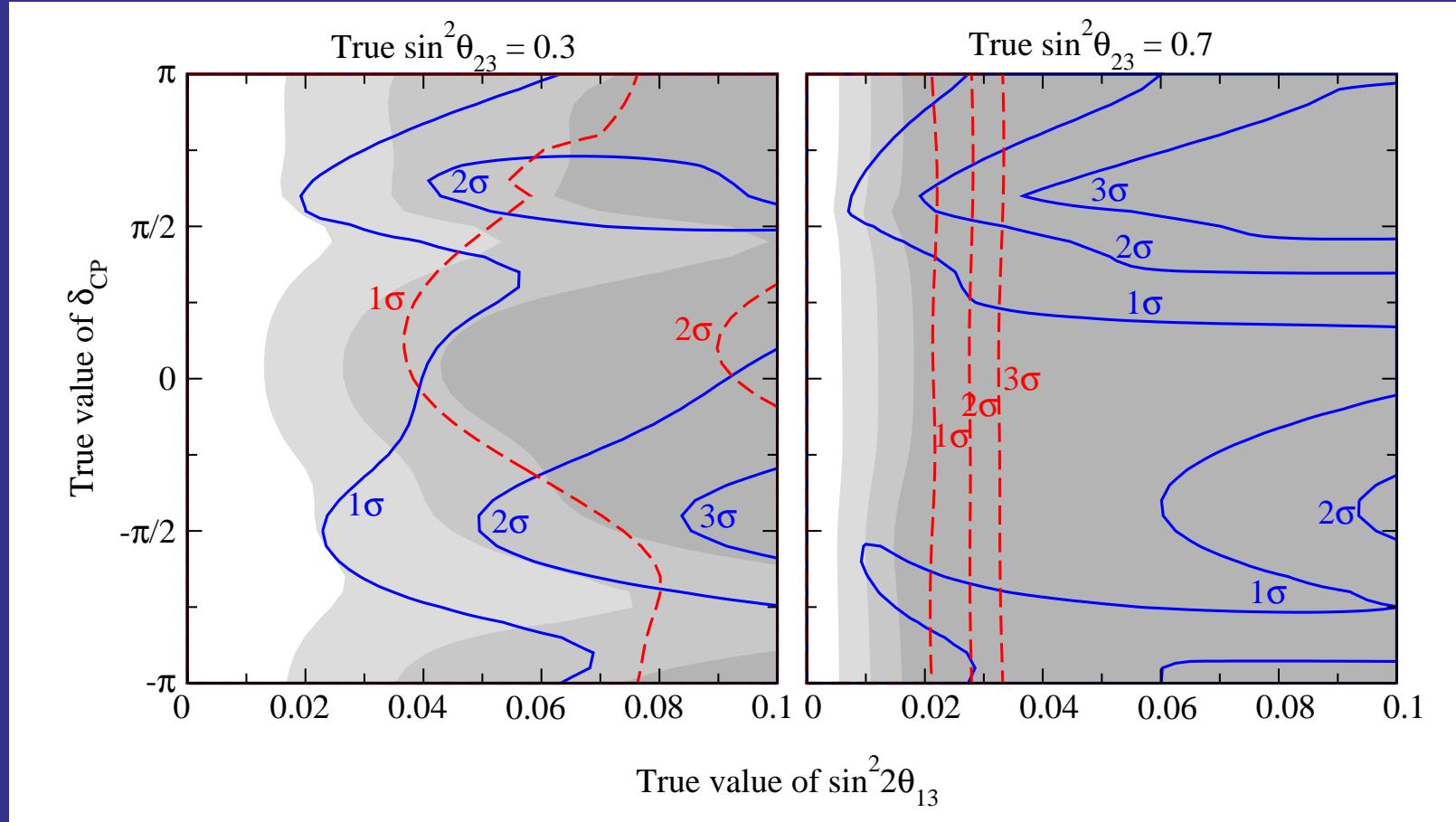
solid: LBL-only, dashed: ATM-only, shading: LBL+ATM

# *Identifying the mass hierarchy*



solid: LBL-only, dashed: ATM-only, shading: LBL+ATM

# *Identifying the mass hierarchy*



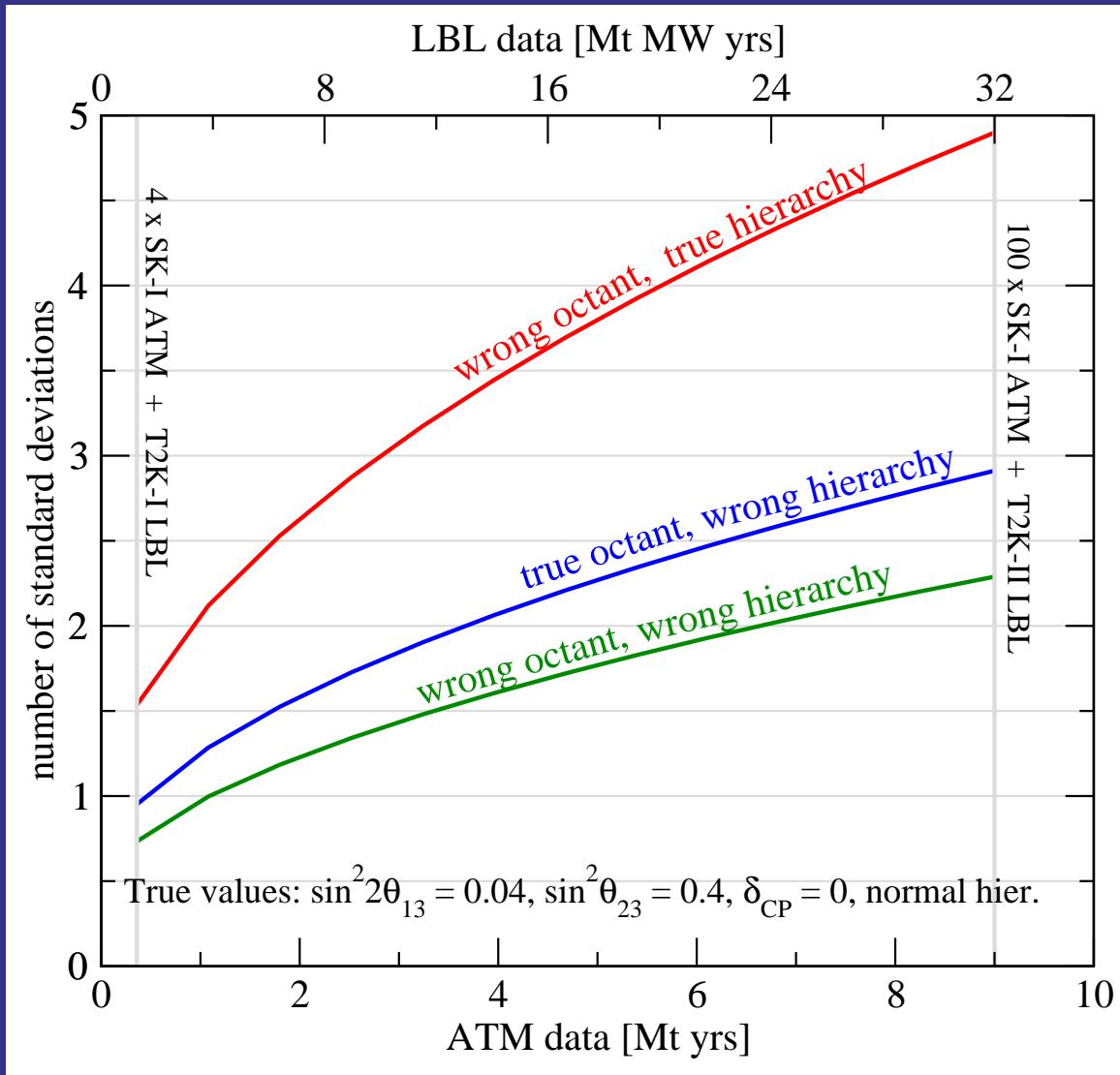
solid: LBL-only, dashed: ATM-only, shading: LBL+ATM

# *Luminosity scaling*

---

**Do we really need a Mt experiment?**

# Luminosity scaling



# *Preliminary BB/SPL analysis*

---

CERN-Frejus LBL experiments **(PRELIMINARY)**

simulation from Huber, Lindner, Rolinec, Winter, work in progress

# *Preliminary BB/SPL analysis*

---

## CERN-Frejus LBL experiments **(PRELIMINARY)**

simulation from Huber, Lindner, Rolinec, Winter, work in progress

- **Beta Beam**

similar to the setups from Bouchez, Lindros, Mezzetto, hep-ex/0310059;  
Burguet-Castell et al., hep-ph/0312068; Donini et al., hep-ph/0406132

$\bar{\nu}$ :  ${}^6\text{He}$  ( $\gamma = 60, 3 \times 10^{18}$  decays/yr),

$\nu$ :  ${}^{18}\text{Ne}$  ( $\gamma = 100, 1 \times 10^{18}$  decays/yr),

10 yrs running

# Preliminary BB/SPL analysis

---

## CERN-Frejus LBL experiments (PRELIMINARY)

simulation from Huber, Lindner, Rolinec, Winter, work in progress

- **Beta Beam**

similar to the setups from Bouchez, Lindros, Mezzetto, hep-ex/0310059;  
Burguet-Castell et al., hep-ph/0312068; Donini et al., hep-ph/0406132

$\bar{\nu}$ :  ${}^6\text{He}$  ( $\gamma = 60, 3 \times 10^{18}$  decays/yr),

$\nu$ :  ${}^{18}\text{Ne}$  ( $\gamma = 100, 1 \times 10^{18}$  decays/yr),

10 yrs running

- **SPL Superbeam**

similar to SB from Gomes-Cadenas et al., hep-ex/0105297; Donini et al., hep-ph/0406132

2.2 GeV proton beam from 4 MW SPL, 2 yrs  $\nu$ , 8 yrs  $\bar{\nu}$

# Preliminary BB/SPL analysis

---

## CERN-Frejus LBL experiments (PRELIMINARY)

simulation from Huber, Lindner, Rolinec, Winter, work in progress

- **Beta Beam**

similar to the setups from Bouchez, Lindros, Mezzetto, hep-ex/0310059;  
Burguet-Castell et al., hep-ph/0312068; Donini et al., hep-ph/0406132

$\bar{\nu}$ :  ${}^6\text{He}$  ( $\gamma = 60, 3 \times 10^{18}$  decays/yr),

$\nu$ :  ${}^{18}\text{Ne}$  ( $\gamma = 100, 1 \times 10^{18}$  decays/yr),

10 yrs running

- **SPL Superbeam**

similar to SB from Gomes-Cadenas et al., hep-ex/0105297; Donini et al., hep-ph/0406132

2.2 GeV proton beam from 4 MW SPL, 2 yrs  $\nu$ , 8 yrs  $\bar{\nu}$

- **450 kt water Cherenkov detector at Frejus**

# *Preliminary BB/SPL analysis*

---

main difference to T2K:

- baseline: 130 km
- $E_\nu \simeq 0.2 - 0.3$  GeV
- no spectral information available

# *Preliminary BB/SPL analysis*

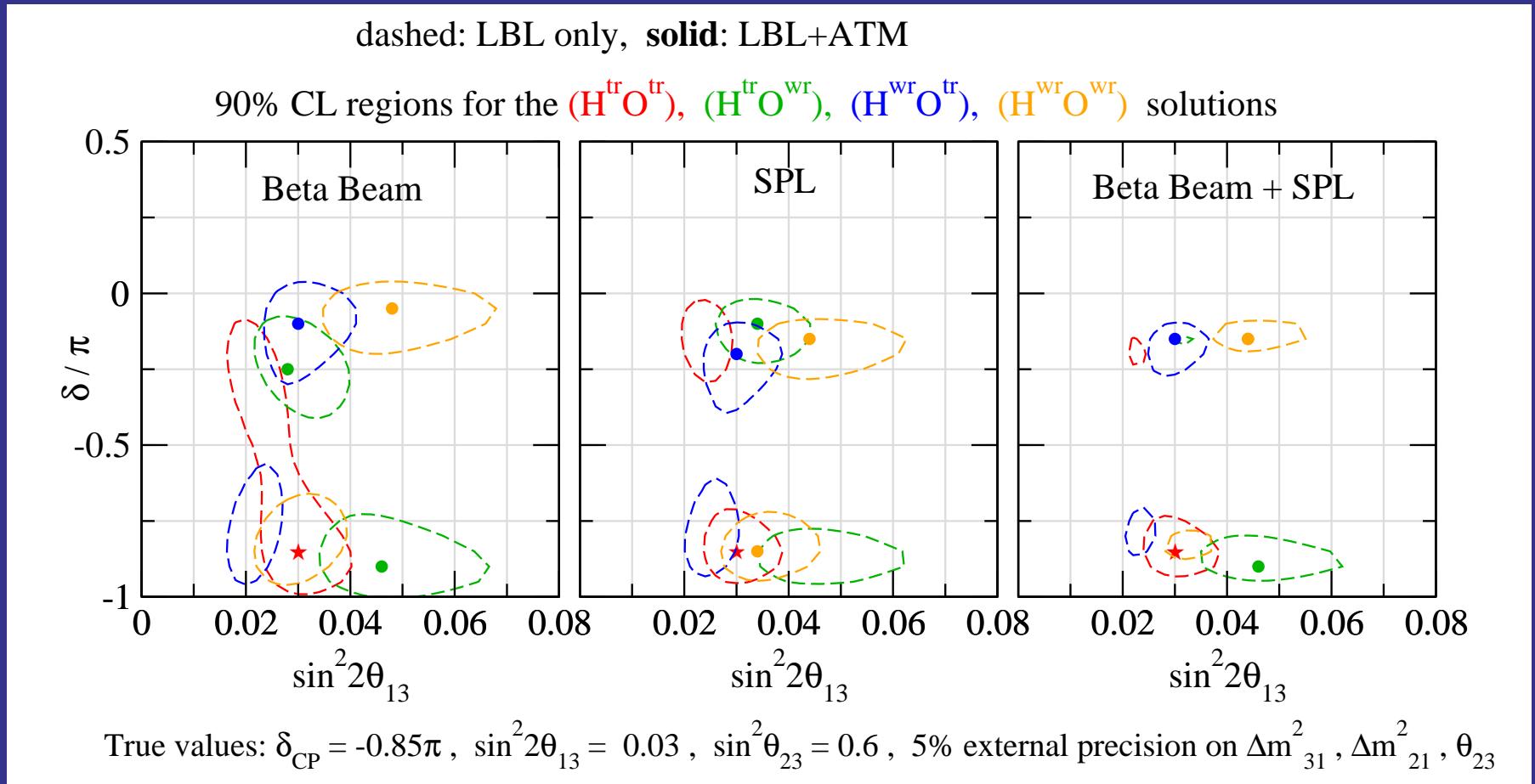
---

main difference to T2K:

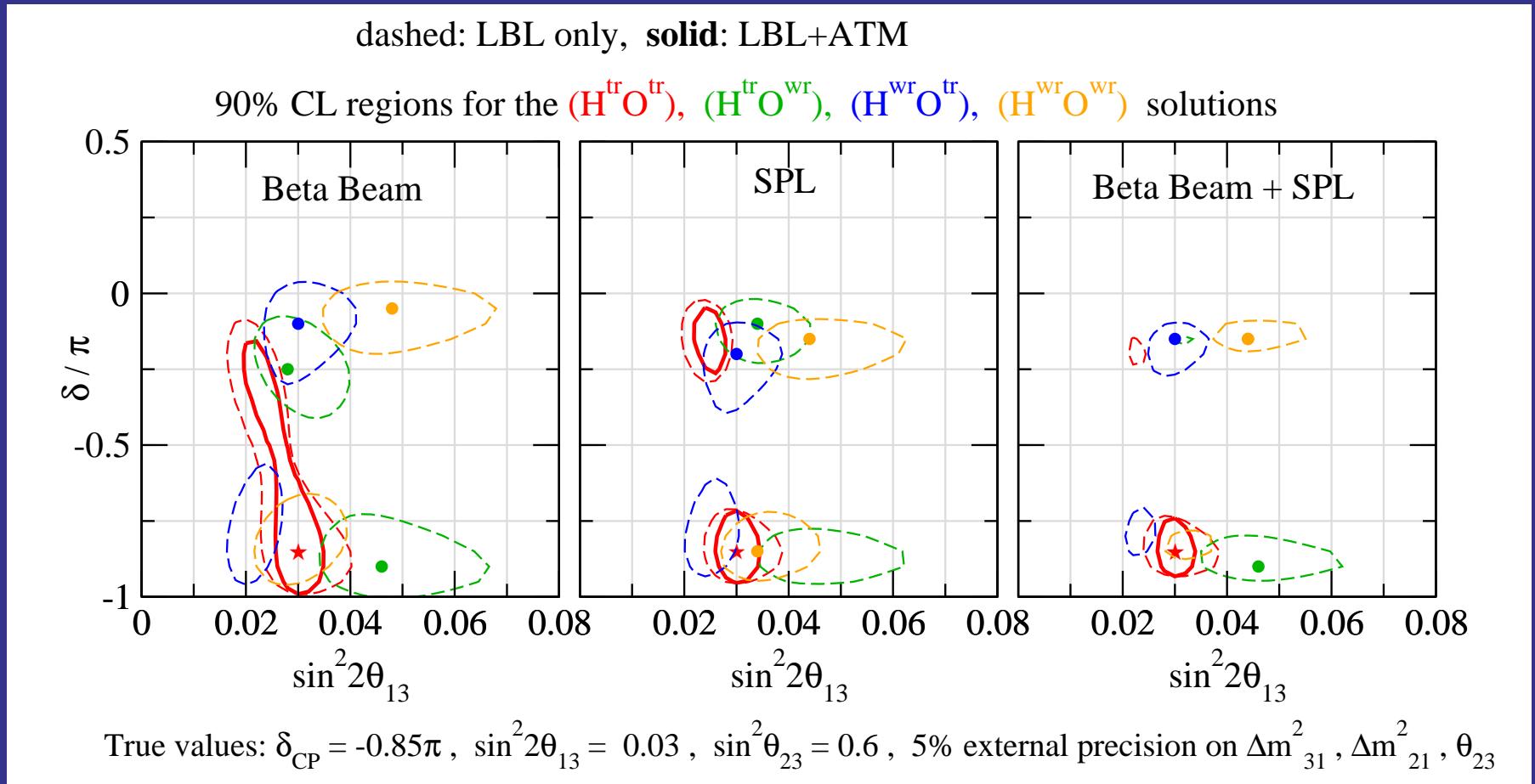
- baseline: 130 km
- $E_\nu \simeq 0.2 - 0.3$  GeV
- no spectral information available

$(\theta_{13}, \delta_{\text{CP}})$ -degeneracy cannot be resolved

# Preliminary BB/SPL analysis



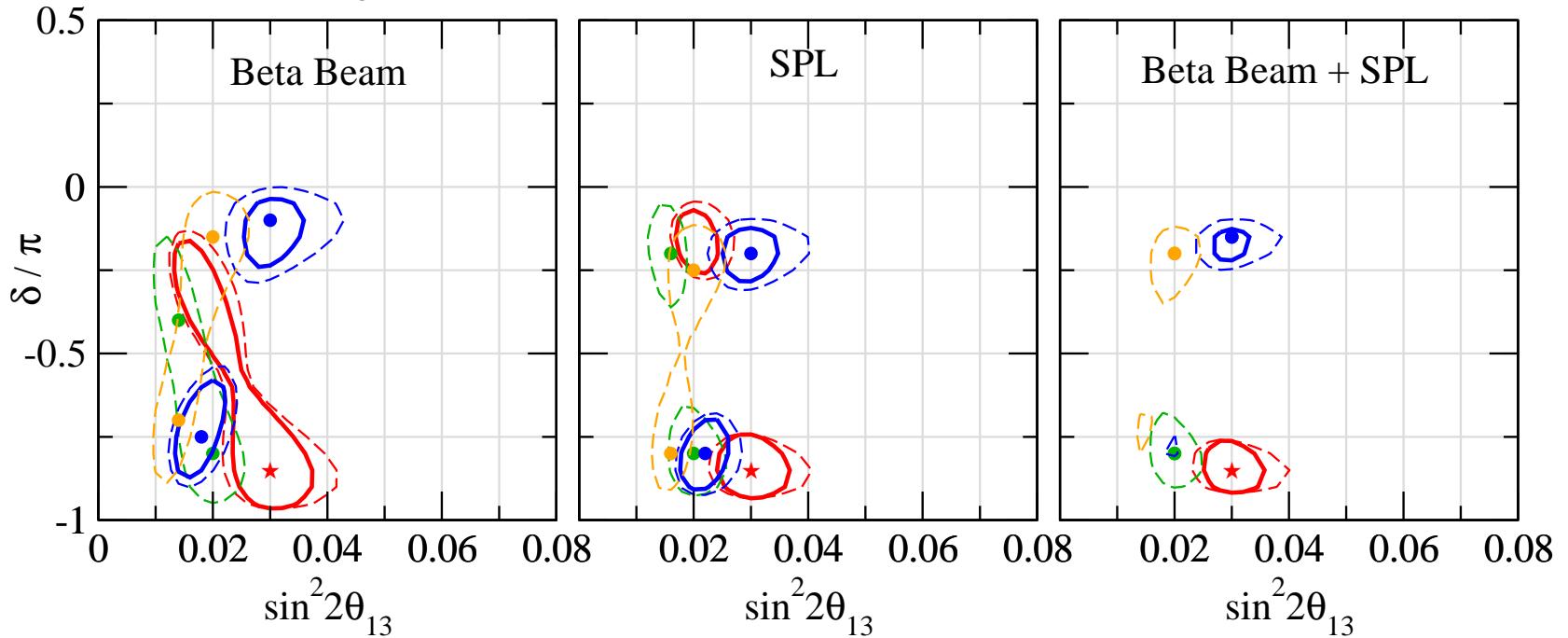
# Preliminary BB/SPL analysis



# Preliminary BB/SPL analysis

dashed: LBL only, solid: LBL+ATM

90% CL regions for the  $(H^{tr}O^{tr})$ ,  $(H^{tr}O^{wr})$ ,  $(H^{wr}O^{tr})$ ,  $(H^{wr}O^{wr})$  solutions



True values:  $\delta_{CP} = -0.85\pi$ ,  $\sin^2 2\theta_{13} = 0.03$ ,  $\sin^2 \theta_{23} = 0.4$ , 5% external precision on  $\Delta m^2_{31}$ ,  $\Delta m^2_{21}$ ,  $\theta_{23}$

---

# **Concluding remarks**

# *Concluding remarks*

---

Combined analysis of LBL and ATM data provides an interesting method to resolve degeneracies

# *Concluding remarks*

---

Combined analysis of LBL and ATM data provides an interesting method to resolve degeneracies

- sensitivity to the neutrino mass ordering significantly increased

# *Concluding remarks*

---

Combined analysis of LBL and ATM data provides an interesting method to resolve degeneracies

- sensitivity to the neutrino mass ordering significantly increased
- good sensitivity to the octant of  $\theta_{23}$

# *Concluding remarks*

---

Combined analysis of LBL and ATM data provides an interesting method to resolve degeneracies

- sensitivity to the neutrino mass ordering significantly increased
- good sensitivity to the octant of  $\theta_{23}$
- ambiguities in the determination of  $\sin^2 2\theta_{13}$  and  $\delta_{CP}$  can be resolved

# *Concluding remarks*

---

Combined analysis of LBL and ATM data provides an interesting method to resolve degeneracies

- sensitivity to the neutrino mass ordering significantly increased
- good sensitivity to the octant of  $\theta_{23}$
- ambiguities in the determination of  $\sin^2 2\theta_{13}$  and  $\delta_{CP}$  can be resolved

given the Mt detector for the LBL experiment,  
**ATM data come for free!**

# *Concluding remarks*

---

Complementarity of LBL and ATM data:

# *Concluding remarks*

---

Complementarity of LBL and ATM data:

- Three-flavour effects in ATM data provide sensitivity to mass ordering and octant of  $\theta_{23}$

# *Concluding remarks*

---

Complementarity of LBL and ATM data:

- Three-flavour effects in ATM data provide sensitivity to mass ordering and octant of  $\theta_{23}$
- The determination of  $\Delta m_{31}^2$  and  $\sin^2 2\theta_{23}$  at the sub-percent level and a constraint on  $\sin^2 2\theta_{13}$  from LBL data is necessary

# *Concluding remarks*

---

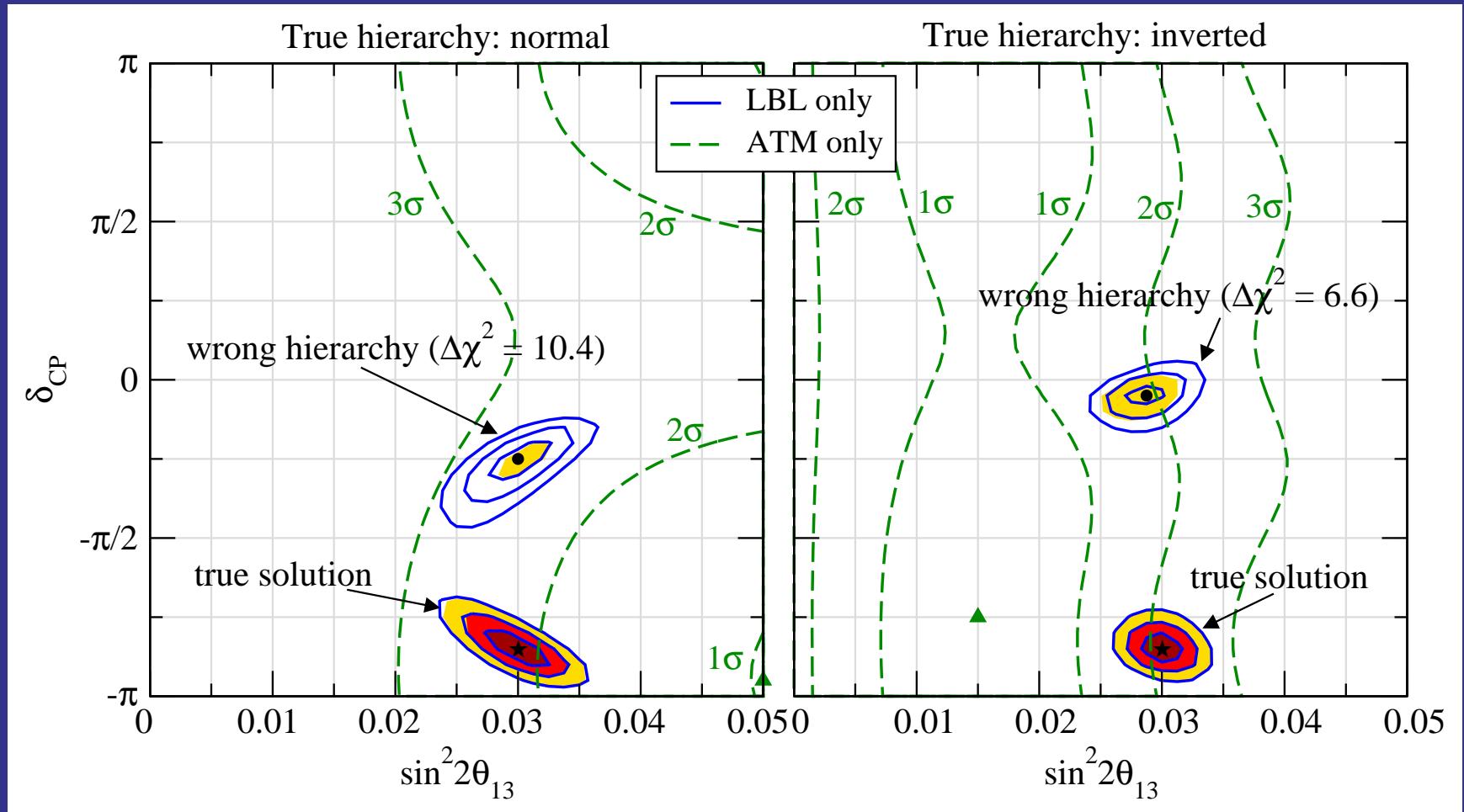
Complementarity of LBL and ATM data:

- Three-flavour effects in ATM data provide sensitivity to mass ordering and octant of  $\theta_{23}$
- The determination of  $\Delta m_{31}^2$  and  $\sin^2 2\theta_{23}$  at the sub-percent level and a constraint on  $\sin^2 2\theta_{13}$  from LBL data is necessary

**Thank you for your attention!**

P.Huber, M.Maltoni, TS, hep-ph/0501037

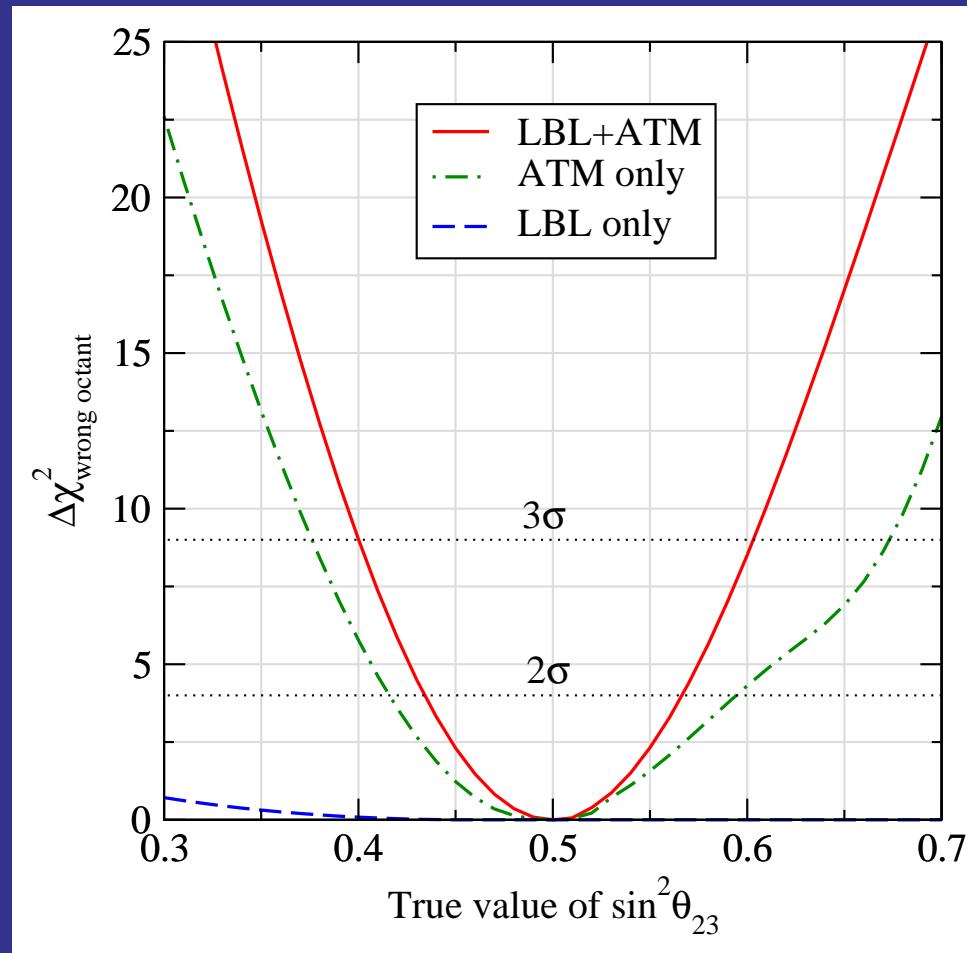
# Additional slides



*True*  $\theta_{13} = 0$

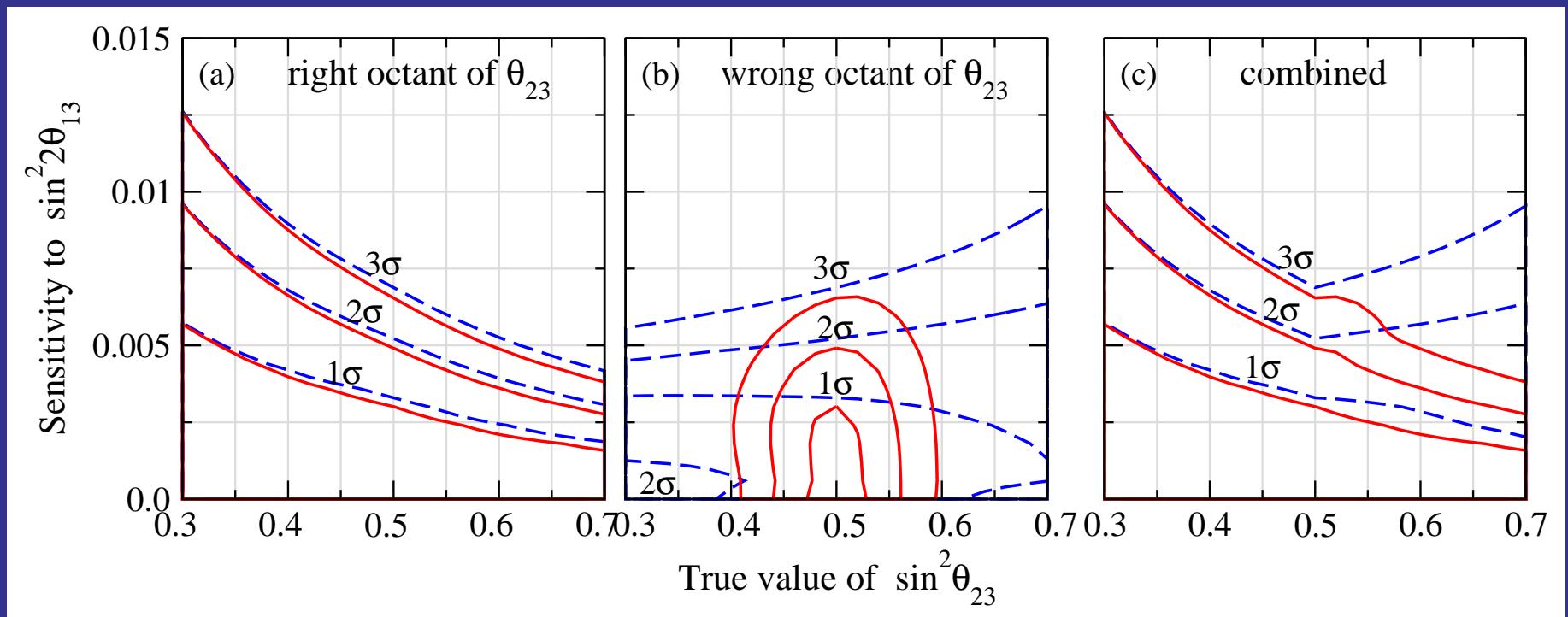
---

## Resolving the octant-degeneracy:



*True*  $\theta_{13} = 0$

The limit on  $\sin^2 2\theta_{13}$ :



$$P_{\mu e} \simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \Delta_{31} + \dots$$