

# *Neutrino mixing at high energy neutrino telescopes*

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*MPL - Munich*

*CARE '05 - ECFA/BENE*

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$$\Delta x \Delta p_x \geq \hbar$$

Theoretical Physics Division

# Overview of the Talk

- *Neutrino telescopes: an overview*
- *Neutrino mixing at neutrino telescopes*
- *“Galactic  $\beta$ -beams” and muon-damped sources*
- *Conclusions*

# *Neutrino-telescopes: an overview*

# High-Energy $\nu$ astronomy: a new sky

## Neutrinos: a powerful tool for high energy astrophysics

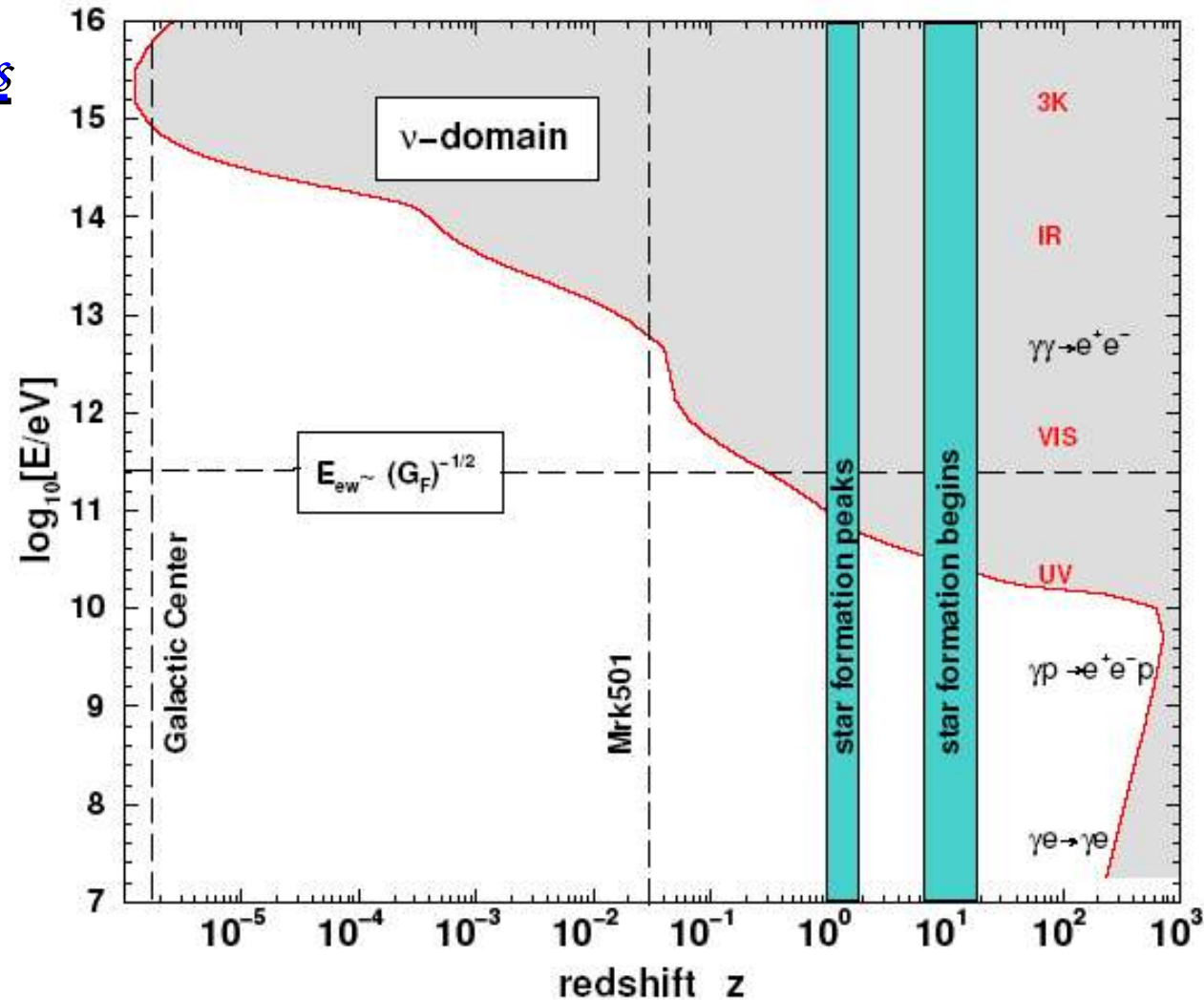
+ ) Directional signal  
(differently from CR)

+ ) No absorption  
(differently from  $\gamma$ )

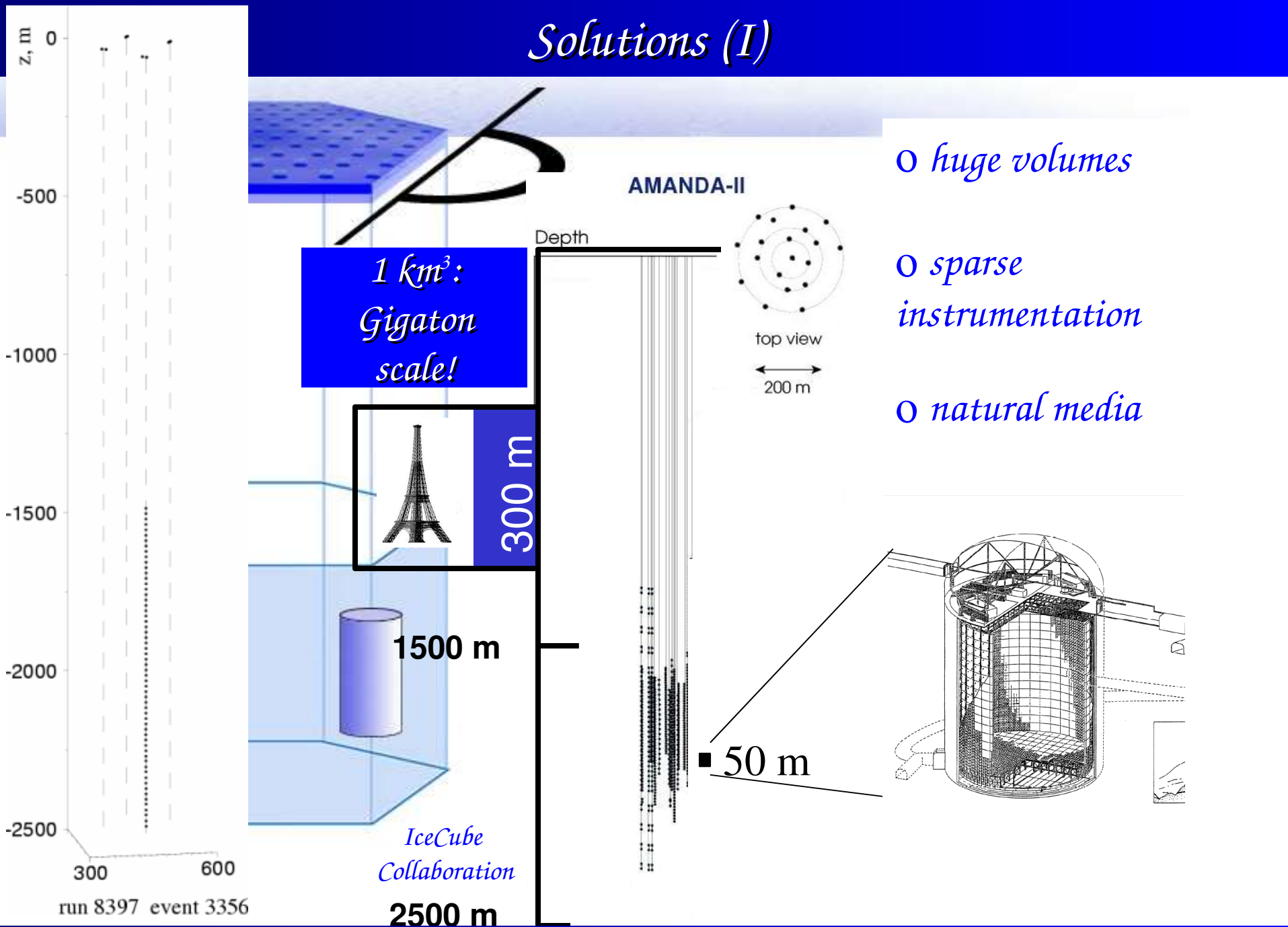
+ ) HEV guaranteed  
(HECR & HE $\gamma$  observed)

Main problem

- ) Small  $\sigma$



# Solutions (I)



# Status of Optical Cherenkov Telescopes

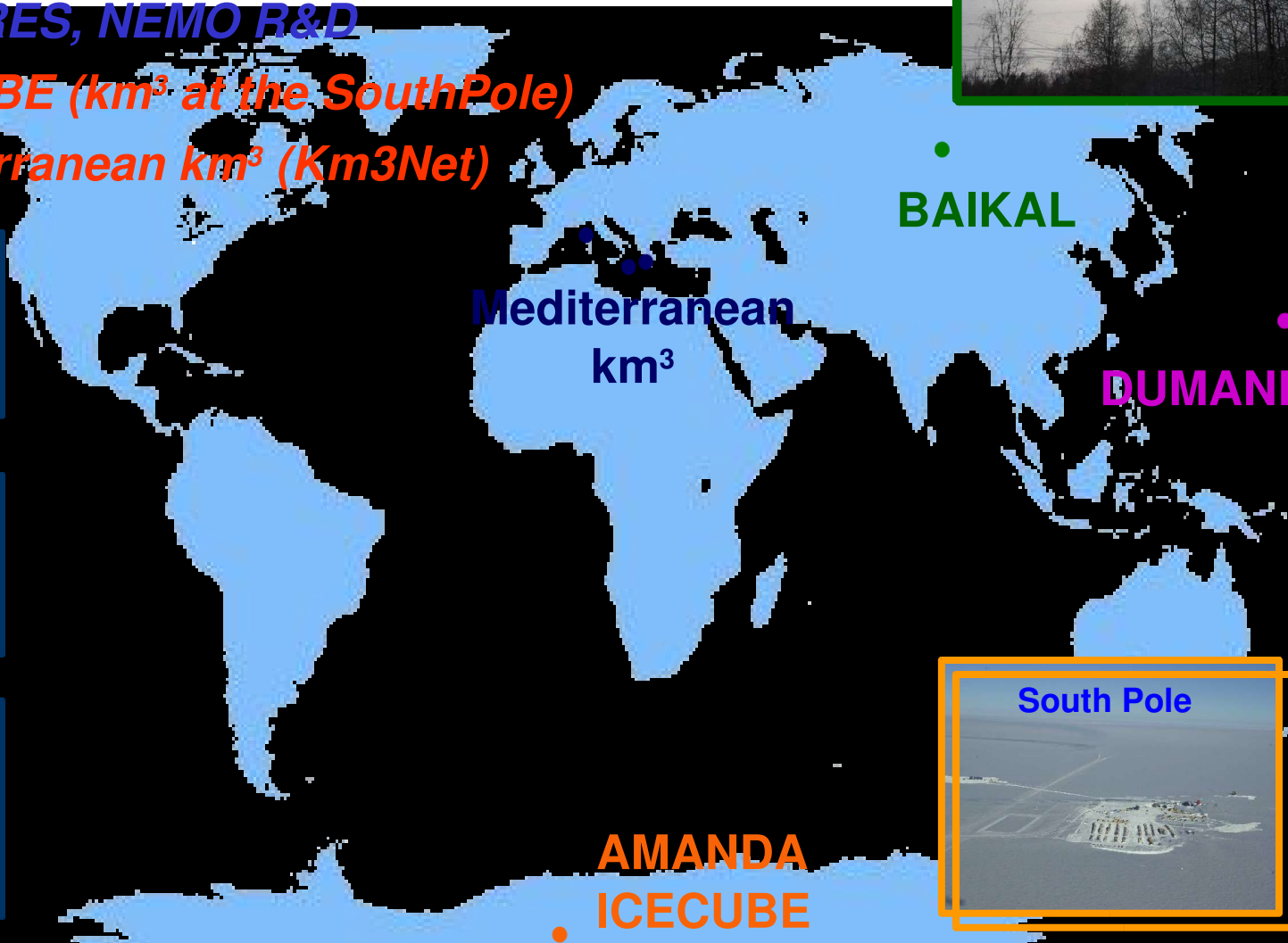
80's: DUMAND R&D

90's: BAIKAL, AMANDA, NESTOR

2k's: ANTARES, NEMO R&D

<2010: ICECUBE (km<sup>3</sup> at the South Pole)

.....? Mediterranean km<sup>3</sup> (Km3Net)



# Flavour discrimination (I)

**1<sup>st</sup> detection channel:  $O(\text{km}) \mu$  tracks**

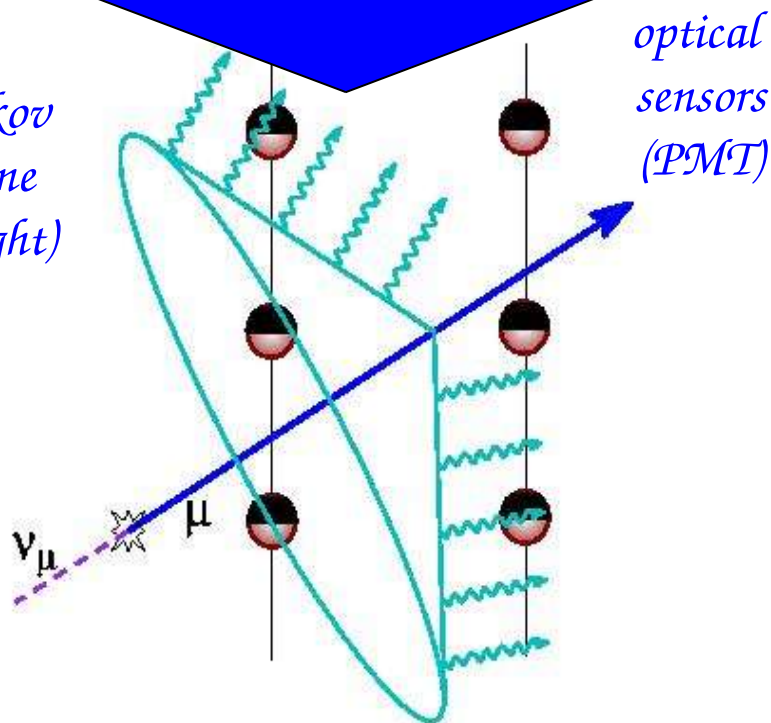
directional error:  $\sim 1^\circ$

$\sigma [\log_{10}(E/\text{TeV})] : \sim 0.3$

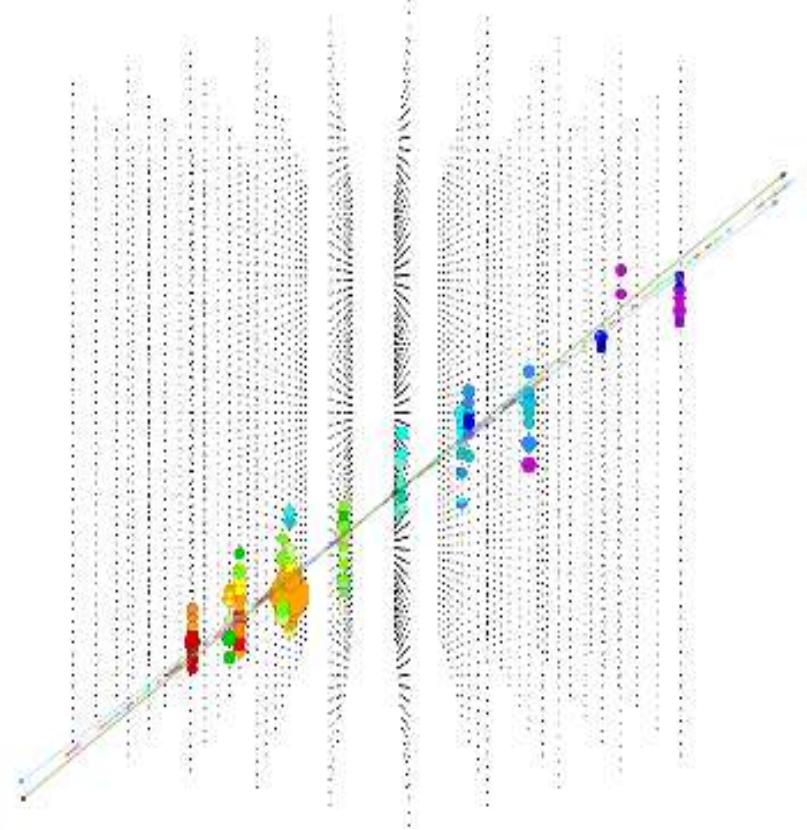
coverage:  $2\pi$

energy range:  $\sim 50 \text{ GeV}$  to  $100 \text{ PeV}$

Cherenkov  
light cone  
(blue light)



$\nu_\mu + N \rightarrow \mu + X$  (DIS)





# Flavour discrimination (II)

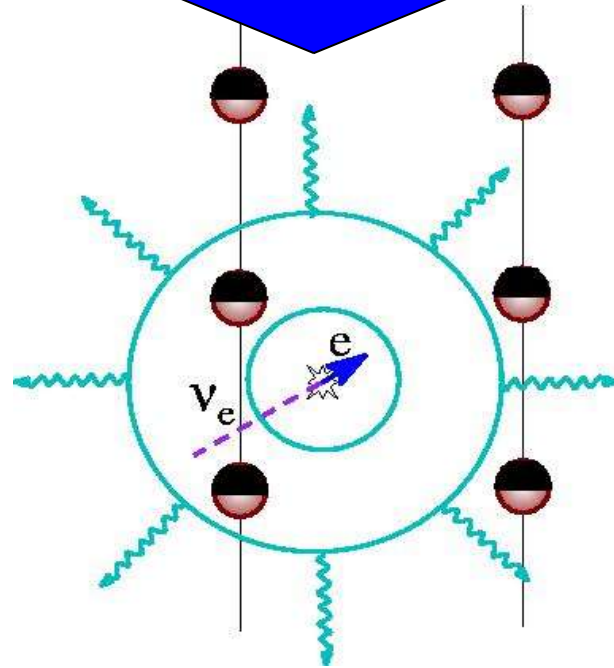
**2<sup>nd</sup> detection channel:  
cascades from  $\nu_e$  &  $\nu_\tau$  CC + all flavors NC**

directional error:  $\sim 10\text{-}40^\circ$

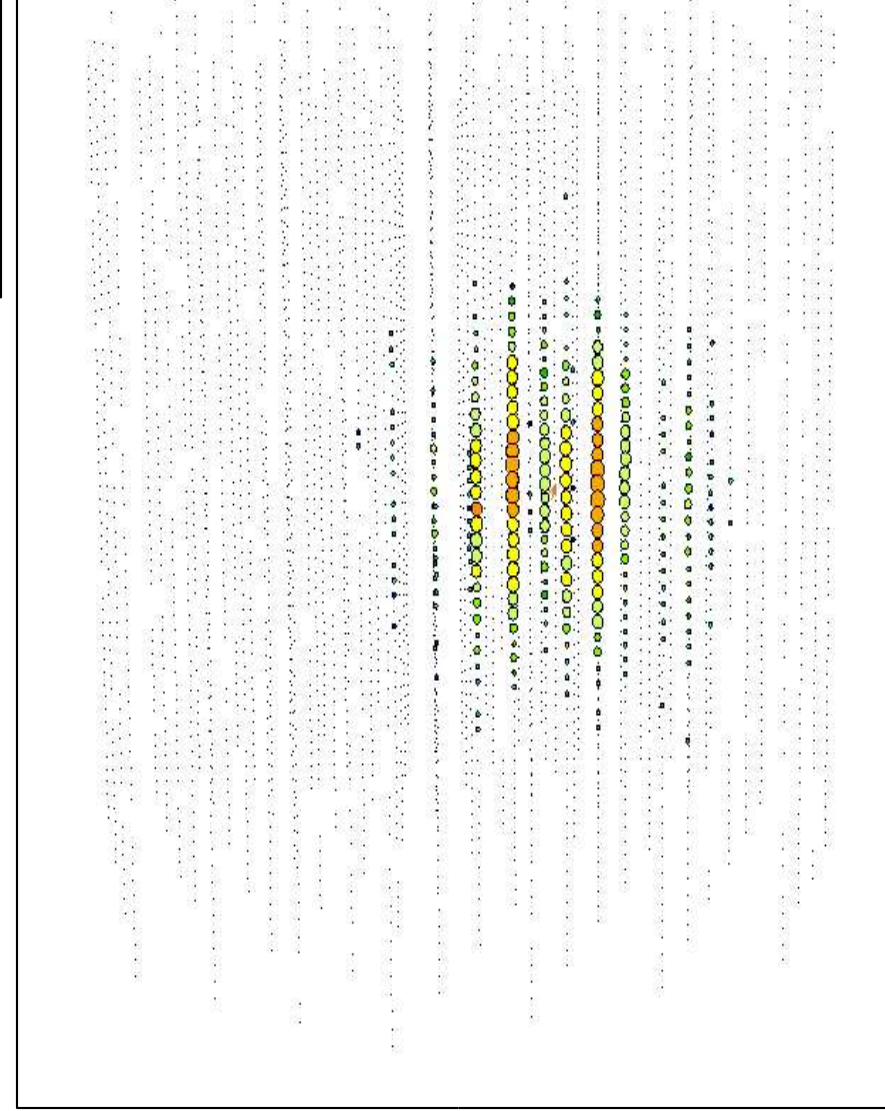
$\sigma [\log_{10}(E/\text{TeV})] : \sim 0.1$

coverage:  $4\pi$

energy range:  $\sim 1 \text{ TeV to } 100 \text{ PeV}$



**$\nu_e + N \rightarrow e + X$  (DIS)**





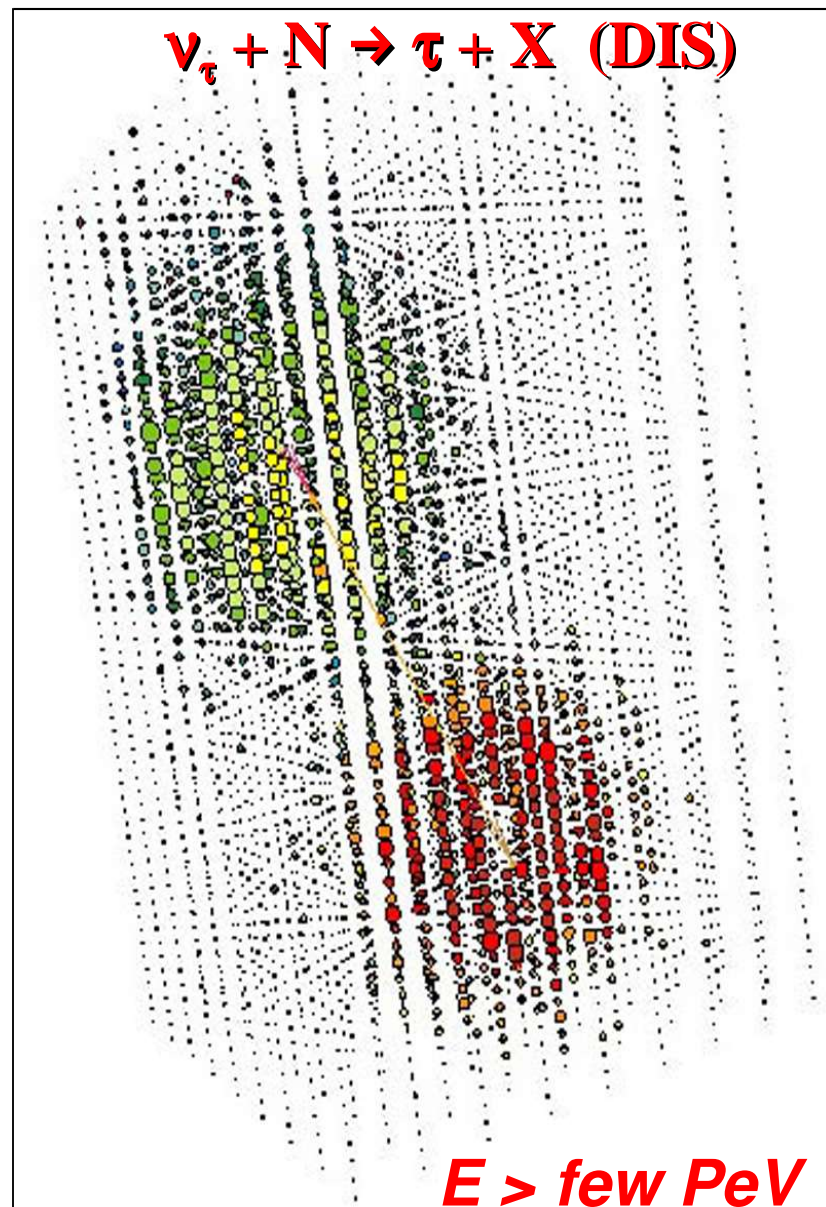
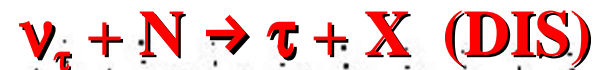
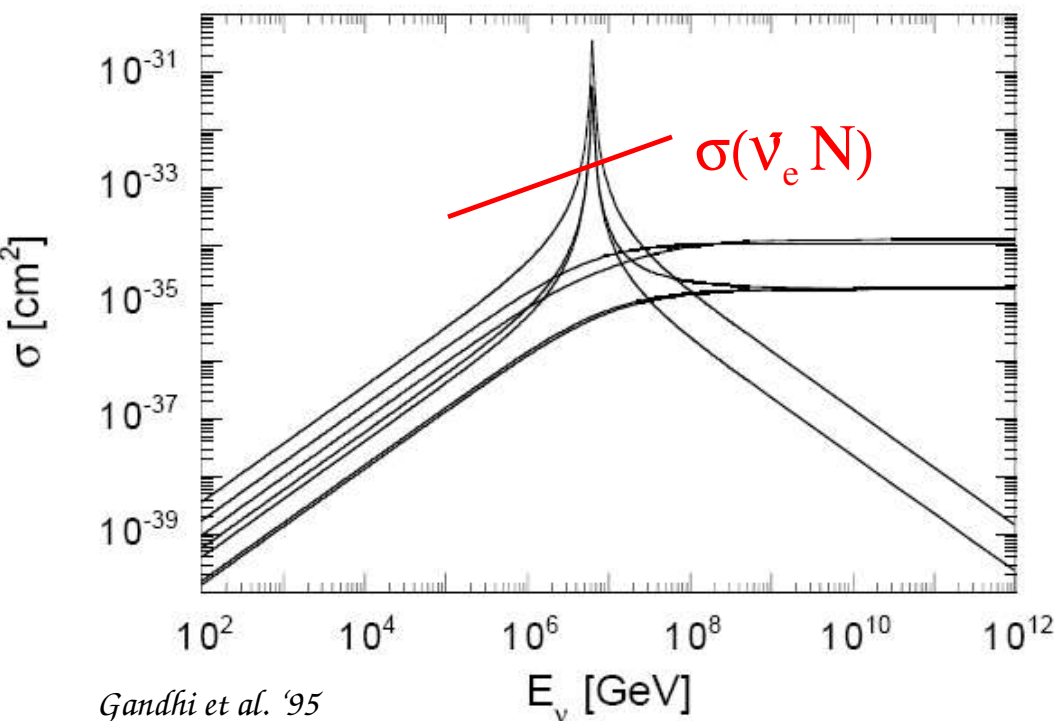
# Flavour discrimination (III)

"Glashow Resonance"



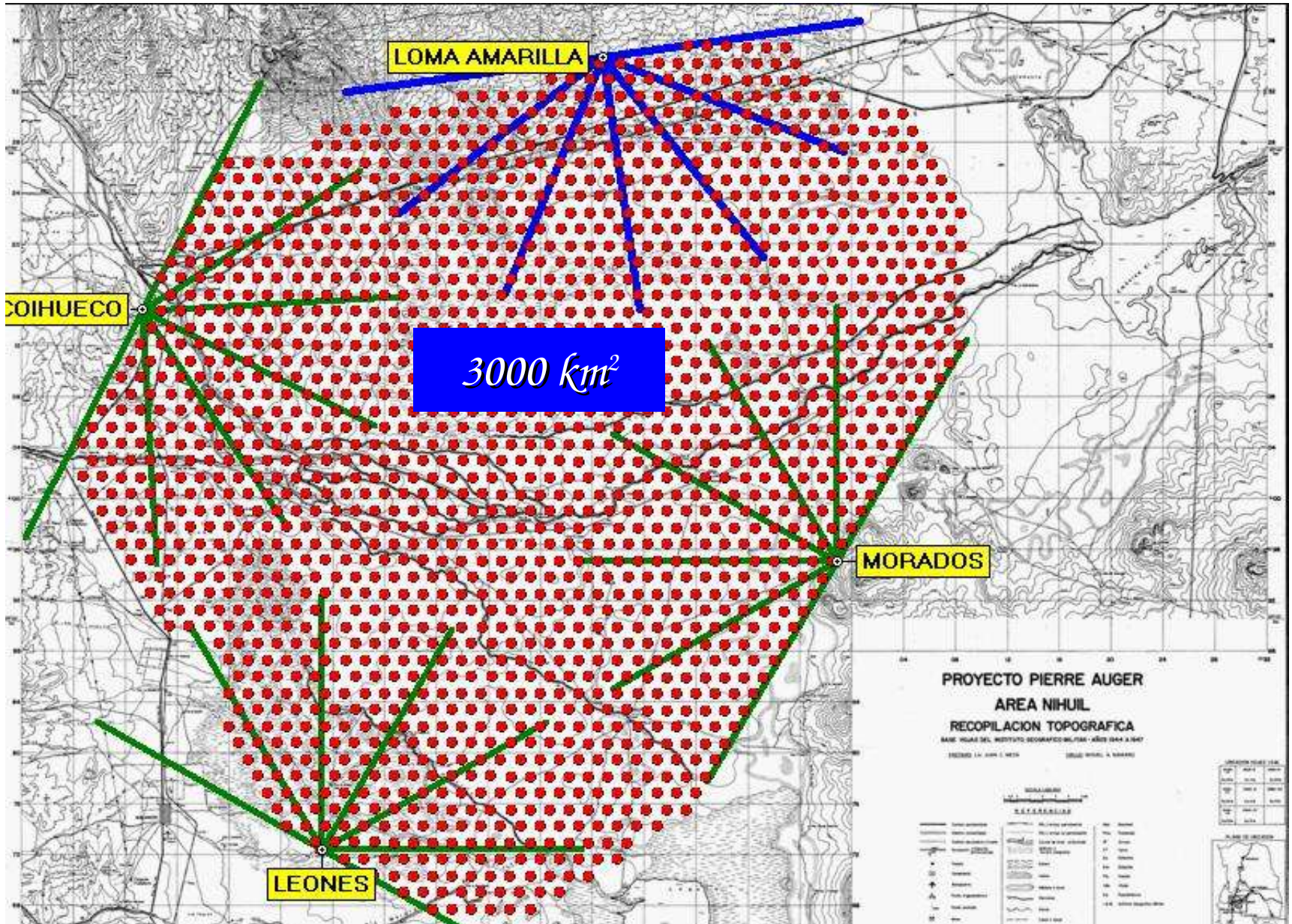
Unique to  $\nu_e$

$\sigma$  enhanced at  $E \approx 6.3 \text{ PeV}$

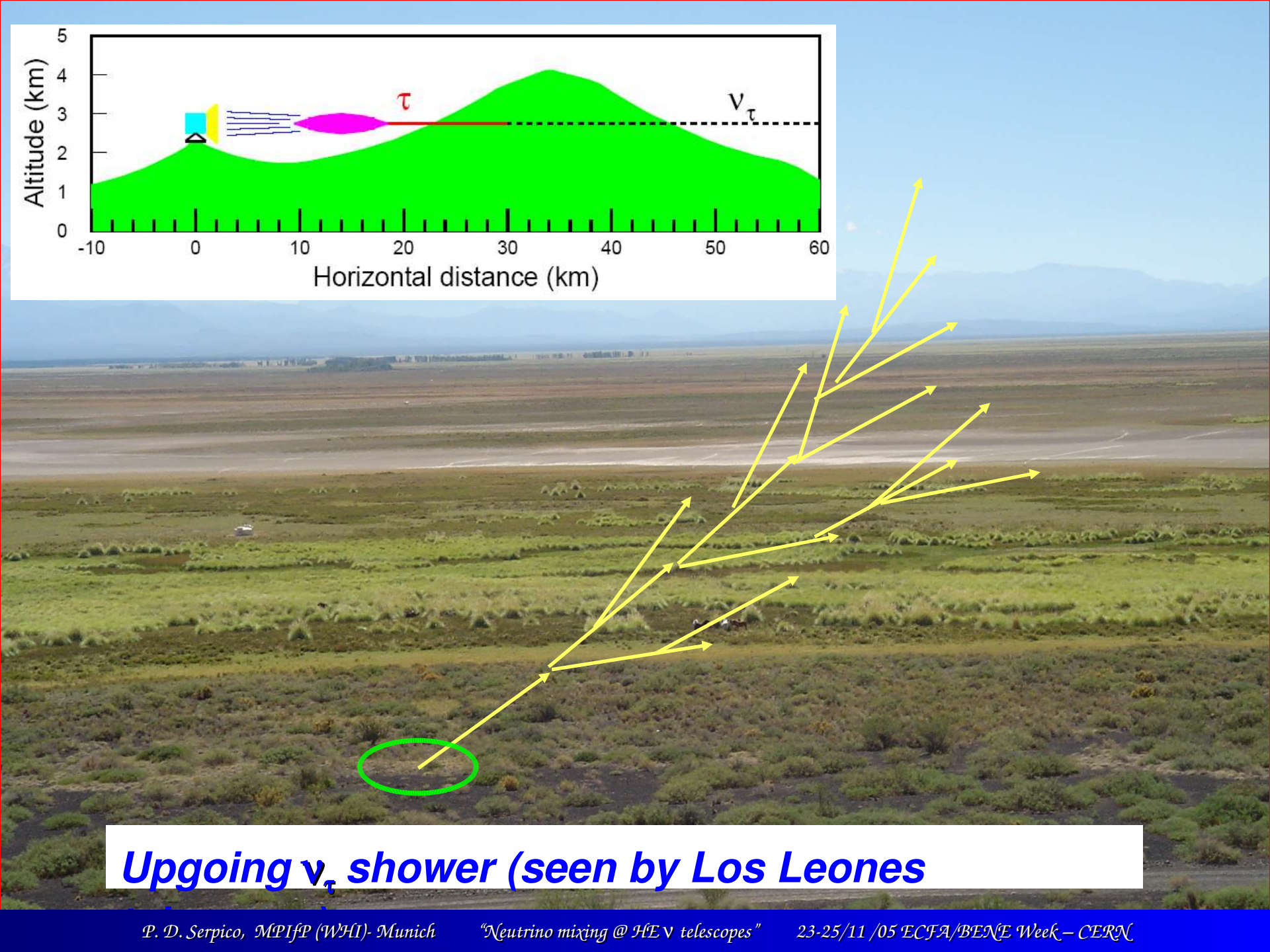
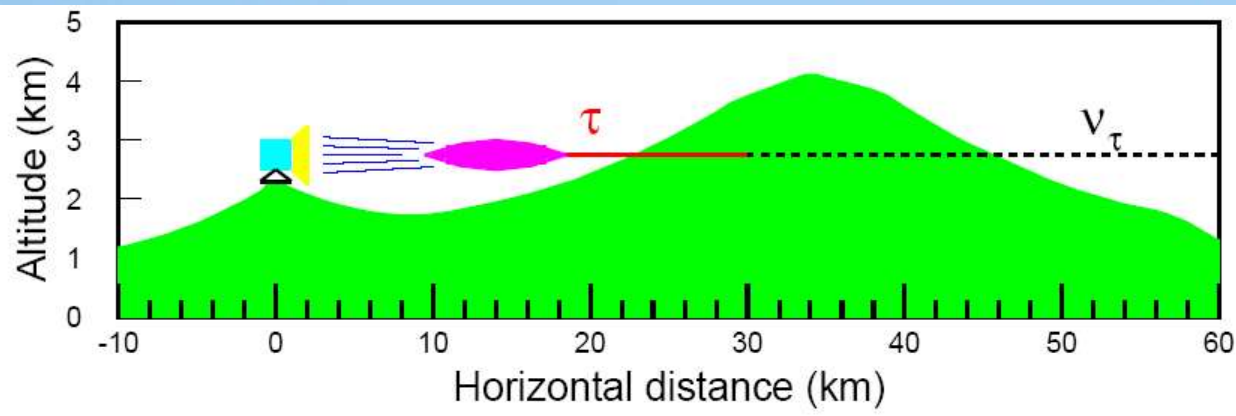




# Solutions (II)





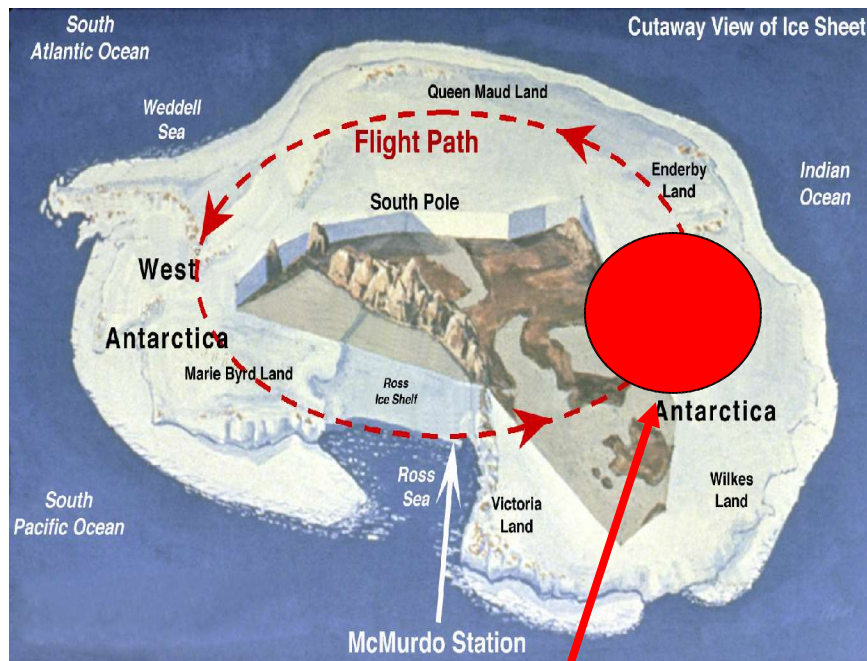


**Upgoing  $\nu_\tau$  shower (seen by Los Leones)**

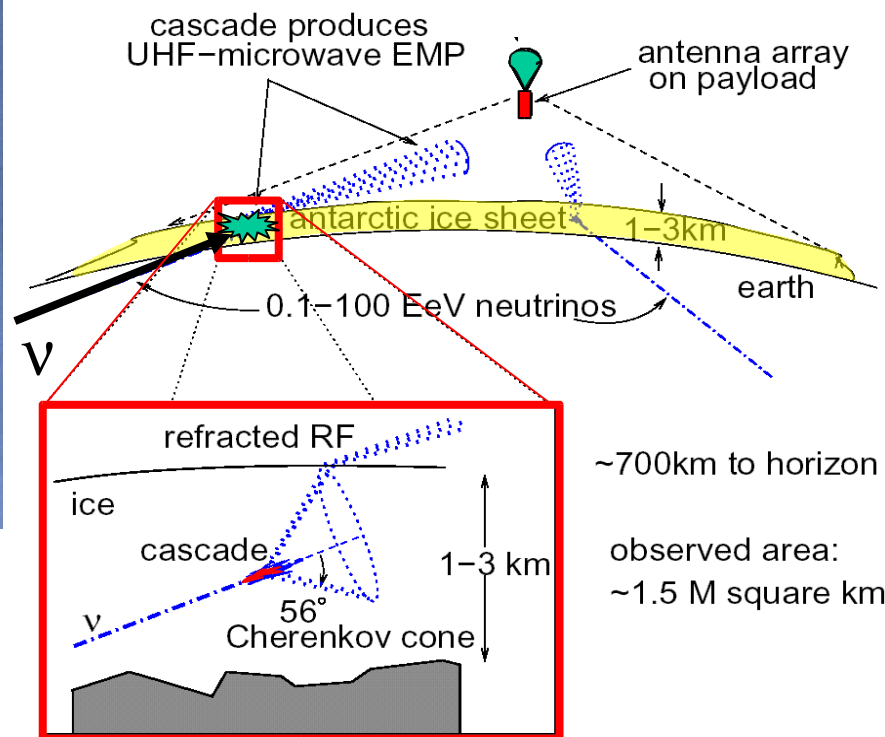
# Solutions (III)



## ANtarctic Impulsive Transient Antenna



600 km radius,  
1.1 million km<sup>2</sup>



*V-mixing at V-telescopes*

# $\nu$ -telescopes and $\nu$ -mixing

*Astrophysical  $\nu$  fluxes come from*

$$pp \rightarrow \pi X$$

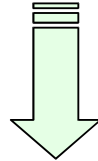
$$p\gamma \rightarrow \pi X$$

*flavour ratios at source  $\rightarrow \phi_e : \phi_\mu : \phi_\tau \approx 1/3 : 2/3 : 0$*

*at Earth after oscillations  $\rightarrow \phi_e : \phi_\mu : \phi_\tau \approx 1/3 : 1/3 : 1/3$*

*quite insensitive to mixing parameters*

*$d_{\text{source}} \gg L_{\text{osc}} \rightarrow$  no sensitivity to  $\Delta m_{\text{sol}}^2, \Delta m_{\text{atm}}^2$*



*Standard Paradigm: Neutrino mixing studies  
hopeless at high energy neutrino telescopes*

*I shall try to argue that this is misleading!*

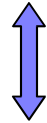


# $\nu$ -telescopes and $\nu$ -mixing

1. Standard oscillation phenomenology “rescues” signals, allowing some interesting measurements

1. Matter effects might imply observations sensitive to  $\Delta m^2$  's, e.g. to hierarchy

3. Input from  $\nu$ -mixing very important for diagnostics of astrophysical sources



4. “Peculiar” (but not “exotic”!) neutrino sources may exist sensitive to mixing parameters (including  $\theta_{13}$  and  $\delta_{CP}$ )

Only standard oscillation scenarios considered!

# A “rescued” signal: The Galactic diffuse $\nu_\tau$

*H. Athar et al. APP 18 (2003) 581*

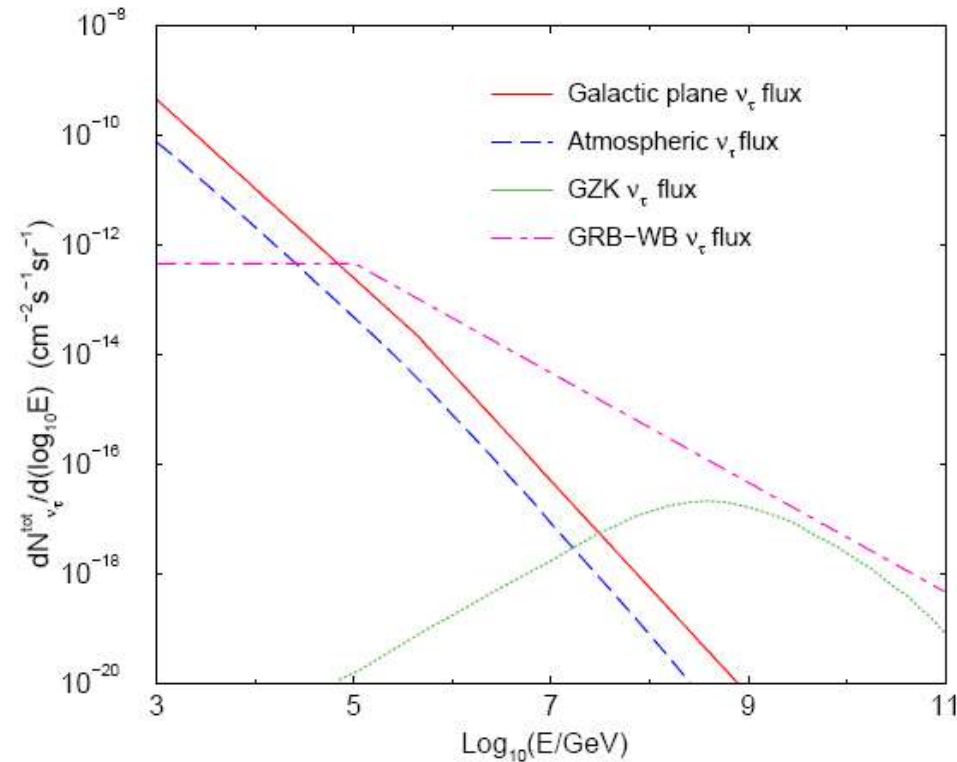
$\nu$ -flux from CR hitting Galactic matter develops a large  $\nu_\tau$ -component via oscillations.

Atmospheric  $\nu$  background is

○ softer (relevant energy losses of mesons)

○  $\nu_\tau$ -suppressed (prompt  $\nu_\tau$ )  
 $L_{\text{osc}}(E \approx \text{TeV-PeV})$  is too large

Event rate of  $O(1 \text{ yr}^{-1} \text{ sr}^{-1})$  for two separable and contained showers with  $E \approx \text{PeV}$  in a  $\text{km}^3$   $\nu$ -telescope



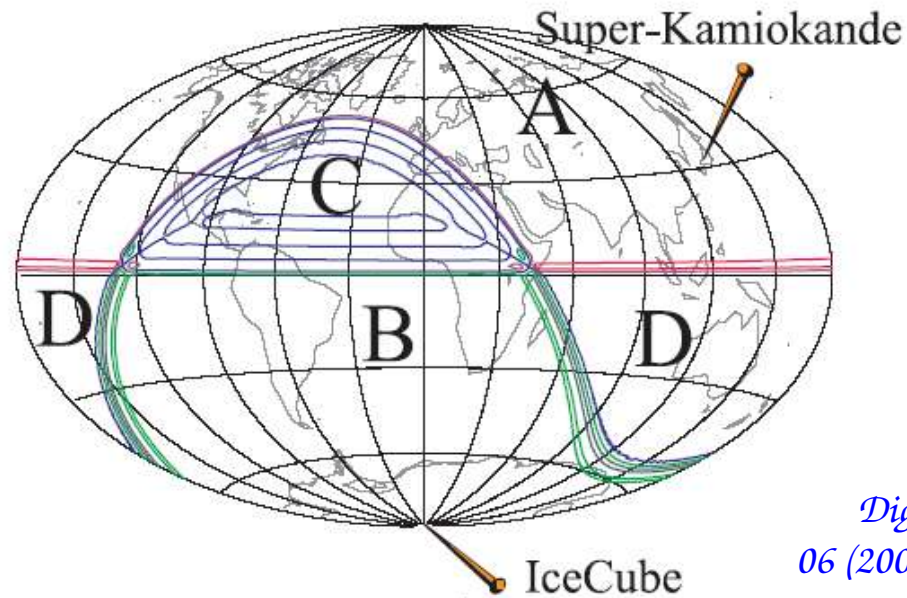
Independent confirmation of the (large) mixing in the  $\mu$ - $\tau$  sector via  $\nu_\tau$  appearance



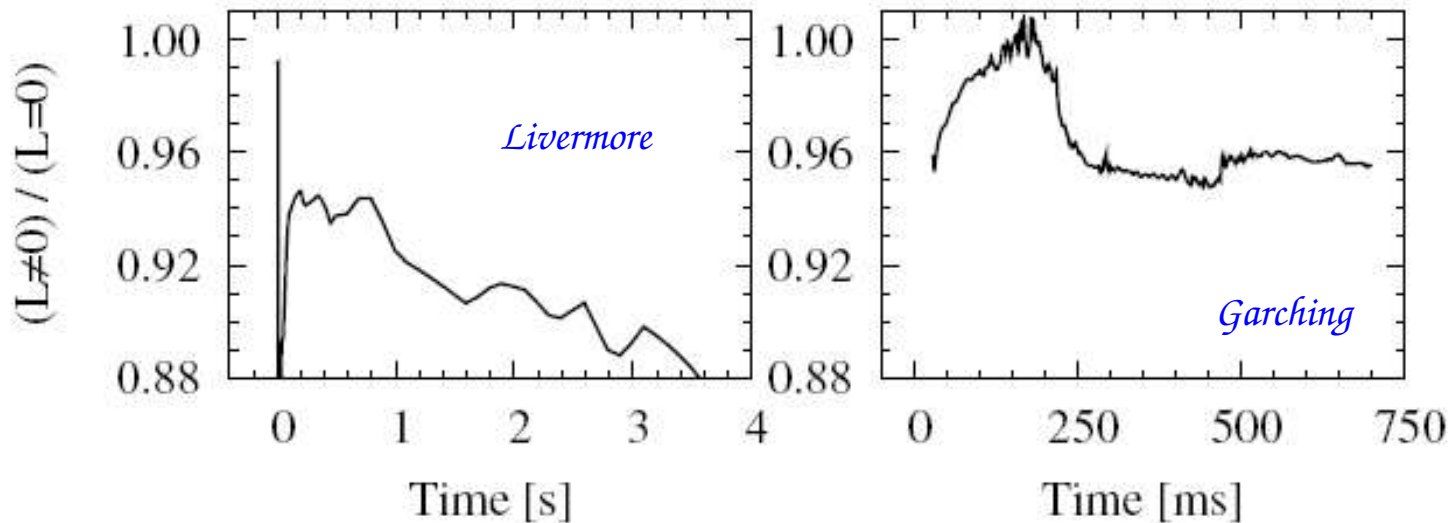
# Earth matter effect with a SN at IceCube



Flux vs. time at  
 IceCube + SK (or HK)  
 can detect Earth  
 matter effects  
 (normal hierarchy  
 and  $\sin^2 \theta_{13} > 10^{-3}$ )  
 Exploits high statistics  
 for a galactic SN



Dighe et al.  
 06 (2003) JCAP 005



# $\nu$ -telescopes, the Glashow resonance and $\theta_{12}$

“Standard” astrophysical sources produce both  $\nu$  and  $\bar{\nu}$  via

$$pp \rightarrow \pi X$$

$$p\gamma \rightarrow \pi X$$

Both give flavour ratios at production

$$\phi_e : \phi_\mu : \phi_\tau \approx 1/3 : 2/3 : 0$$

but  $p\gamma$  mainly gives  $\nu_e$  (via  $\pi^+$ ), while  $pp$  almost equally  $\nu_e$  and  $\bar{\nu}_e$

The measurable ratio

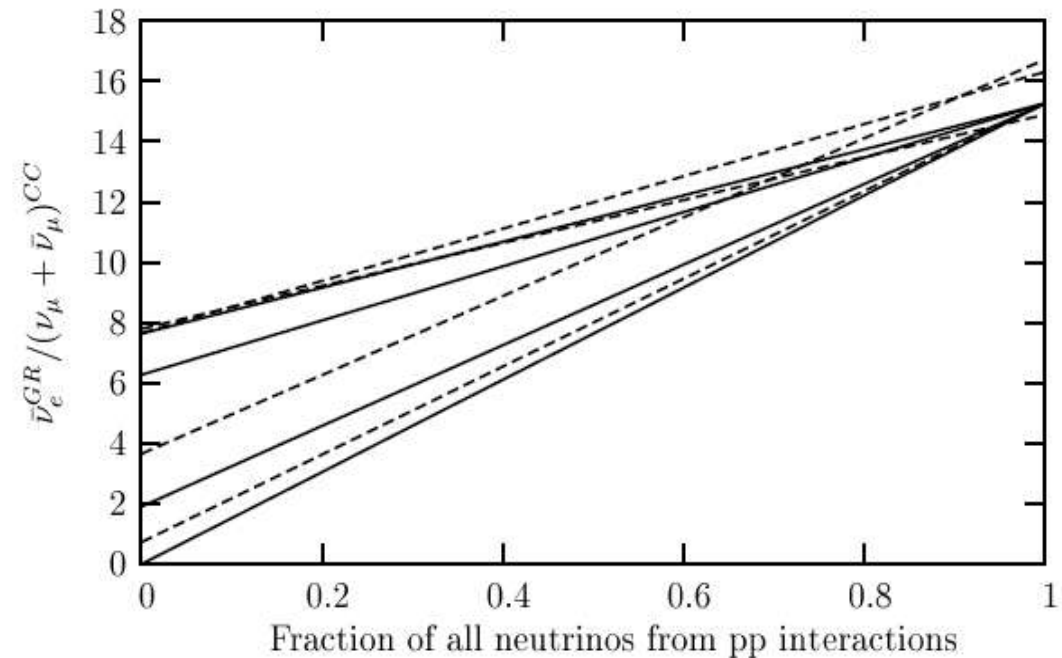
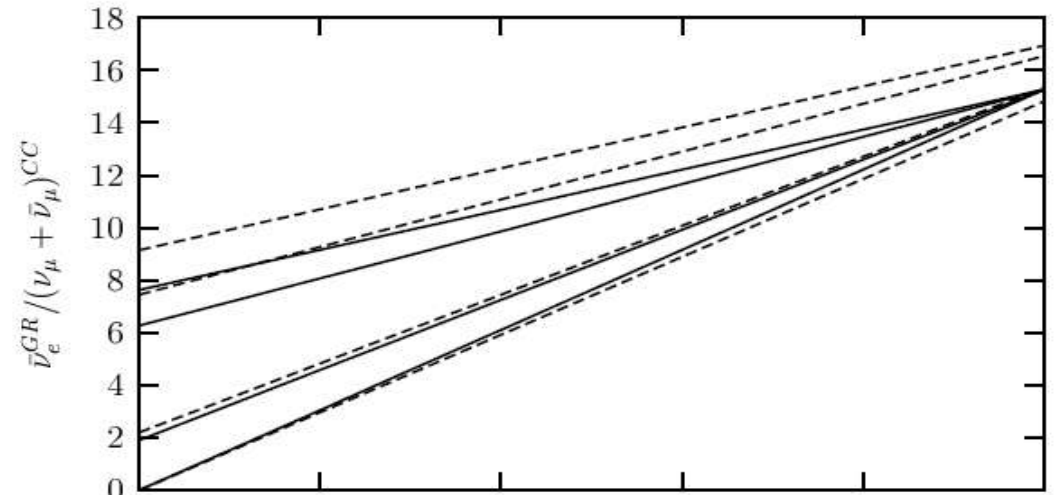
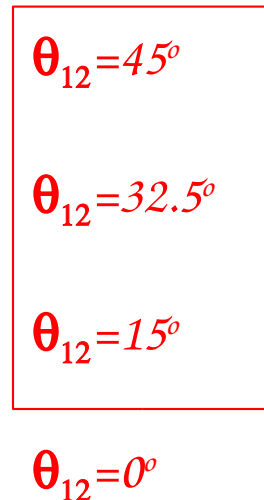
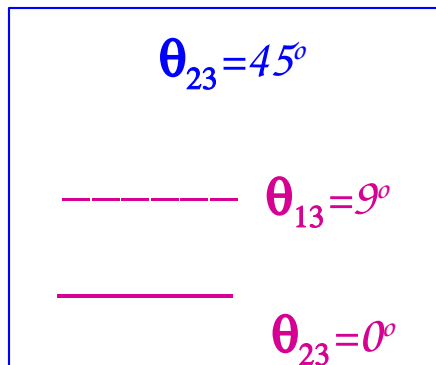
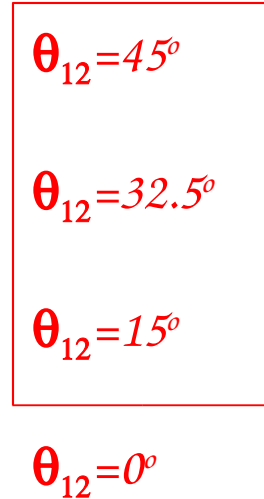
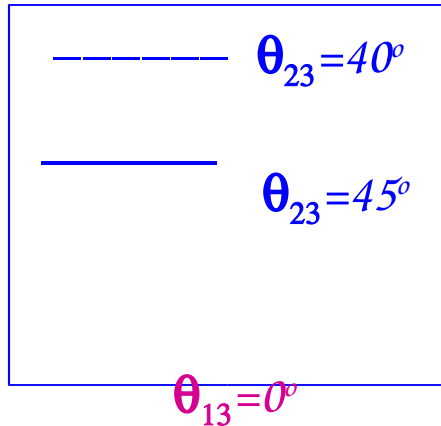
$$\mathcal{R}^{\text{GR}} \equiv \nu_e^{\text{GR}} / (\nu_\mu + \bar{\nu}_\mu)^{\text{CC}} \approx 15 [\text{Sin}^2 2\theta_{12} + \kappa (1 - 0.5 \text{Sin}^2 2\theta_{12})]$$

$(\theta_{13} = 0^\circ \text{ and } \theta_{23} = 45^\circ)$

is sensitive both to mixing angles (mainly  $\theta_{12}$ ) AND to the production mechanism (% of  $pp$  “contamination”  $\equiv \kappa$ )

(Bhattacharjee & Gupta, astro-ph/0501191)

# $\nu$ -telescopes, the Glashow resonance and $\theta_{12}$



# “Peculiar” high energy neutrino (re)sources

1. *neutrons beams from nuclear dissociations*  $\rightarrow$  pure  $\nu_e$  beam -

2. *pion beams from muon damped sources*  $\rightarrow$  pure  $\nu_\mu + \bar{\nu}_\mu$  beam -

*In both cases, the observable ratio of  $\mu$  tracks to  $e+\tau$  showers*

$$\mathcal{R} = \frac{\Phi_\mu}{(\Phi_e + \Phi_\tau)}$$

*is sensitive to crucial information of the neutrino mixing matrix !!!*

*P.S. & M. Kachelrieß PRL 94, 211102 (2005) [hep-ph/0502088],*

*P.S., work in progress*



# Neutrino Mixing - Probabilities

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \underbrace{\begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{CP}} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta_{CP}} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta_{CP}} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta_{CP}} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta_{CP}} & c_{13}c_{23} \end{pmatrix}}_{\text{Mixing Matrix } U} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$s_{lk} \equiv \text{Sin } \theta_{lk}, c_{lk} \equiv \text{Cos } \theta_{lk}$

- Matter effects negligible
- $d_{\text{source}} \gg L_{\text{osc}}$ : Terms sensitive to  $\Delta m^2$ ,  $\text{sign}(\delta_{CP})$  average out
- Also imply equal expressions for neutrinos and antineutrinos

$$P_{\alpha\beta} \equiv P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 2 \sum_{j>k} \text{Re}(U_{\beta j} U_{\beta k}^* U_{\alpha j}^* U_{\alpha k})$$

Flavor ratios at detector  $\phi_\beta^D = \sum_\alpha P_{\alpha\beta} \phi_\alpha$  Flavor ratios at source

*“Galactic  $\beta$ -beams”*

# Sensitivity to $\theta_{13}$ (and $\theta_{23}$ )

$$\mathcal{R} \equiv \frac{\phi_\mu}{(\phi_e + \phi_\tau)} = \frac{P_{e\mu}}{P_{ee} + P_{e\tau}}$$

$$P_{ee} \approx \frac{5}{8} - \frac{5}{4}\theta_{13}^2$$

$$P_{e\mu} \approx \frac{3}{16} + \frac{\sqrt{3}}{8}\theta_{13} \cos \delta_{\text{CP}} + \frac{5\theta_{13}^2}{8}$$

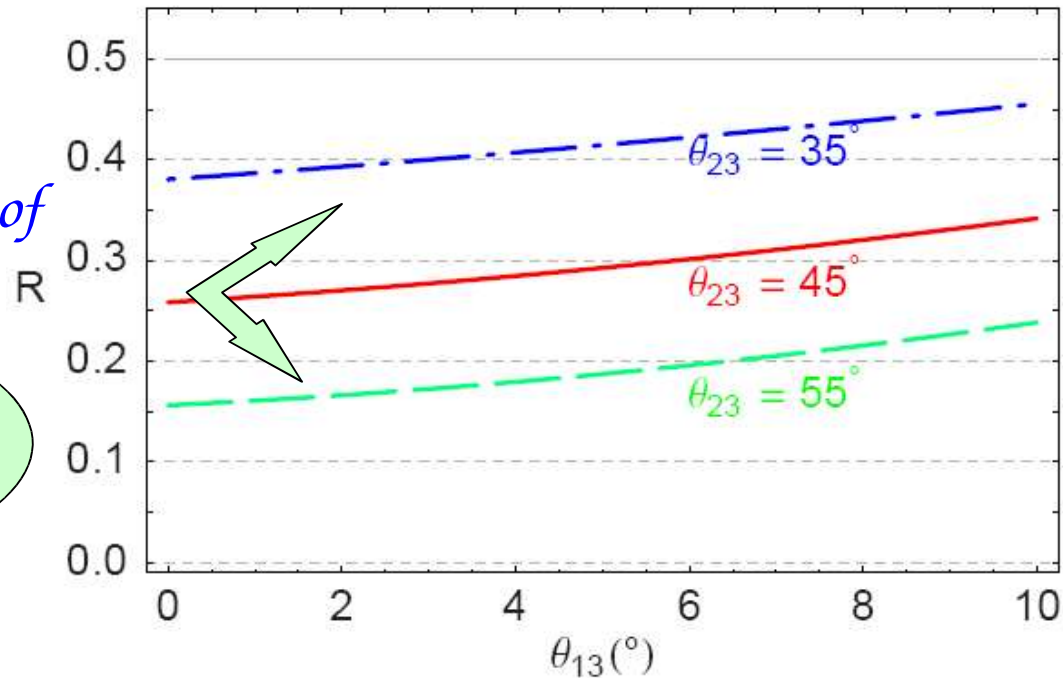
$$P_{e\tau} \approx \frac{3}{16} - \frac{\sqrt{3}}{8}\theta_{13} \cos \delta_{\text{CP}} + \frac{5\theta_{13}^2}{8}$$

$\theta_{12} = \pi/6$   
 $\theta_{23} = \pi/4$

Variation of order 25-50%  
 in  $0^\circ < \theta_{13} < 10^\circ$ , depending on  $\theta_{23}$   
 ( $\theta_{12} = 32.5^\circ$ , best case  $\delta_{\text{CP}} = 0$ )

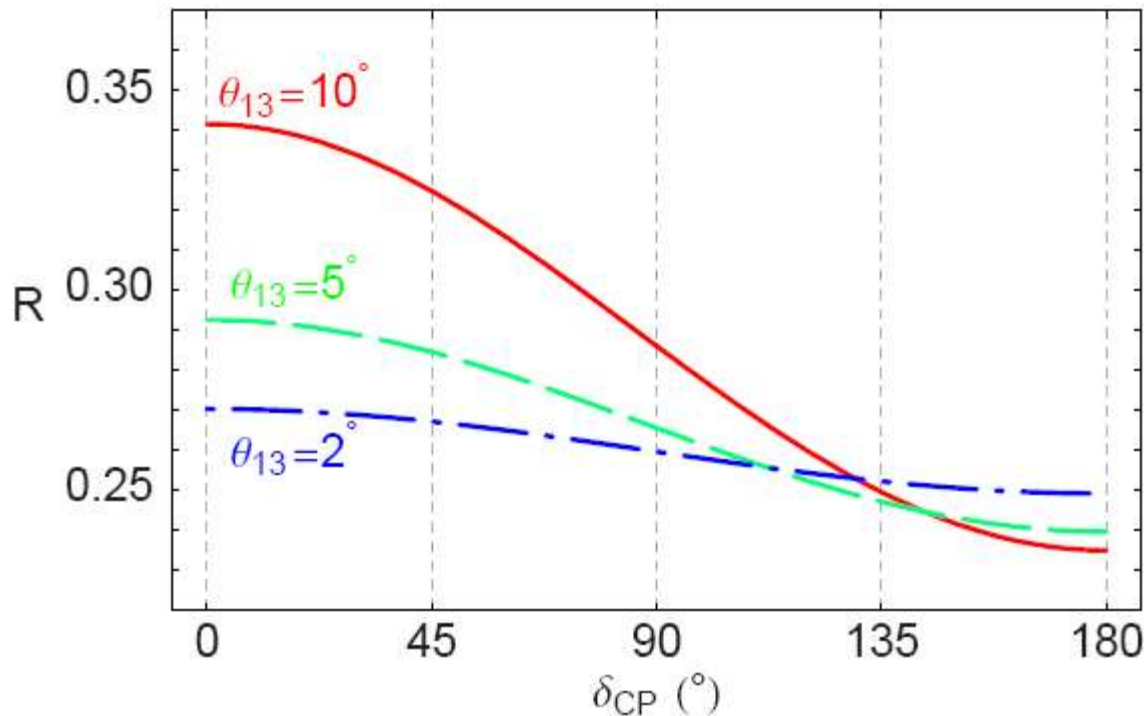
For  $\theta_{23} = 45^\circ$ ,  $\mathcal{R}$  is reduced even to  $\frac{1}{2}$  of  
 the canonical  $\mathcal{R} = 0.5$

Note the octant  
 dependence!



# Sensitivity to $\delta_{CP}$

For experimental best fit  $\theta_{12}=32.5^\circ$  and  $\theta_{23}=45^\circ$ , the flux ratio has a maximal variation of about 30%



*NOTE: only sensitive to  $\cos(\delta_{CP})$  [CP-even term] not "direct" observation of CP-violation*

# Determination of the octant of $\theta_{23}$

$$\mathcal{R} = \frac{P_{e\mu}}{P_{ee} + P_{e\tau}}$$

$$P_{ee} \approx \frac{5}{8},$$

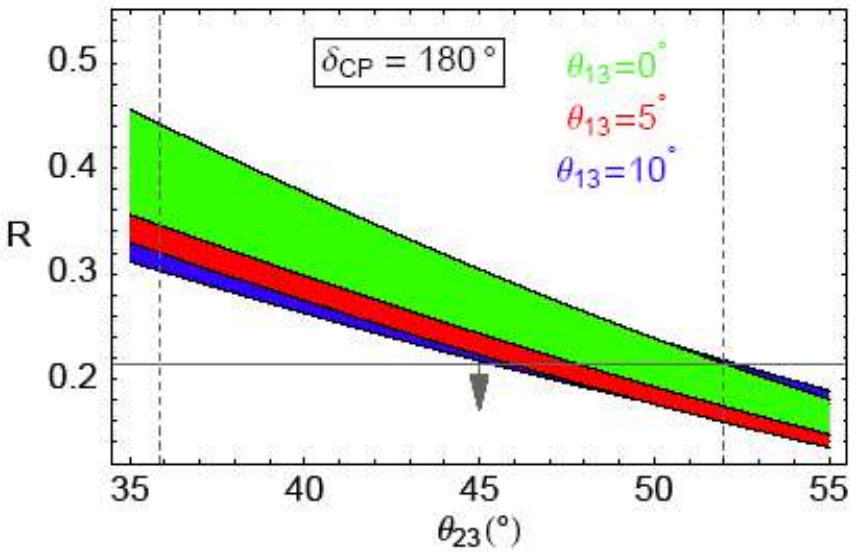
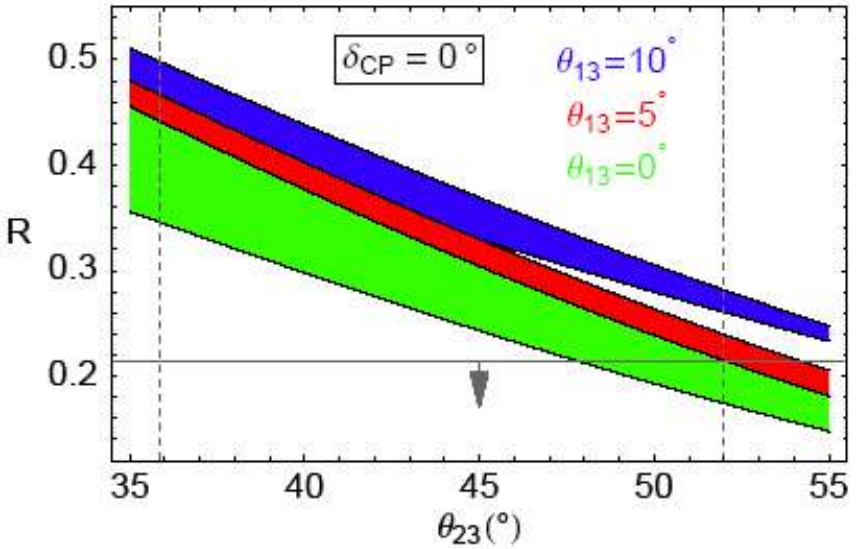
$$P_{e\mu} \approx \frac{3}{8} c_{23}^2 + \frac{\sqrt{3}}{4} s_{23} c_{23} s_{13} c_{\delta},$$

$$P_{e\tau} \approx \frac{3}{8} s_{23}^2 - \frac{\sqrt{3}}{4} s_{23} c_{23} s_{13} c_{\delta},$$

$$\mathcal{R} < 0.21 \rightarrow \theta_{23} > \pi/4$$

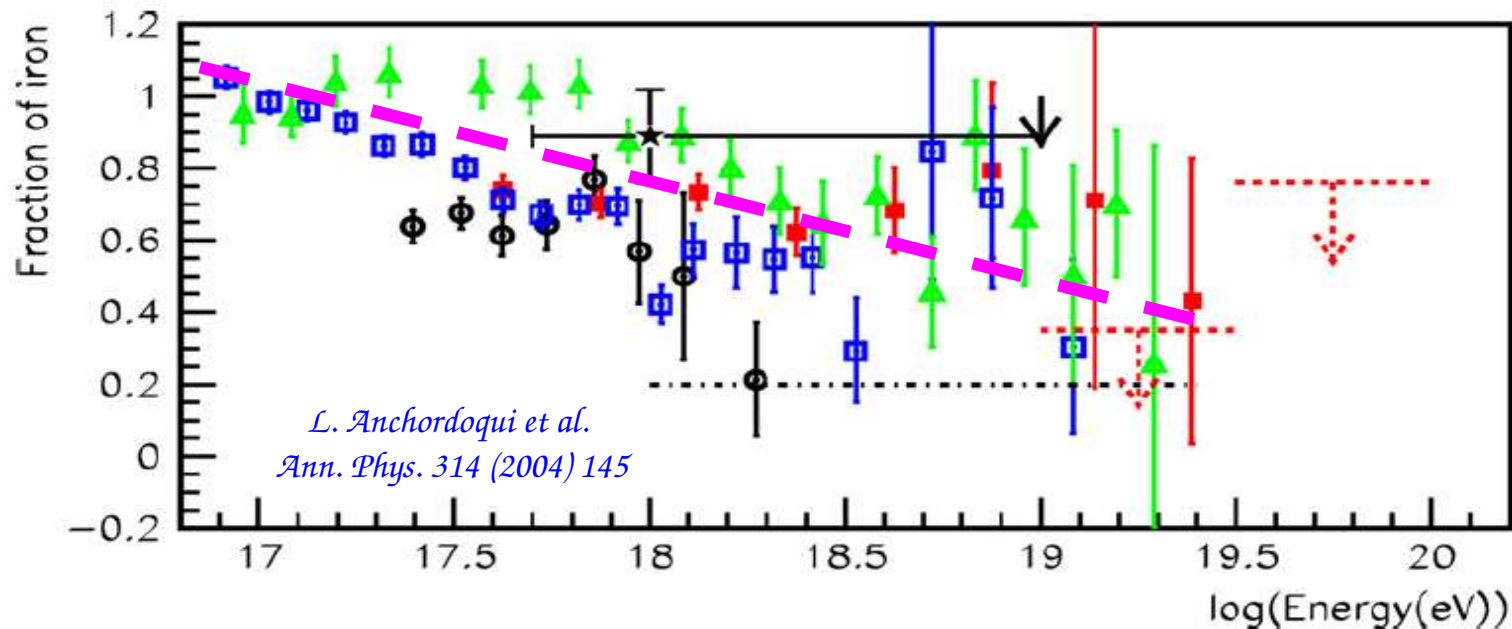
*Backgrounds can only increase  $\mathcal{R}$ !*

*Model-independent statement*



# Neutrinos from nuclei in the Galaxy

*In cosmic rays, at  $E \approx O(1 \text{ EeV})$  a transition between High-Z nuclei of the Galactic spectrum (acceleration and confinement requirements are alleviated) and p-dominated Extragalactic contribution is expected. Recent CR data support this scenario*



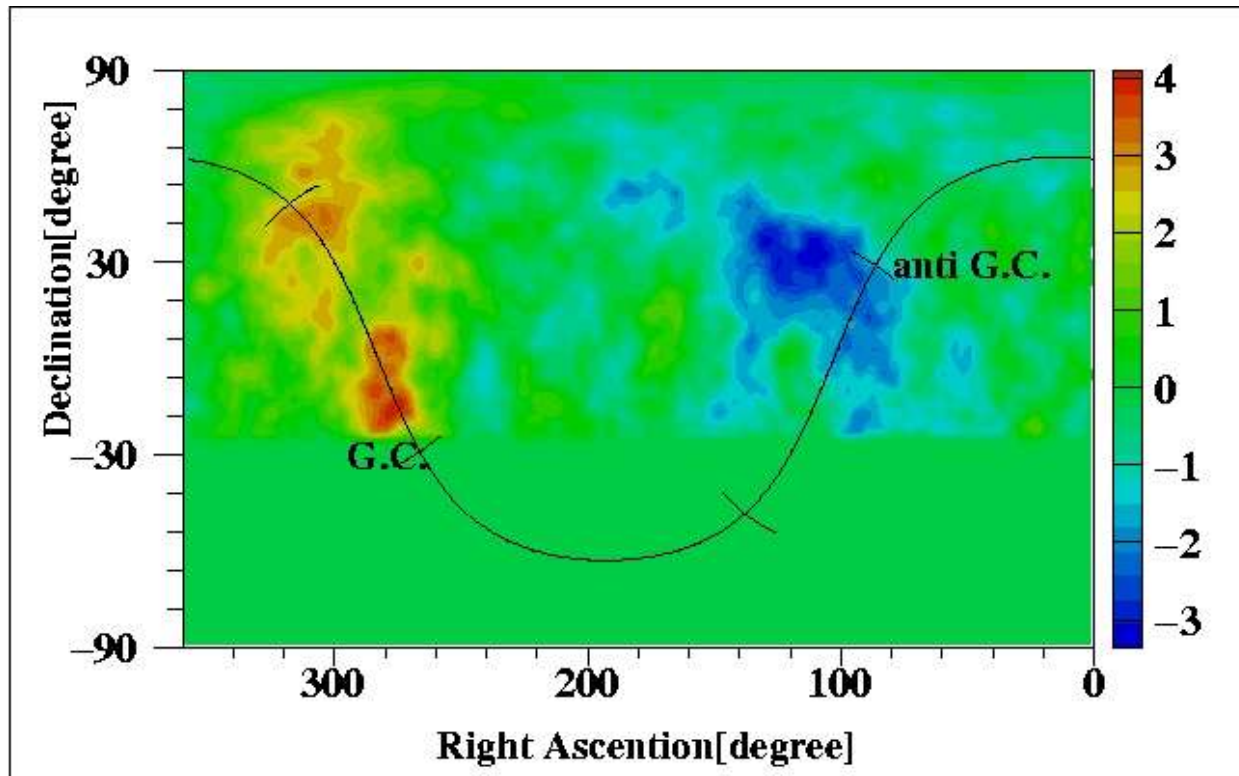
*n from nuclei dissociations in matter and  $\gamma$ -fields in (a few) galactic accelerators might become visible at EeV.*

*Favored regions: Nuclear Bulge, dense clouds (high B-field) ...*



# Hint: A Galactic Plane excess in EeV Cosmic Rays

AGASA reported a 4% excess in UHECR around  $10^{18}$  eV (1 EeV) from a couple of hot-spots in the galactic disk



Similar, independent hints also from SUGAR and Fly's Eye  
(but negative results from preliminary analysis of Auger data)

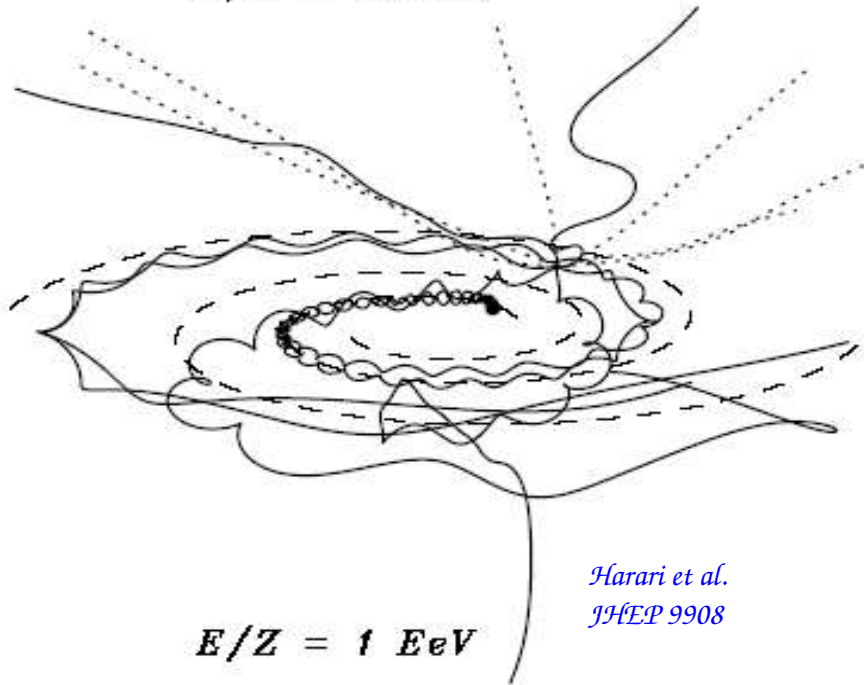
# The birth of Galactic neutron Astronomy?

Neutrons are natural candidates to explain the signal

no GMF bending (huge for p too!)

Energy-range of the Signal  
 $\approx$  boosted n-lifetime

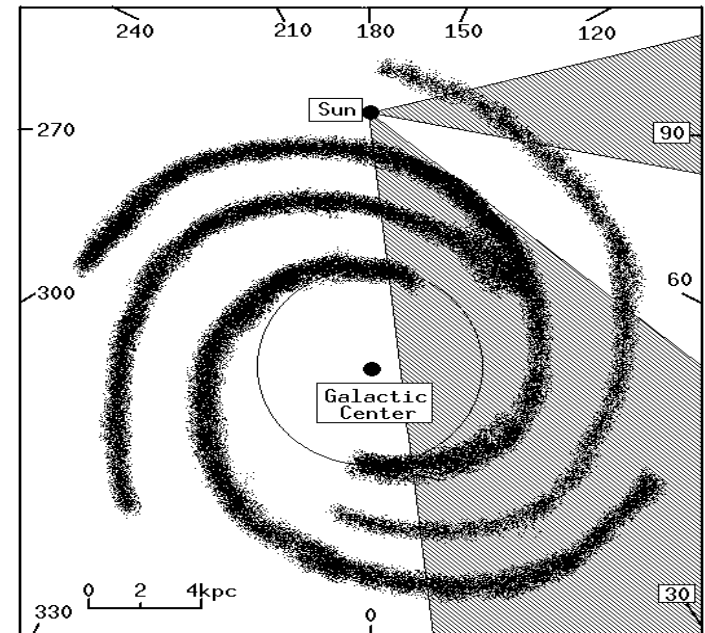
$$E/Z = 10 \text{ EeV}$$



$$E/Z = 1 \text{ EeV}$$

Harari et al.  
JHEP 9908

$$c\tau_n \approx 10 \text{ kpc } (E_n / \text{EeV})$$



# From Neutrons to Neutrinos

The existence of galactic neutron beams would imply

$\nu_e$  fluxes up to the PeV from n-decay.

$$(\mathcal{E}_\nu / \mathcal{E}_n \sim Q / m_n \sim 10^{-3} \rightarrow \mathcal{E}_\nu \sim \text{PeV}, \text{ for } \mathcal{E}_n \sim \text{EeV})$$

If neutrons come from nuclear photodissociations on Optical/UV photons, the flux is likely to extend down to (at least) TeV region

This energy range nicely fits the energy-window accessible to  $\nu$ -telescopes under construction.

Notice that n are undetectable as CR anisotropies below  $\mathcal{E} \sim 10^{17}$  eV: similar sources of lower Energy might show-up only in the  $\nu_e$  channel !!!

*A model of galactic neutron beams*

# Detectability in IceCube

Normalizing to the CR anisotropy,  $\sim 20$  events per year from Cygnus region in IceCube  
(under construction at the South pole)

Standard  $\nu$  oscillation phenomenology implies

$\approx 4 \nu_\mu$  /yr tracks in  $0.7^\circ$  circle

(Atm. background is  $\sim 2.3 \nu_\mu$  /yr)

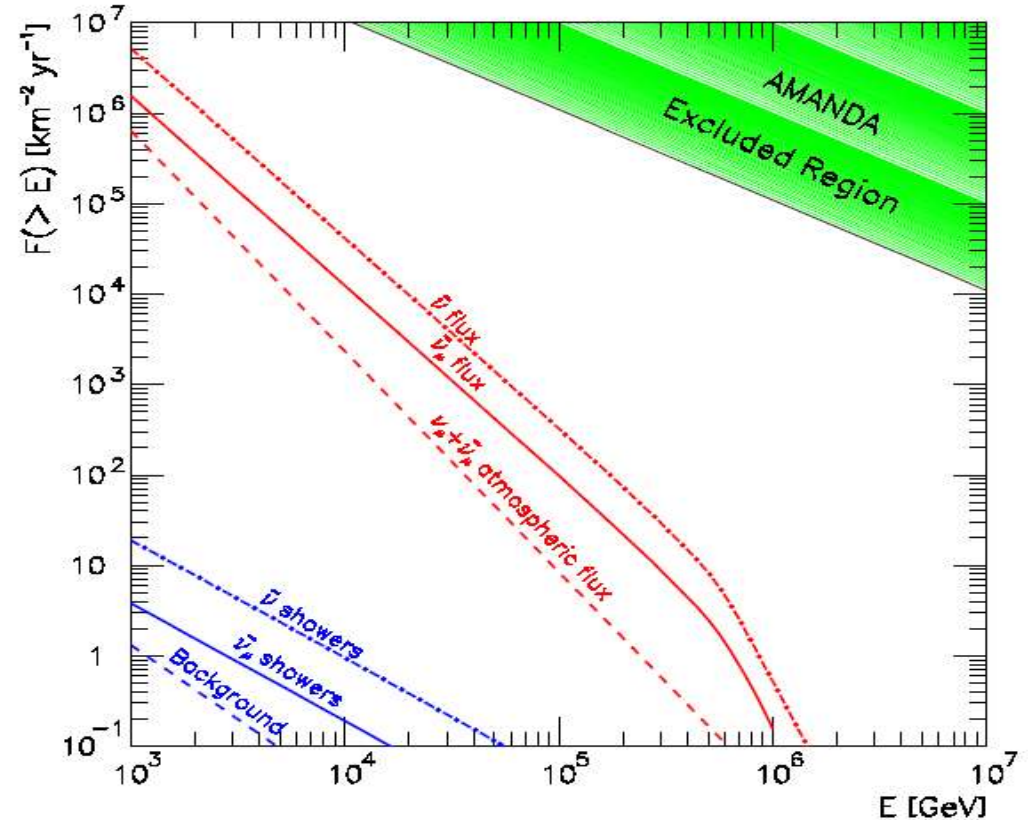
$\approx 16 \nu_e + \nu_\tau$  showers/yr in  $25^\circ$  cone, due to poor resolution.

(Atm. background fluctuation is  $\sim 12$

$\nu_e + \nu_\tau$  /yr)

In a few years, IceCube should attain discovery sensitivity

for  $n \rightarrow \nu_e \rightarrow \nu_\mu$  !!!



L. Anchordoqui, H. Goldberg,  
F. Halzen & T.J. Weiler  
PLB 593 (2004) 42



# How large is the expected “pion contamination”?

Viable models of  $\mathcal{A} \rightarrow n \rightarrow \nu$  scenarios exist, e.g.:

Cygnus region: L. Anchordoqui et al. *PLB* 593 (2004) 42

SGR A East SN remnant: Grasso and Maccione [astro-ph/0504323]

From astrophysical data e.g. on the Cygnus region (e.g.  $UV\gamma$  density) and hadronic physics data (e.g. secondary population yields in hadronic interactions)

$$V_{\text{nuclear dissociation}} \approx 27 \chi V_{pp \text{ hadronic interactions}}$$

In this case, likely  $\pi$  contaminations to  $\nu$  flux are at the  $O(10\%)$  level  $\rightarrow \Delta\mathcal{R} \approx +0.02$  only!

Within the expected statistical accuracy of IceCube & at the same subleading level of other effects neglected in our estimate

# Is this scenario falsifiable?

Normalizing the anisotropy to the “n-chain” model,  
 $n \rightarrow \nu$ -fluxes should easily be observable in IceCube,  
with a detailed measurement in a decade.

If the  $\pi$ -chain dominates, the flux should be much  
higher, though with a flavour ratio of about 1:1:1

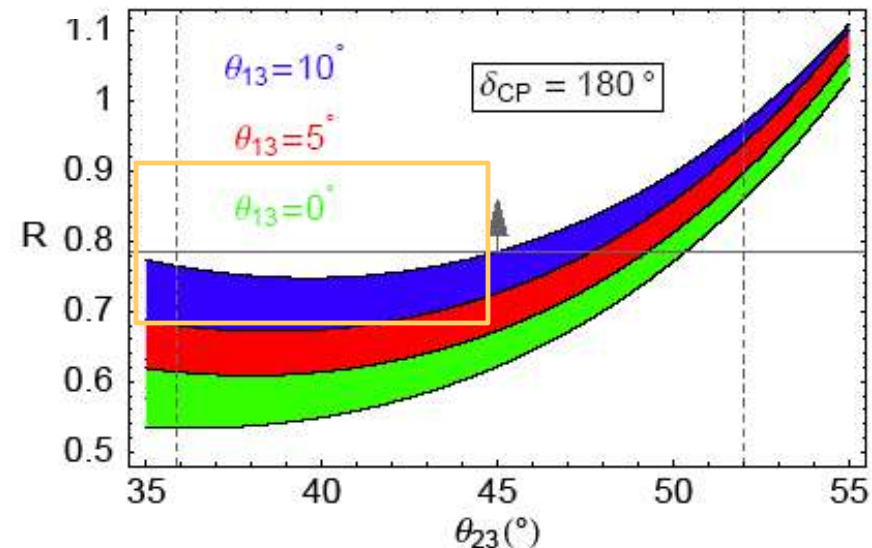
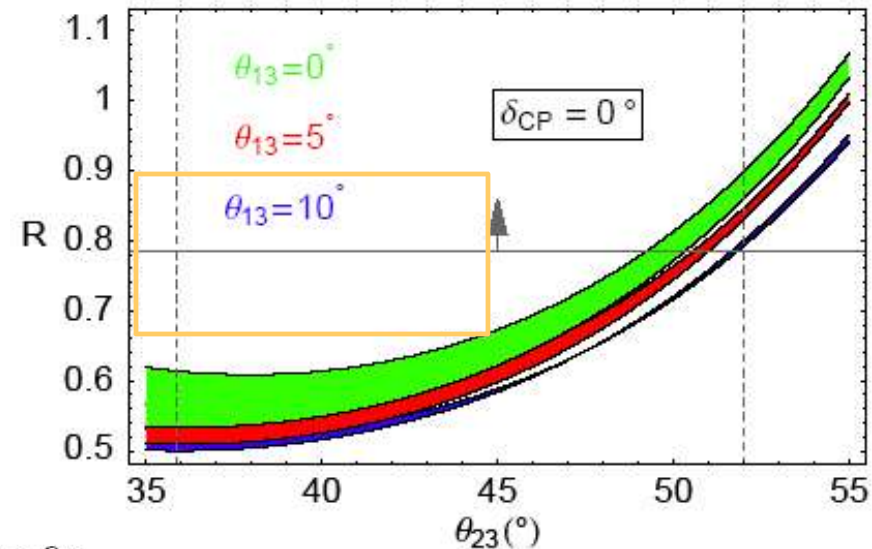
Also  $\gamma$ -rays constraints!

High  $\nu$  flux and  $R=0.5$  would disprove  
the dominance of  $\mathcal{A} \rightarrow n \rightarrow \nu$ !

*muon-damped sources*

# Sensitivity to the octant of $\theta_{23}$

$$\mathcal{R} \equiv \frac{\phi_{\mu}}{(\phi_e + \phi_{\tau})} = \frac{P_{\mu\mu}}{1 - P_{\mu\mu}}$$



$$P_{\mu\mu} \approx 1 - \frac{3}{8}c_{23}^4 - 2c_{23}^2s_{23}^2 - \frac{\sqrt{3}}{2}c_{23}^3s_{23}s_{13}c_{\delta}$$

$$\mathcal{R} > 0.78 \rightarrow \theta_{23} > \pi/4$$

Backgrounds can only decrease  $\mathcal{R}$ !

Model-independent statement

# Why pion beams?

Effective “*pion beams*” produced in sources where muons  
(but not pions) are damped sources  $\rightarrow$  pure  $\nu_\mu + \bar{\nu}_\mu$  beam

Boosted Lifetime  $\propto \mathcal{E}$

E.m. cooling time  $\propto \mathcal{E}^{-1}$  (Inv. Compton),  $\mathcal{E}^0$  (adiabatic expansion),...

Their ratio increases with  $\mathcal{E}$ , at a certain  $\epsilon_0$  the particle is stopped before decaying.

The lifetime implies  $\epsilon_{0\mu} \ll \epsilon_{0\pi}$

For AGN,  $\pi$  beams @  $O(10^6)$  TeV  $\rightarrow$  unobservable at OCT

For GRB,  $\pi$  beams possibly @  $O(10)$  TeV  $\rightarrow$  optimal for OCT!!!

Flavour ratios can be used for astrophysical diagnostics

Kahsti & Waxman, *PRL* 95 (2005) 181101



*Concluding remarks*

# Overview - I

*Neutrino telescopes are optimized for astrophysical purposes, but they may have a potential for  $\nu$ -mixing physics, too.*

*$\nu_\tau$  appearance expected to be seen within 3-4 years (IceCube completed + 1 year of running)*

*“Calorimetric” detection of a galactic core-collapse SN possible. Earth matter effect (and thus hierarchy/ $\theta_{13}$ ) possibly identified at IceCube+ “HK”, or +Mediterranean km<sup>3</sup>*

## Overview - II

*I showed that it is conceivable or even likely that Nature might provide “ $\beta$ -beams” (or pion beams) for free, that could be studied at  $\nu$ -telescopes already in construction.*

*Measurable flavor ratios are sensitive to  $\theta_{13}$ ,  $\delta_{CP}$ , and to the octant of  $\theta_{23}$ . The latter is particularly suitable for a model-independent determination (if  $\theta_{23} > \pi/4$ )*

*Going beyond the paradigm of a “canonical” flavor equipartition would repropose at neutrino telescopes the fruitful synergy between neutrino physics and astrophysical diagnostics*

*Synergy between Earth & Heaven*



*THANK YOU!*

# Neutrino mixing parameters

## Solar/Kamland

Best Fit:  $\sin^2 \theta_{sol} = 0.29$ ,  $\Delta m_{sol}^2 = 8.1 \times 10^{-5} \text{ eV}^2$

3 $\sigma$  range:  $0.23 < \sin^2 \theta_{12} < 0.37$ ,  $7.3 \times 10^{-5} < \Delta m_{sol}^2 / \text{eV}^2 < 9.1 \times 10^{-5}$

Best Fit:  $\theta_{sol} = 32.6^\circ$

3 $\sigma$  range:  $28.7^\circ < \theta_{sol} < 37.5^\circ$

## Atmospheric/K2K

Best Fit:  $\sin^2 \theta_{atm} = 0.5$ ,  $\Delta m_{atm}^2 = 2.2 \times 10^{-3} \text{ eV}^2$

3 $\sigma$  range:  $0.34 < \sin^2 \theta_{atm} < 0.66$ ;  $1.4 \times 10^{-3} < \Delta m_{atm}^2 / \text{eV}^2 < 3.3 \times 10^{-3}$

Best Fit:  $\theta_{atm} = 45^\circ$

3 $\sigma$  range:  $35.7^\circ < \theta_{sol} < 54.3^\circ$

## Global (CHOOZ+others)

Best Fit:  $\sin^2 \theta_{13} = 0$

3 $\sigma$  range:  $\sin^2 \theta_{13} < 0.047$ ,

$\theta_{13} < 12.5^\circ$

Maltoni et al.,  
NJP 6 (2004) 122



# $\sigma(\nu\mathcal{N})$ vs. $E$

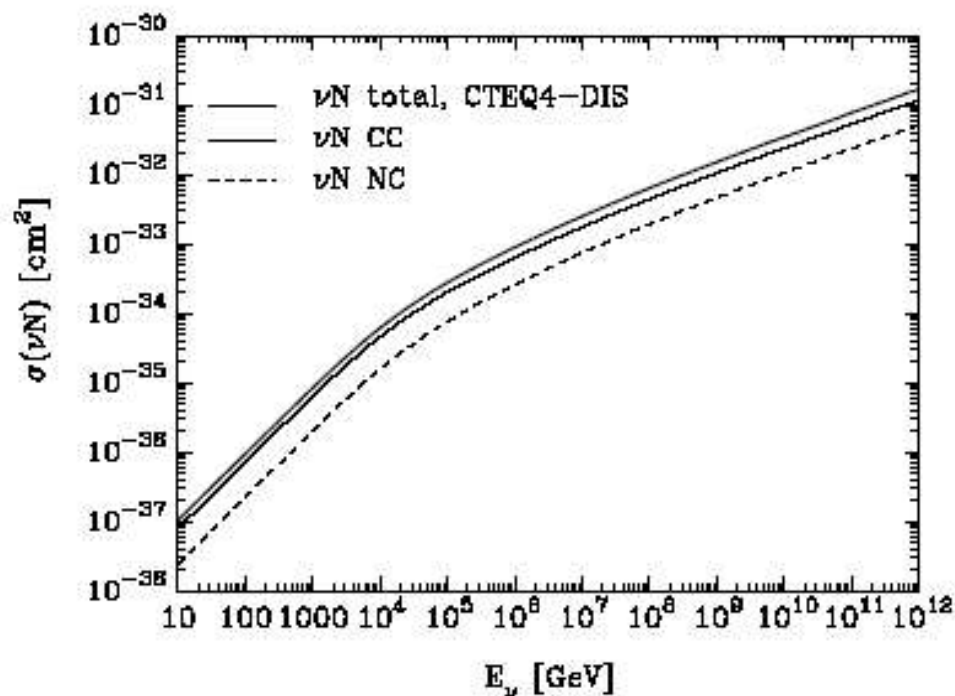


FIG. 1. Cross sections for  $\nu_\ell N$  interactions at high energies, according to the CTEQ4-DIS parton distributions: dashed line,  $\sigma(\nu_\ell N \rightarrow \nu_\ell + \text{anything})$ ; thin line,  $\sigma(\nu_\ell N \rightarrow \ell^- + \text{anything})$ ; thick line, total (charged-current plus neutral-current) cross section.

*R. Gandhi, C. Quigg, M. H. Reno and I. Sarcevic,  
Neutrino interactions at ultrahigh energies,  
Phys. Rev. D 58, 093009 (1998)  
[hep-ph/9807264].*

# $\sigma(\bar{\nu}N)$ vs. $E$

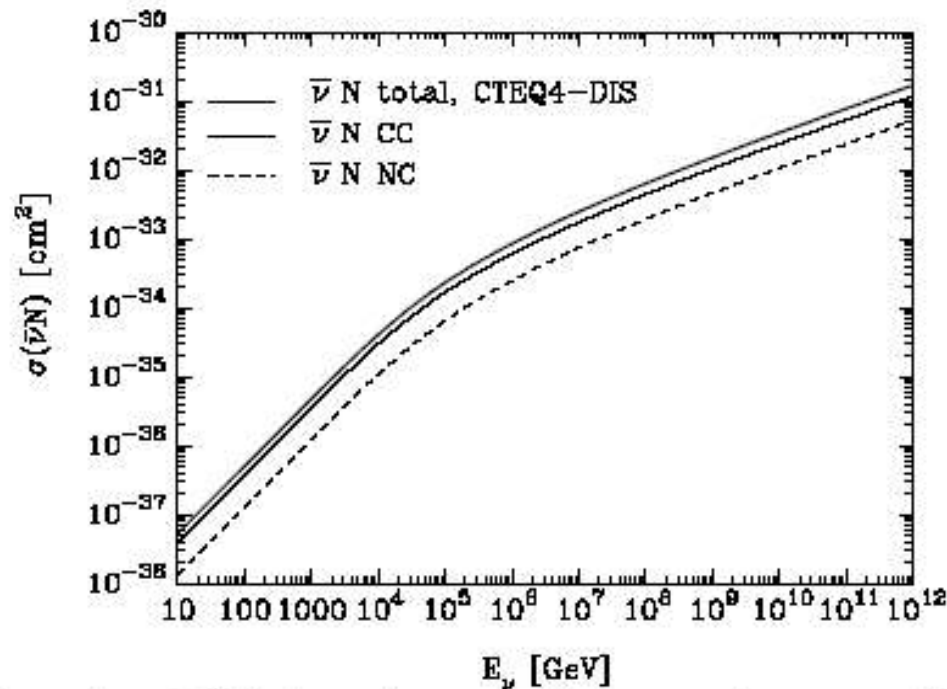


FIG. 3. Cross sections for  $\bar{\nu}_\ell N$  interactions at high energies, according to the CTEQ4-DIS parton distributions: dashed line,  $\sigma(\bar{\nu}_\ell N \rightarrow \bar{\nu}_\ell + \text{anything})$ ; thin line,  $\sigma(\bar{\nu}_\ell N \rightarrow \ell^+ + \text{anything})$ ; thick line, total (charged-current plus neutral-current) cross section.

*R. Gandhi, C. Quigg, M. H. Reno and I. Sarcevic,  
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# Clarification on $\delta_{CP}$

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{j>k} \text{Re}(J_{\alpha\beta jk}) \sin^2 \frac{\Delta m_{jk}^2 L}{4E} + 2 \sum_{j>k} \text{Im}(J_{\alpha\beta jk}) \sin \frac{\Delta m_{jk}^2 L}{2E}$$

$$J_{\alpha\beta jk} = U_{\beta j} U_{\beta k}^* U_{\alpha j}^* U_{\alpha k} \quad \nu \rightarrow \bar{\nu} \quad J_{\alpha\beta jk} \rightarrow J_{\alpha\beta jk}^*$$

$$\text{Im}(J_{\alpha\beta jk}) = J \sum_{\gamma, l} \epsilon_{\alpha\beta\gamma} \epsilon_{jkl}$$

Jarlskog determinant

$$J = c_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \sin \delta$$

$$P(\nu_e \rightarrow \nu_\mu) = P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) = 4c_{13}^2 [\sin^2 \Delta_{23} s_{12}^2 s_{13}^2 s_{23}^2 + c_{12}^2 (\sin^2 \Delta_{13} s_{13}^2 s_{23}^2 + \sin^2 \Delta_{12} s_{12}^2 (1 - (1 + s_{13}^2) s_{23}^2))] - \frac{1}{4} |\tilde{J}| \cos \delta [\cos 2\Delta_{12} \cos 2\Delta_{23} - 2 \cos 2\theta_{12} \sin^2 \Delta_{12}] + \frac{1}{4} |\tilde{J}| \sin \delta [\sin 2\Delta_{12} - \sin 2\Delta_{13} + \sin 2\Delta_{23}],$$

*CP-even*

*CP-odd*

Apollonio et al. hep-ph/0210192