

NuFact Summer Institute

Capri 2005

Physics of massive ν_s

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LECTURE III

An *almost* up-to-date phenomenological
overview of the three-neutrino
mass-mixing parameters

(complete 2005 update + details in next lecture)

Outline:

- Overview of 3ν mass-mixing parameters
- Constraints from ν oscillation searches
- Constraints from non-oscillation searches
- Combining oscill. & non-oscill. ν observables
- Beyond the standard 3ν scenario (LSND)
- Conclusions

3ν mixing - brief recap

- Neutrinos fields mix:

$$(\nu_e, \nu_\mu, \nu_\tau)^T = U (\nu_1, \nu_2, \nu_3)^T$$

- The standard rotation ordering of the CKM matrix for quarks happens to be useful also for neutrinos:

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

... but with very different angles - we shall see that:

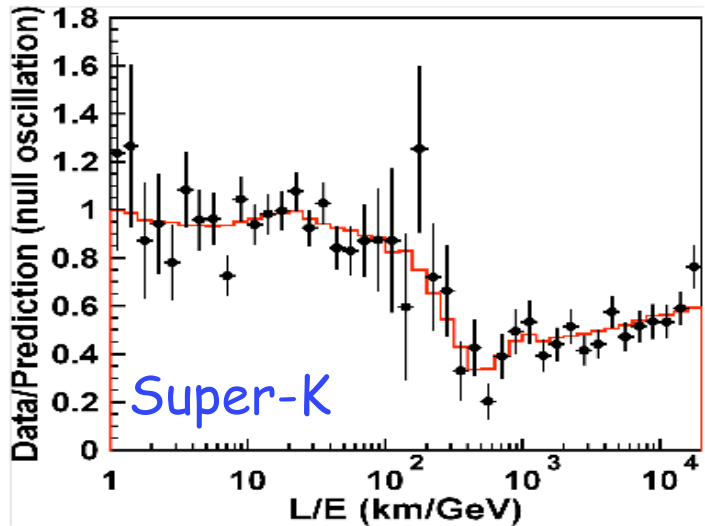
$$s_{23}^2 \sim 0.5$$

$$s_{13}^2 < \text{few } \%$$

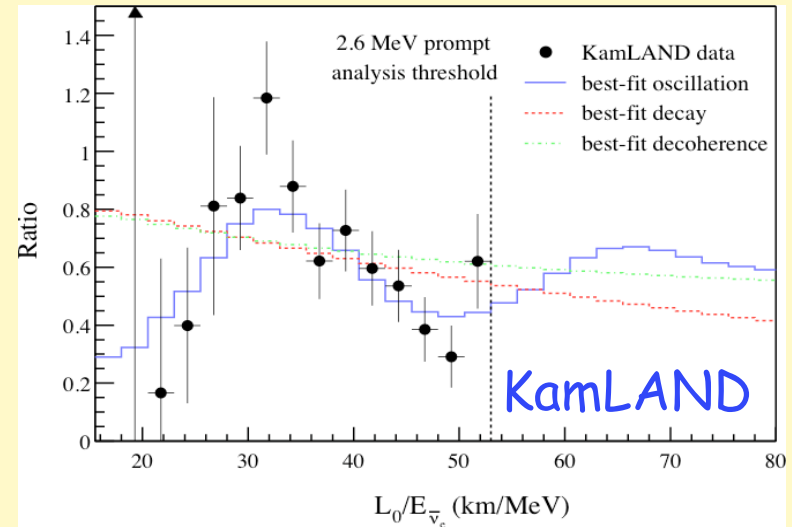
$$s_{12}^2 \sim 0.3$$

- Only if $s_{13}^2 \neq 0$ one can hope to probe the CP-violating phase δ ("holy grail" of future ν oscillation experiments like nu-factories)

Neutrino fields mix ... and oscillate, with at least two frequencies. "Textbook" plots:



Δm^2 -driven oscillations



δm^2 -driven oscillations

(about half-period seen in both cases)

3ν oscillations (remind also Lec. II, one-dominant-mass-scale approximation)

Two macroscopic oscillation lengths governed by δm^2 and Δm^2 , with amplitudes governed by θ_{ij} . Leading expt. sensitivities:

$(\Delta m^2, \theta_{23}, \theta_{13})$ Atmospheric ν , K2K long baseline accelerator (a)

$(\delta m^2, \theta_{12}, \theta_{13})$ Solar ν , KamLAND long baseline reactor ν (b)

$(\Delta m^2, \theta_{13})$ CHOOZ short-baseline reactor ν (a,b)

(a) (ν_1, ν_2) difference weakly probed

(b) (ν_μ, ν_τ) difference not probed

Status of 3-neutrino framework:

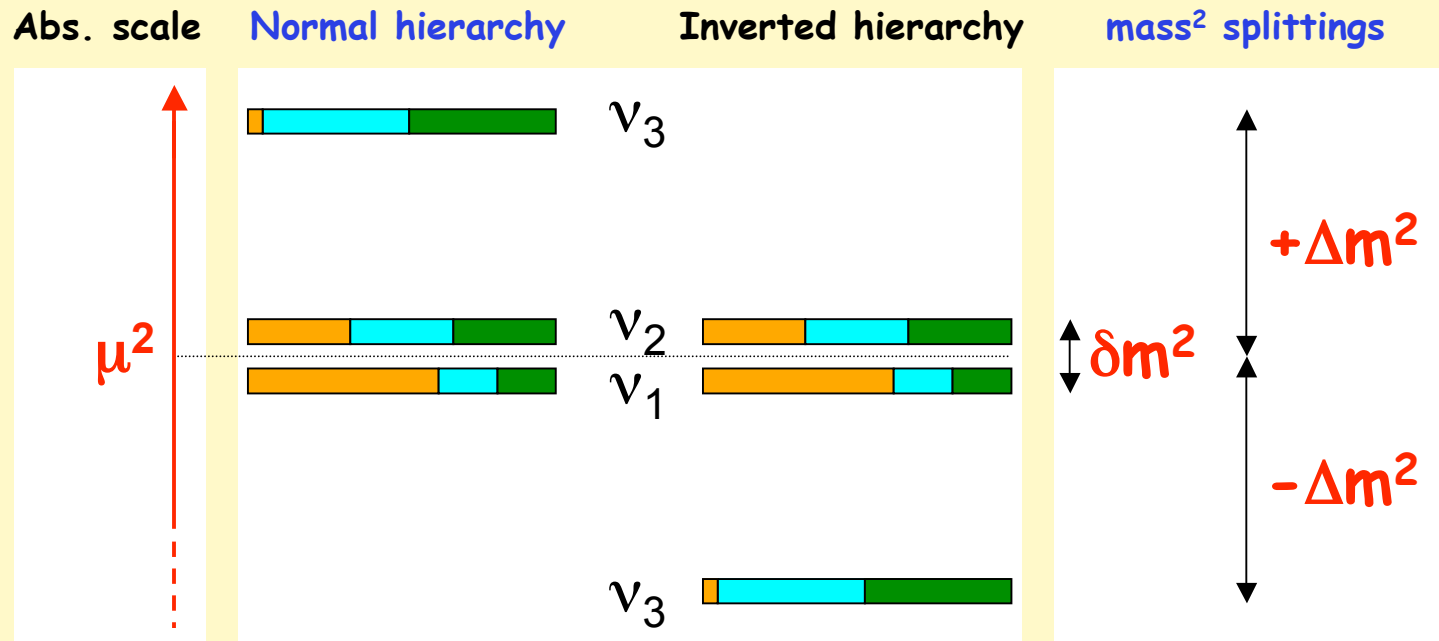
$(\Delta m^2, \theta_{23})$	robust upper + lower bound from atmospheric & accelerator data
$(\delta m^2, \theta_{12})$	robust upper + lower bound from solar & reactor data
$V_{MSW} = 0$	L/E vacuum osc. pattern recently seen in atm. & react. data
$V_{MSW} \neq 0$	matter effects recently established in solar neutrinos
θ_{13}	upper bound from CHOOZ reactor data + above data
μ	upper bound from laboratory (+ 1 st lower bound?) & cosmology
$\text{Sign}(\Delta m^2)$	unknown (is the hierarchy normal or inverted ?)
δ	unknown (is there leptonic CP violation ?)
φ_2, φ_3	unknown (are there Majorana phases?)

Questions beyond the standard 3-neutrino framework:

$\dim(H) = 3 + N_s$?	<i>Light sterile neutrinos?</i>
$V = V_{MSW} + \Delta V$?	<i>New (subleading) interactions in medium?</i>
$H \neq H^\dagger$?	<i>Neutrino decay ?</i>
$i\partial_t/\partial x \neq H\nu$?	<i>Non-hamiltonian evolution (decoherence)?</i>

...

3ν mass² spectrum and flavor content (e μ τ)



Absolute mass scale μ unknown [but $< O(\text{eV})$]

Hierarchy [$\text{sign}(\Delta m^2)$] unknown

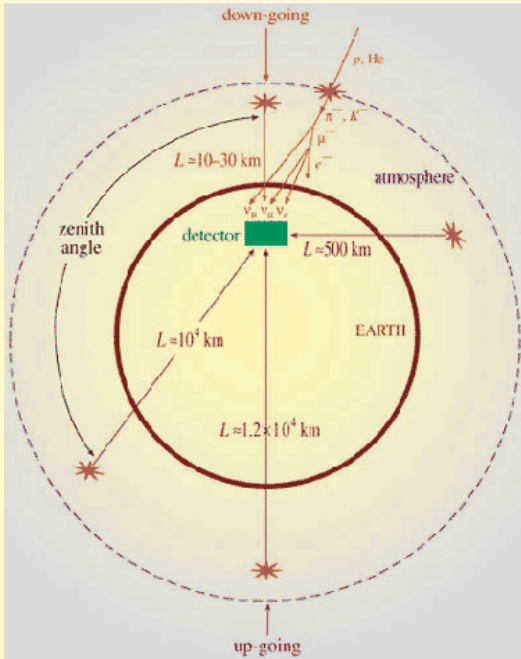
ν_e content of ν_3 unknown [but $< \text{few}\%$]

$$\delta m^2 \simeq 8.0 \times 10^{-5} \text{ eV}^2 \quad (\text{"solar" splitting})$$

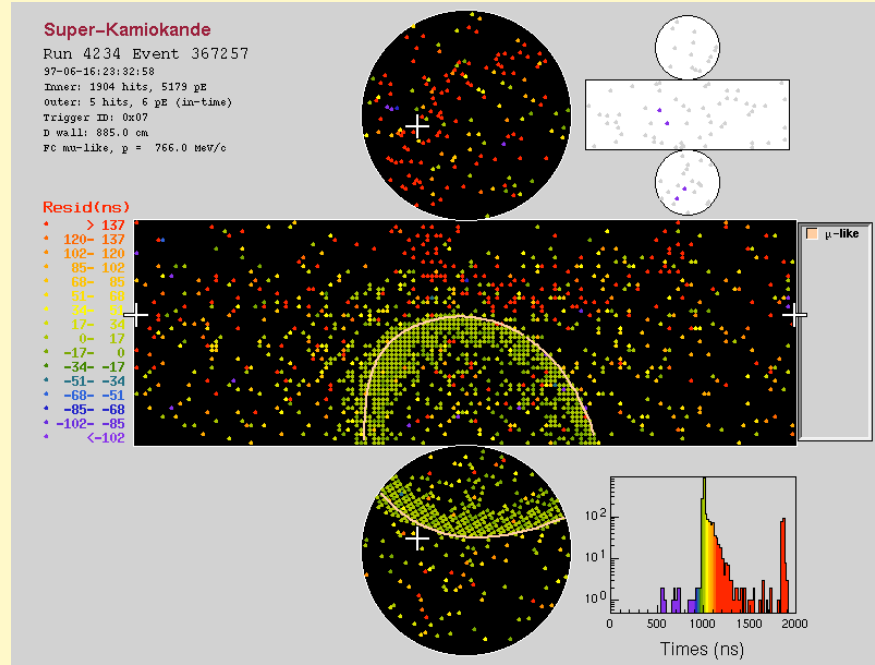
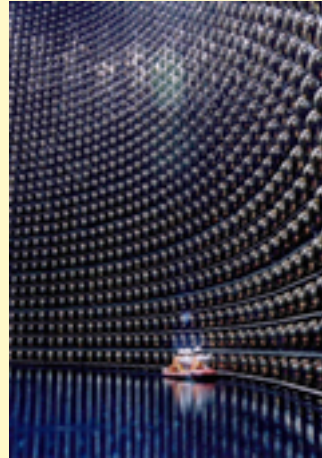
$$\Delta m^2 \simeq 2.4 \times 10^{-3} \text{ eV}^2 \quad (\text{"atmospheric" splitting})$$

**Constraints on $(\Delta m^2, \theta_{23}, \theta_{13})$
from SK + K2K + CHOOZ**

Figure 4



Super-Kamiokande



ν_e induced events: ~ as expected

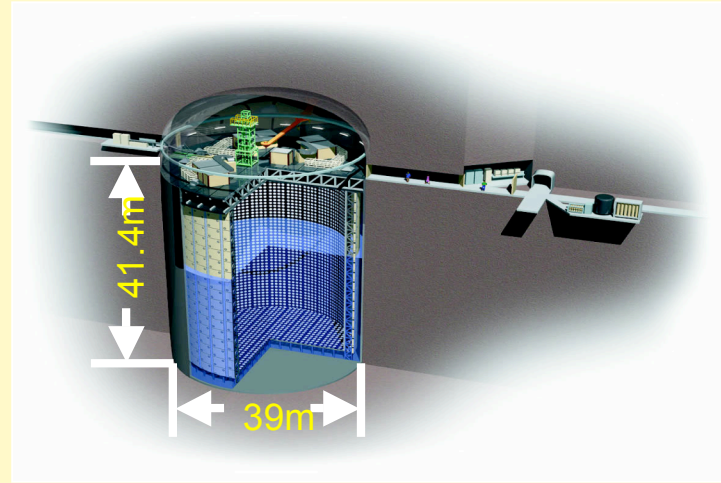
ν_μ induced events: deficit from below

Channel $\nu_\mu \rightarrow \nu_e$? No (or subdominant)

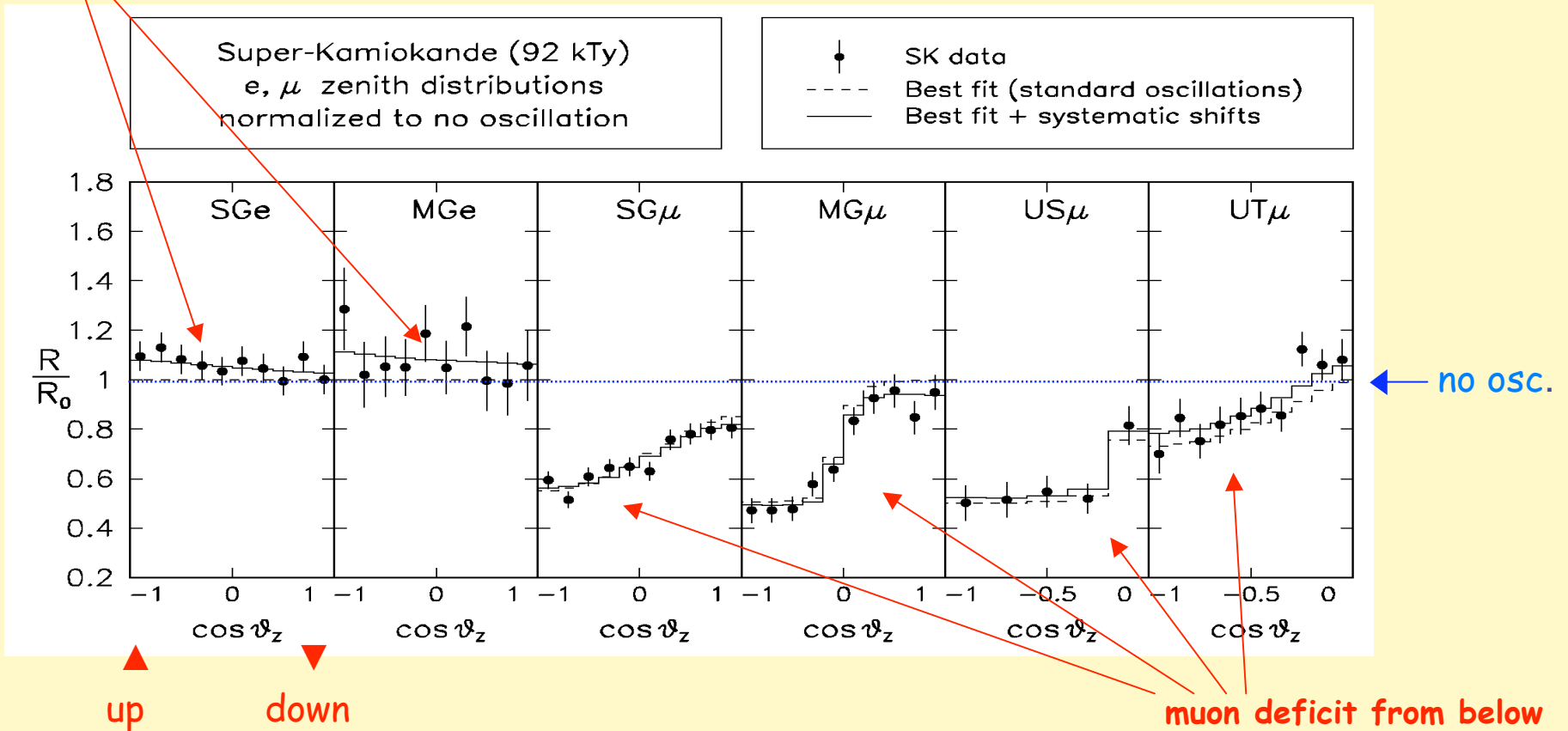
Channel $\nu_\mu \rightarrow \nu_\tau$? Yes (dominant)

Atmospheric neutrinos: Super-Kamiokande

- S_{Ge}** Sub-GeV electrons
- M_{Ge}** Multi-GeV electrons
- S_{Gμ}** Sub-GeV muons
- M_{Gμ}** Multi-GeV muons
- U_{Sμ}** Upward Stopping muons
- U_{Tμ}** Upward Through-going muons



electrons ~OK



Super-Kamiokande atmospheric ν

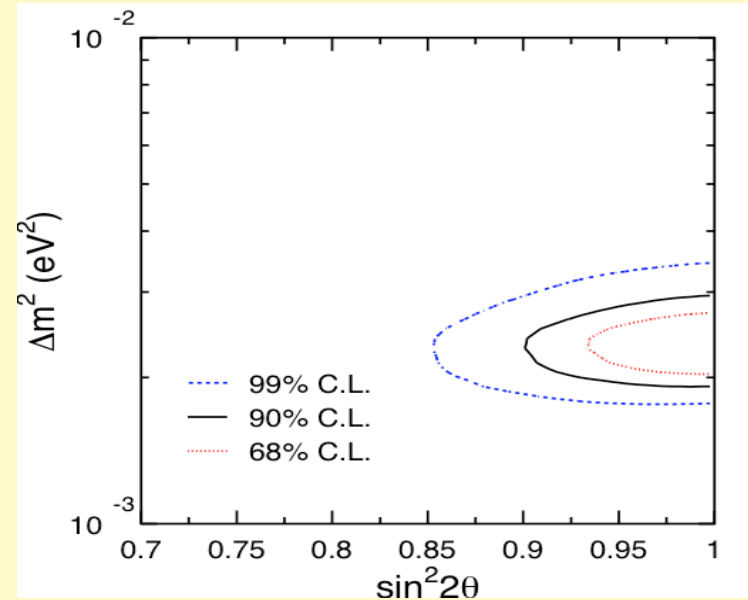
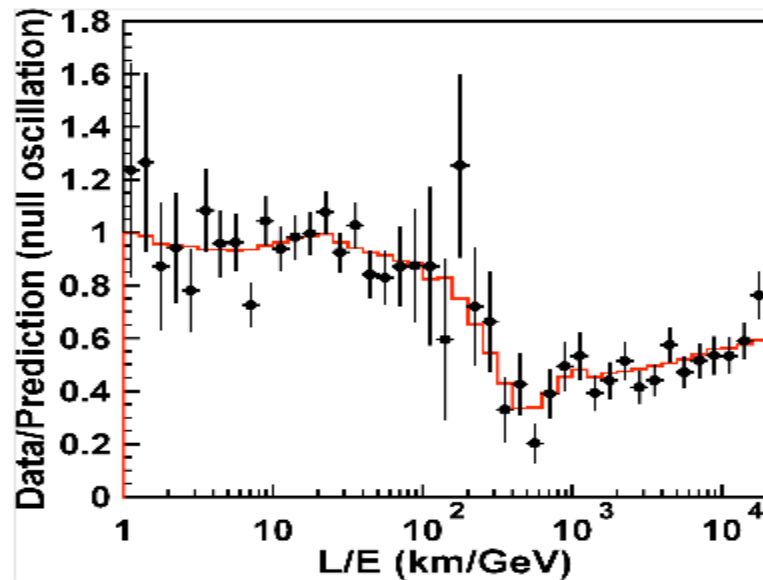
$$E_\nu \sim 10^{-1} - 10^3 \text{ GeV} \quad L \sim 10 - 10^4 \text{ km} \quad (\text{large } L/E \text{ range})$$

For $\theta_{13} \sim 0$ and $\delta m^2 \sim 0$, a very simple formula fits all SK data (+ MACRO & Soudan2)

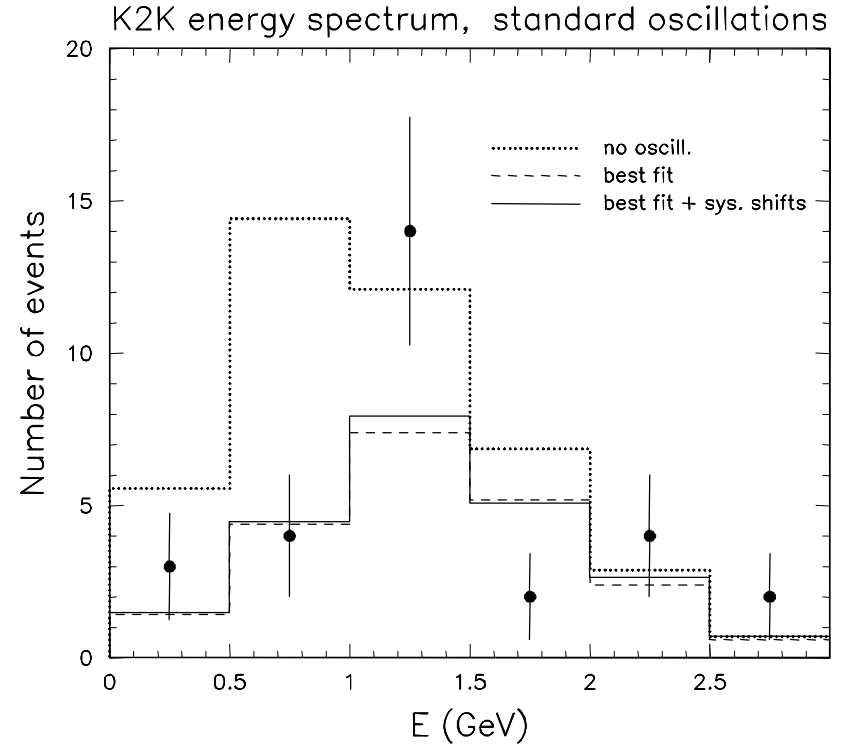
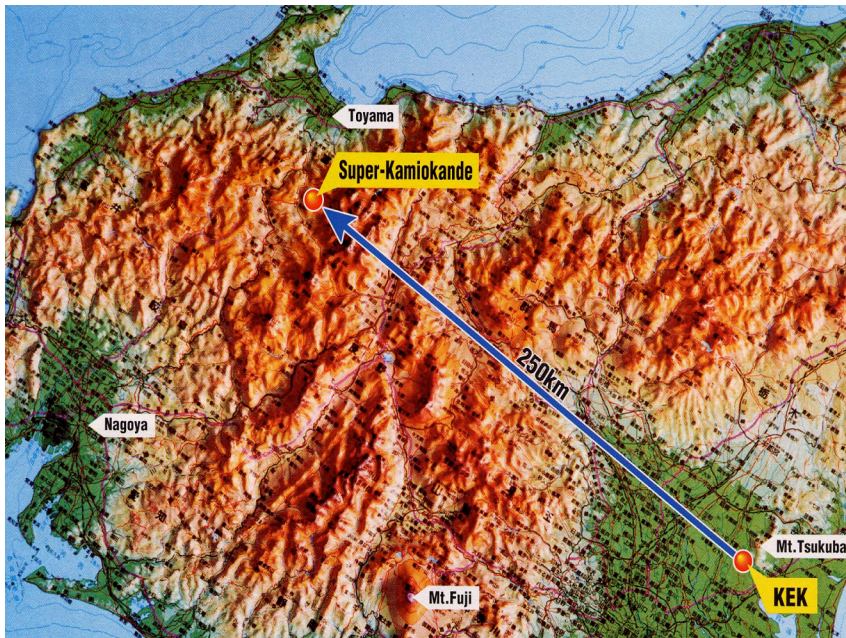
$$P(\nu_\mu \rightarrow \nu_\tau) \simeq \sin^2 2\theta_{23} \sin^2 \left(1.27 \frac{\Delta m^2 (\text{eV}^2) L (\text{km})}{E (\text{GeV})} \right)$$

1st oscillation dip still visible despite large L & E smearing

Strong constraints on the parameters (Δm^2 , θ_{23})



First-generation LBL accelerator experiment: KEK-to-Kamioka (K2K)



Aimed at testing disappearance of
accelerator ν_μ in the same range
probed by atmospheric ν :

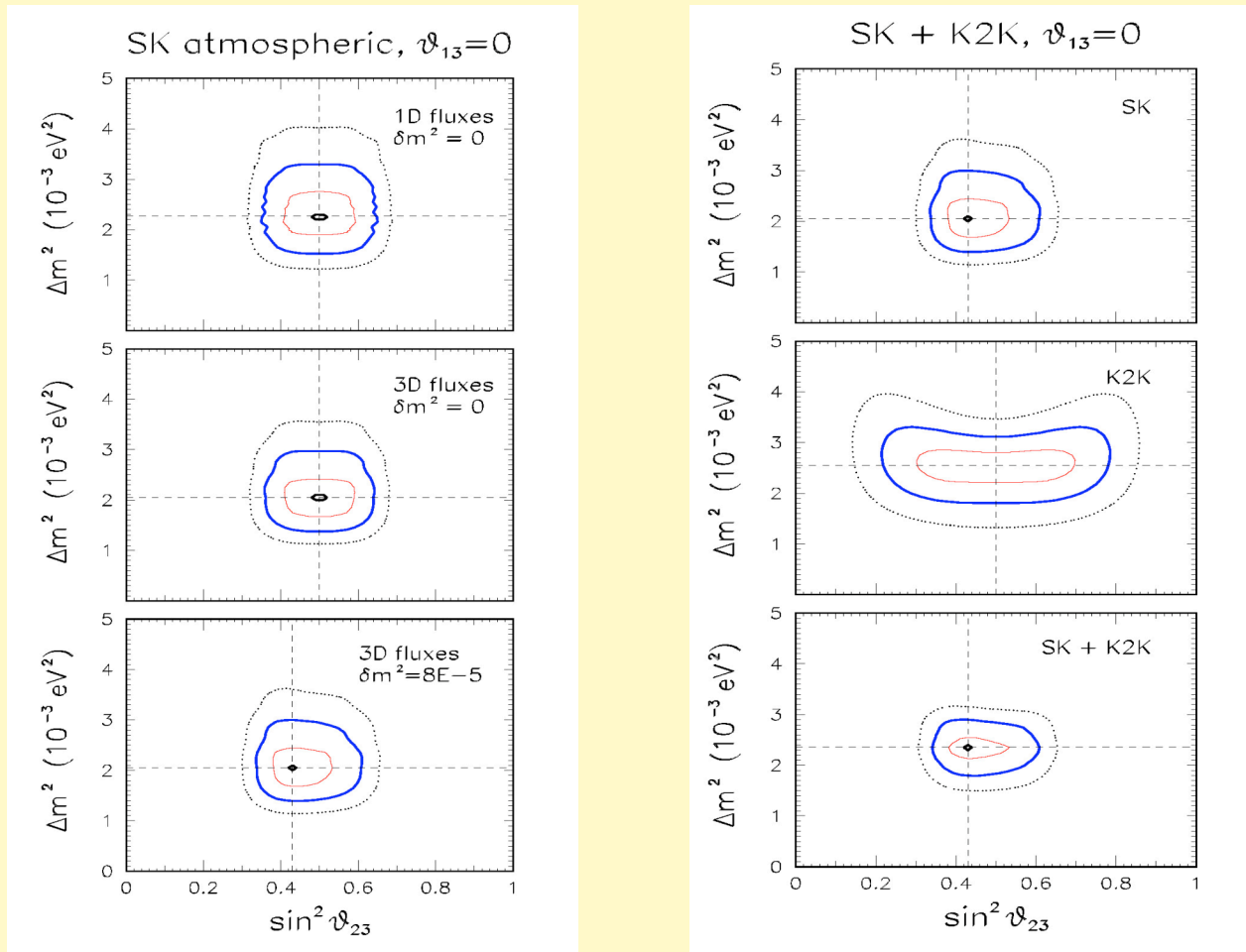
$$(L/E)_{K2K} \sim (250 \text{ km}/1.3 \text{ GeV}) \sim (L/E)_{ATM}$$

**2002: muon disappearance
observed at >99% C.L.**

No electron appearance.

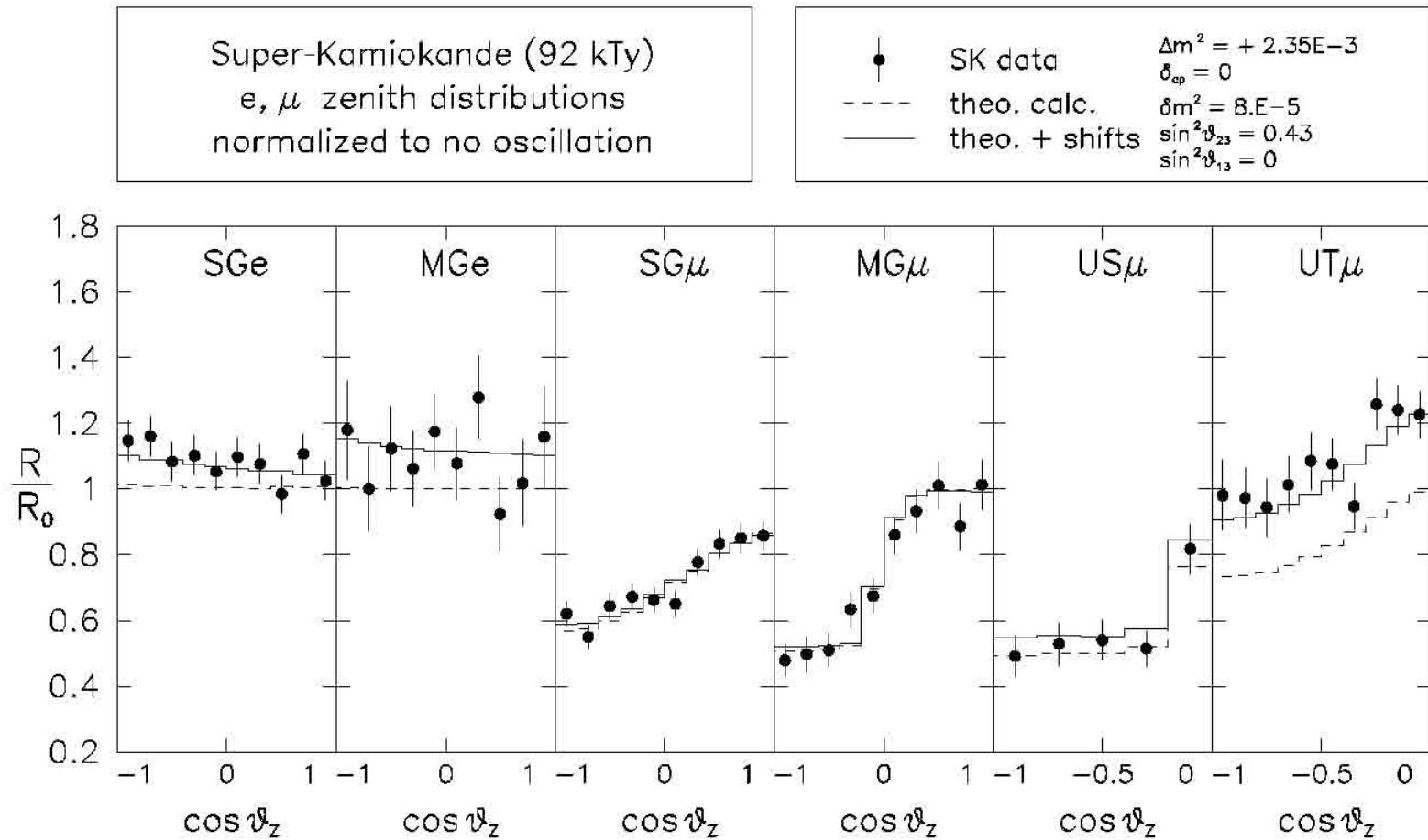
Atmospheric ν oscillation evidence robust & confirmed with lab- ν in K2K

Many interesting details depend on theoretical input & subleading effects



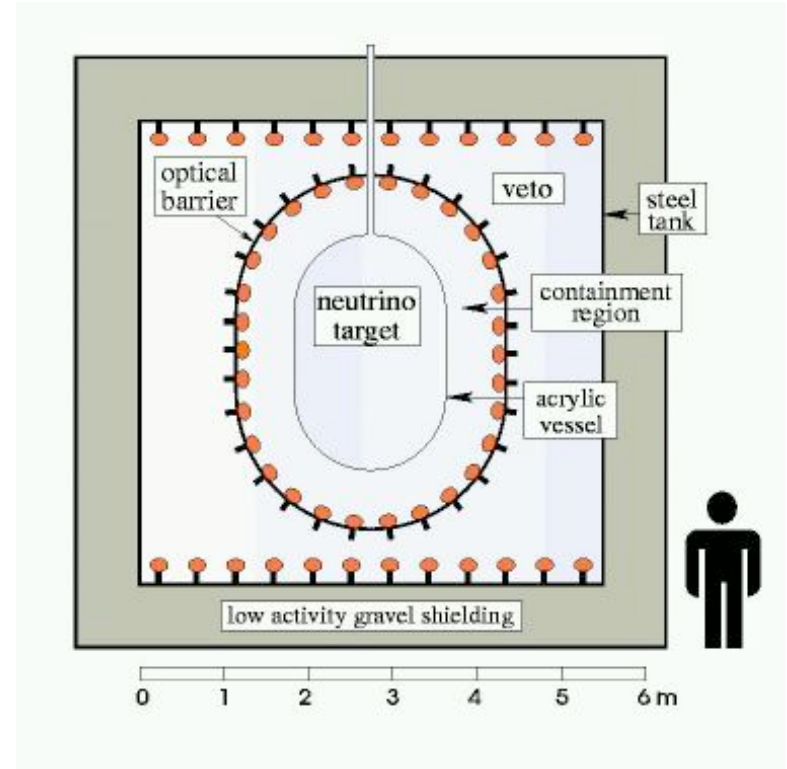
Contours at 1, 2, 3 σ (1 dof). Note linear scale for Δm^2 and $\sin^2 \vartheta_{23}$, with 2nd octant of ϑ_{23} unfolded

... more about subleading effects (induced by "solar parameters")
vs systematic errors
in the Super-Kamiokande zenith distributions



The CHOOZ reactor experiment and θ_{13}

- Searched for disappearance of reactor ν_e ($E \sim \text{few MeV}$) at distance $L = 1 \text{ km}$
- L/E range comparable to atmospheric ν
→ probe the same Δm^2
- No disappearance signal was found (1998)
→ **Exclusion plot in $(\Delta m^2, \theta_{13})$ plane**
- Results also confirmed by later reactor experiment (Palo Verde)

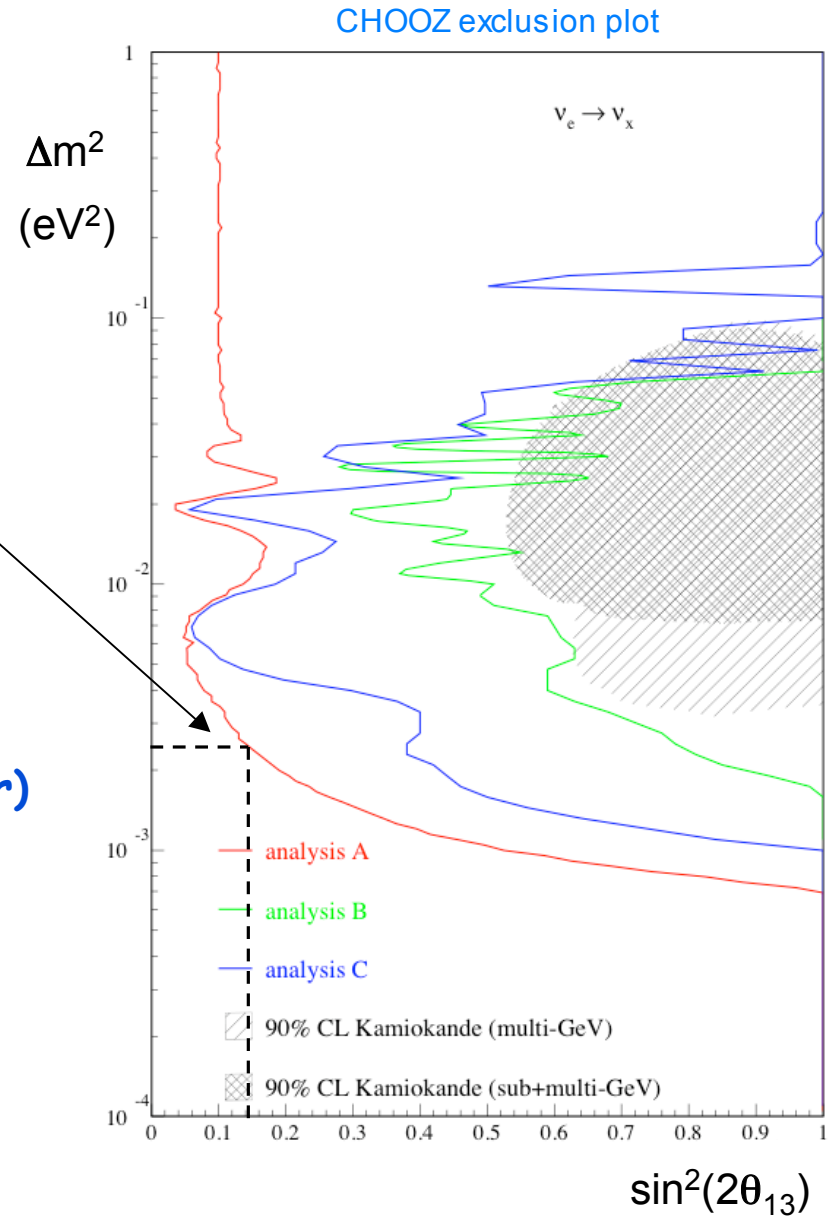


A crucial and beautiful "small-scale" experiment

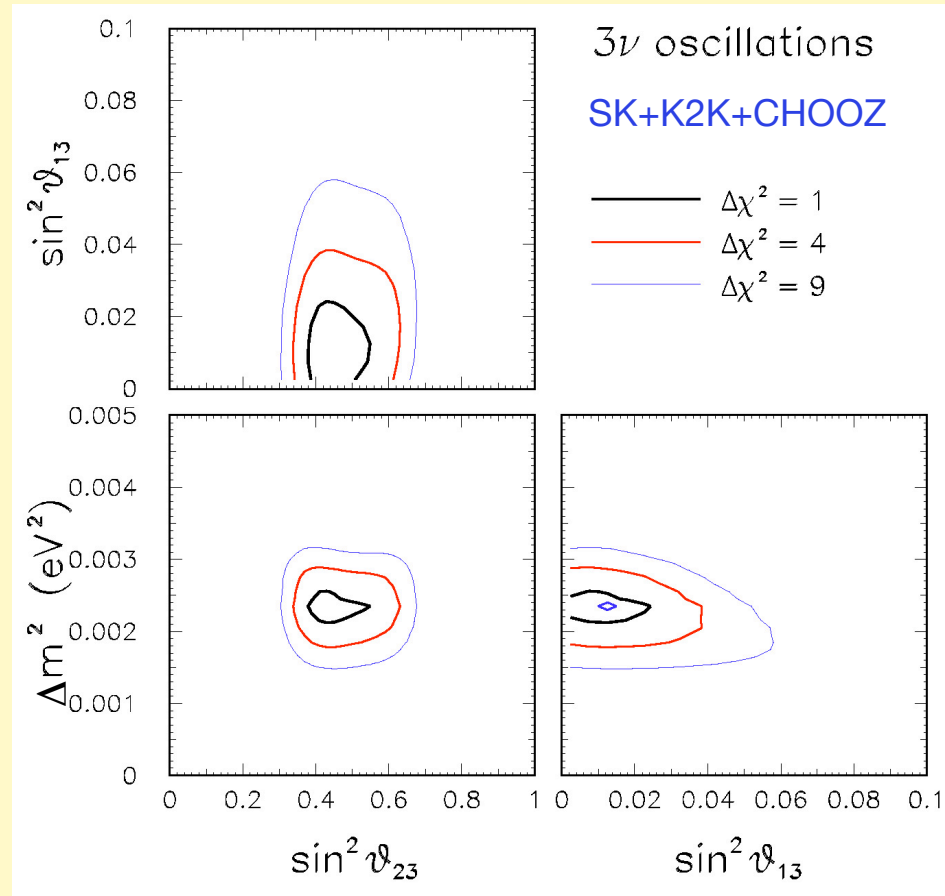
The CHOOZ reactor experiment and θ_{13}

- For any value of Δm^2 in the SK+K2K range, get stringent upper bound on θ_{13}

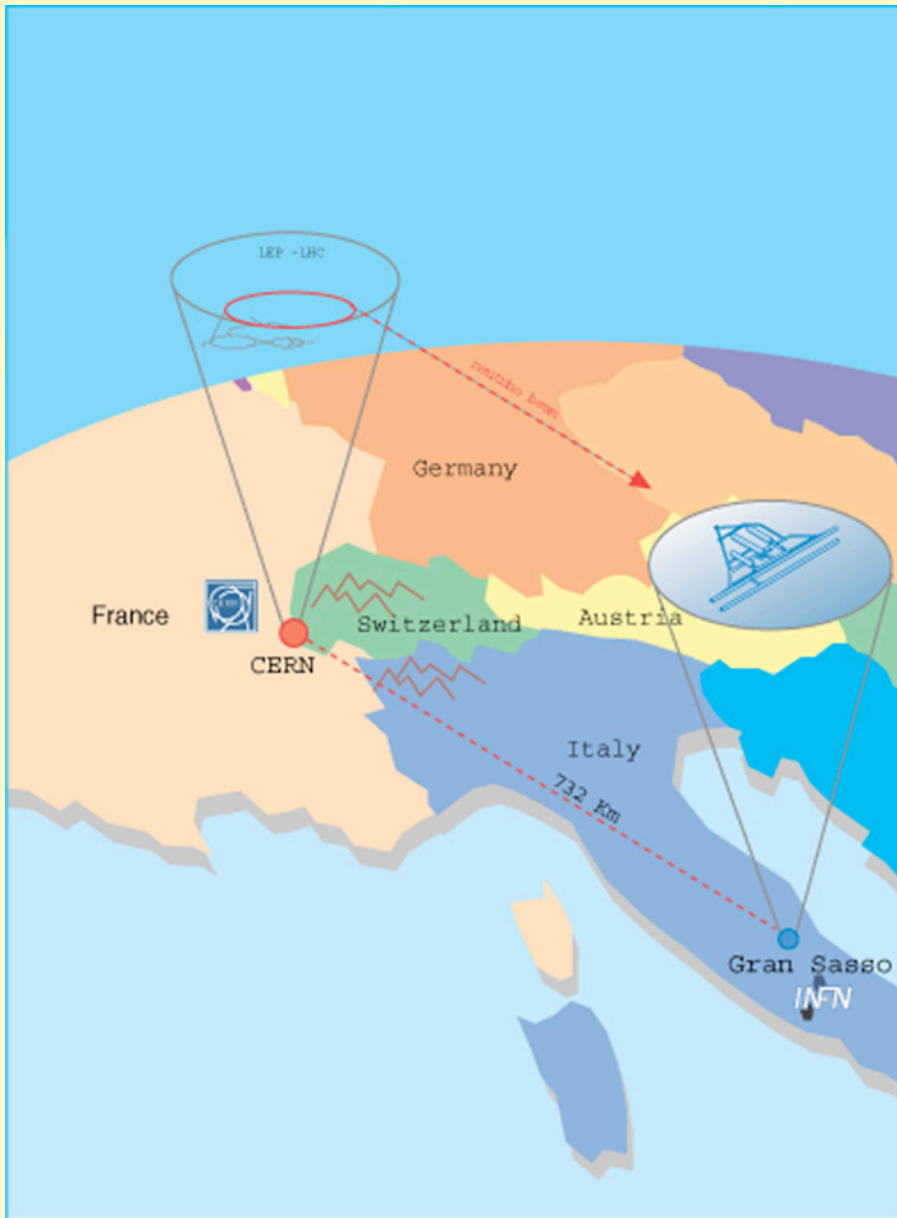
Feverish world-wide activity to make one -or more- new reactor experiment with higher θ_{13} sensitivity (=smaller error)



At the Δm^2 scale of SK+K2K, nonobservation of $\nu_e \rightarrow \nu_e$ in the CHOOZ reactor experiment sets upper bounds $\sin^2 \theta_{13} < \text{few } \%$



Growing literature & interest in subleading effects due to θ_{13} , δm^2 , $\text{sign}(\Delta m^2)$, δ
But need very significant error reduction to probe them
A challenge for future high-statistics experiments



Missing piece in puzzle:

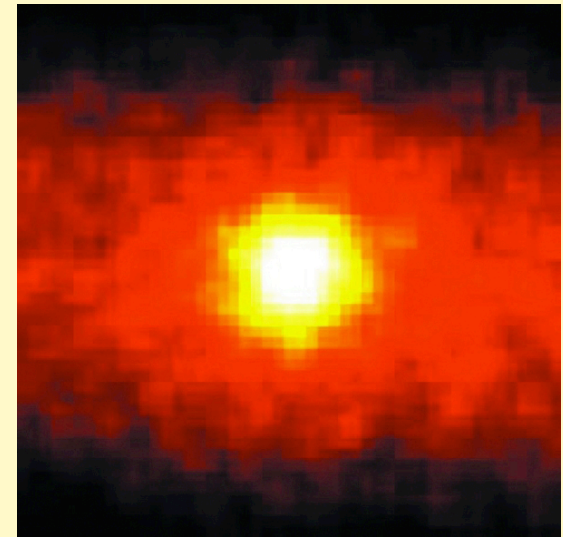
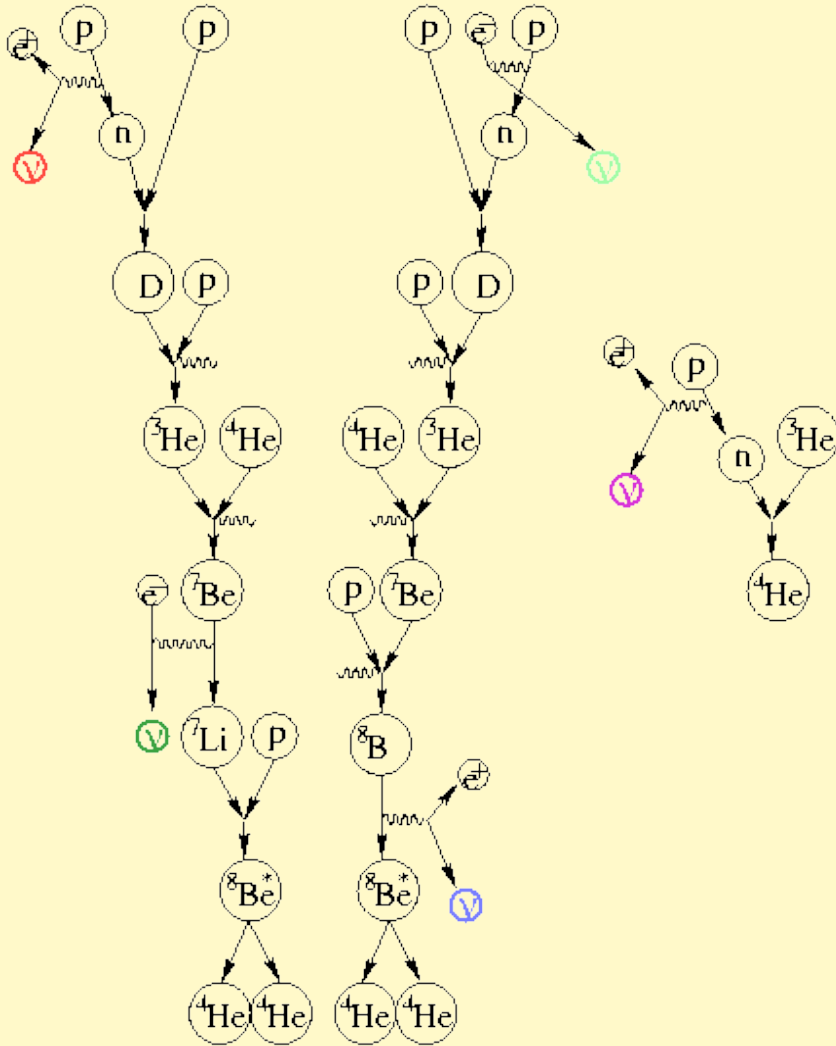
ν_τ appearance

(only 2-sigma hint in Super-K)

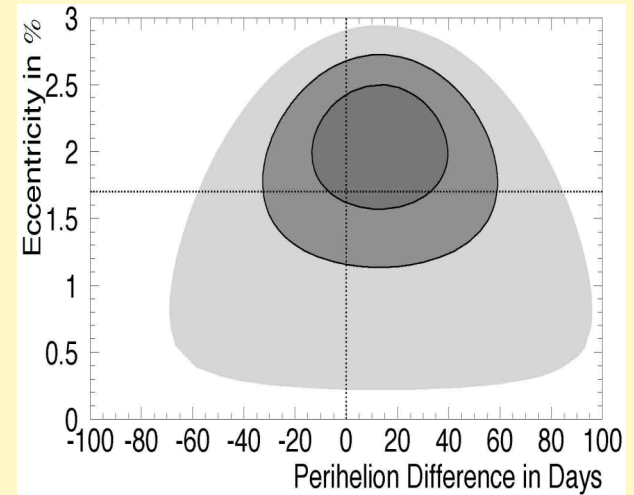
Will be studied at
 Laboratori Nazionali
 del Gran Sasso
(OPERA, ICARUS)
 with
 CERN neutrino beam

**Constraints on $(\delta m^2, \theta_{12}, \theta_{13})$
from solar ν + KamLAND**

Solar neutrinos (ν_e)

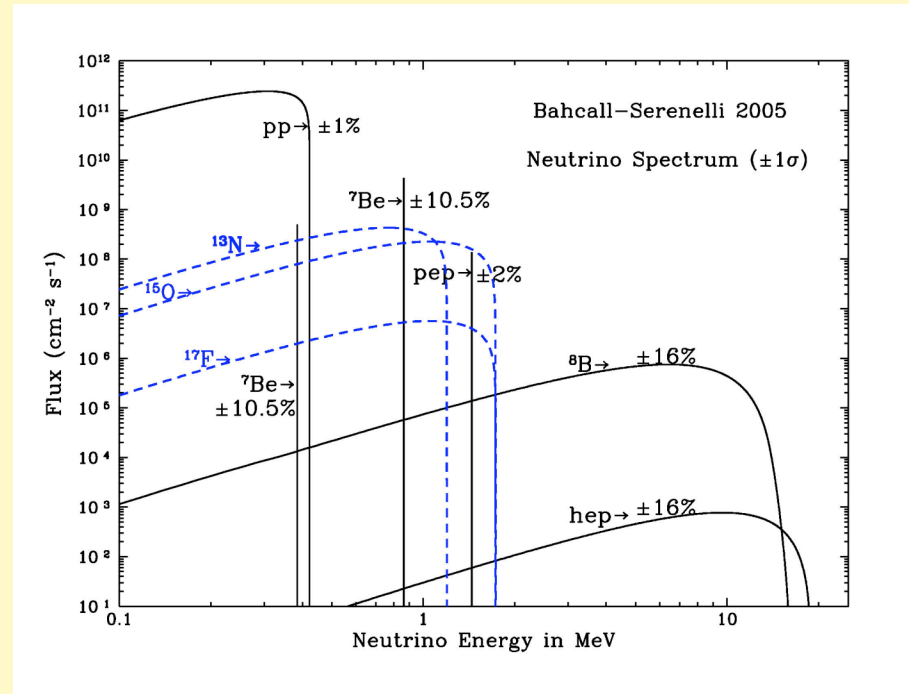


The Sun seen with neutrinos (SK)

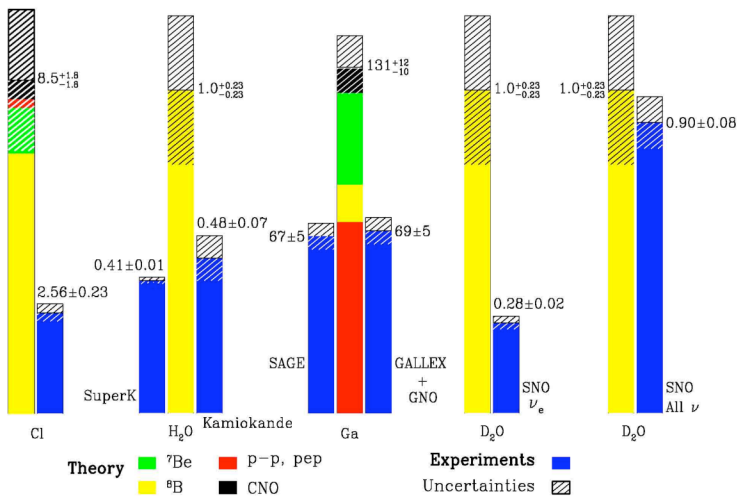


Earth orbit from solar ν (SK)

Standard Solar Model: neutrino energy spectrum...

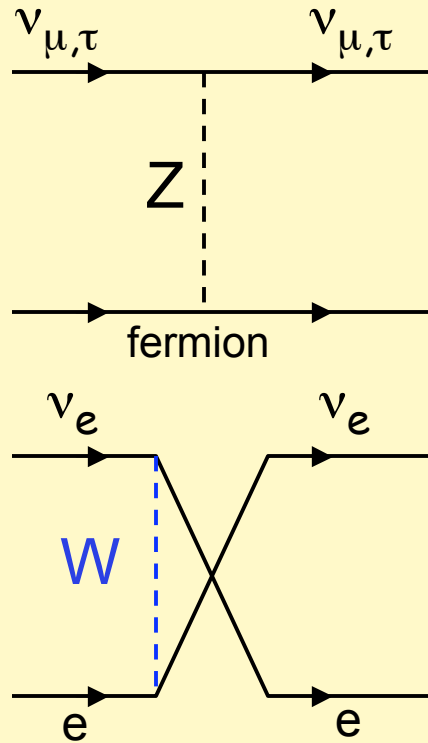


Total Rates: Standard Model vs. Experiment
Bahcall-Pinsonneault 2004



... and experimental deficit

Reminder - Solar $\nu_e \rightarrow \nu_{e,\mu,\tau}$ vs atmospheric $\nu_\mu \rightarrow \nu_\tau$: matter (MSW) effect



Atmospheric ν_μ and ν_τ feel background fermions in the same way (through NC); no relative phase change (\sim vacuum-like)

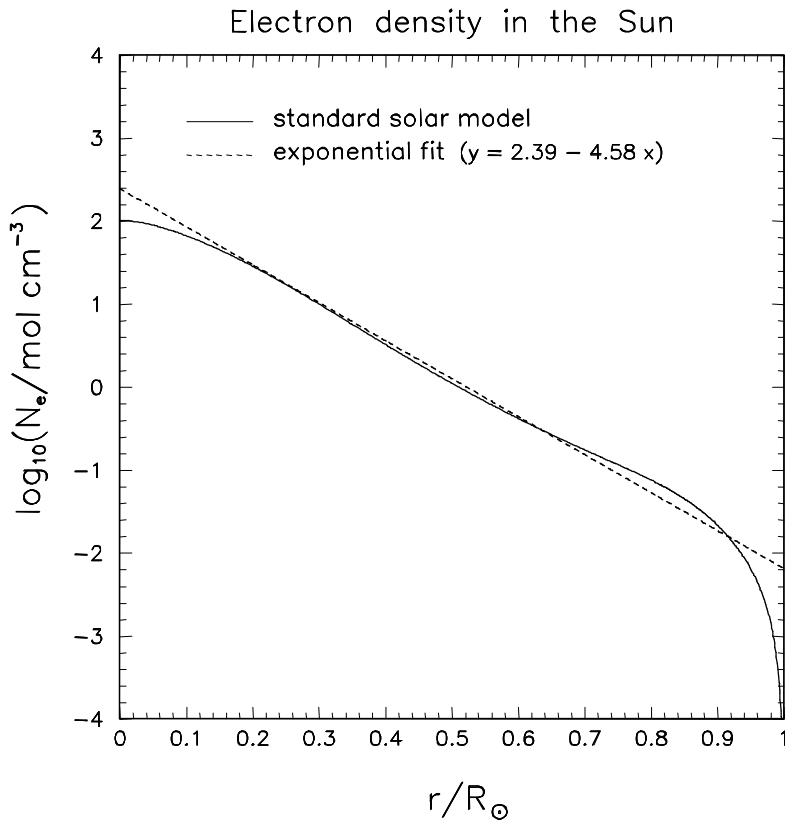
But ν_e , in addition to NC, have CC interac. with background electrons (density N_e).
Energy difference: $V = \sqrt{2} G_F N_e$

Solar ν analysis must account for MSW effects in the Sun and in the Earth
 (Earth matter effects negligible for KamLAND reactor neutrinos)
Solar+KamLAND combination provide evidence for V_{sun} (not yet for V_{earth})

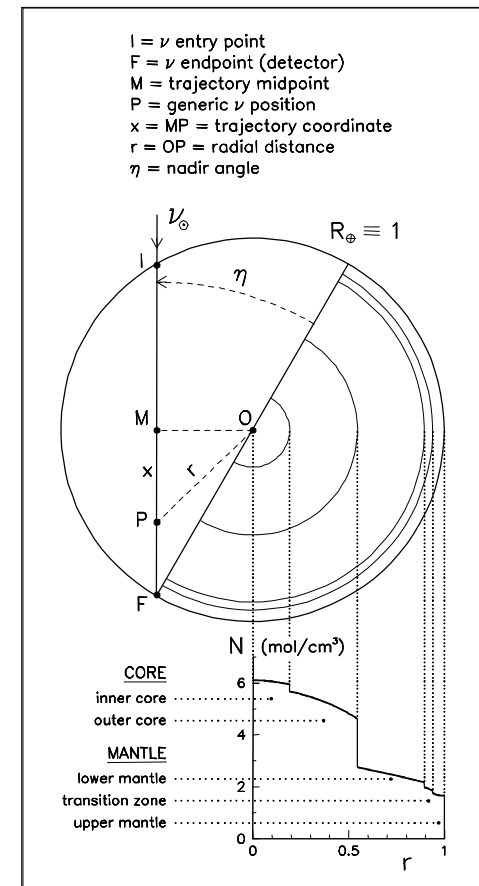
Reminder - Solar neutrinos: Oscillation analysis

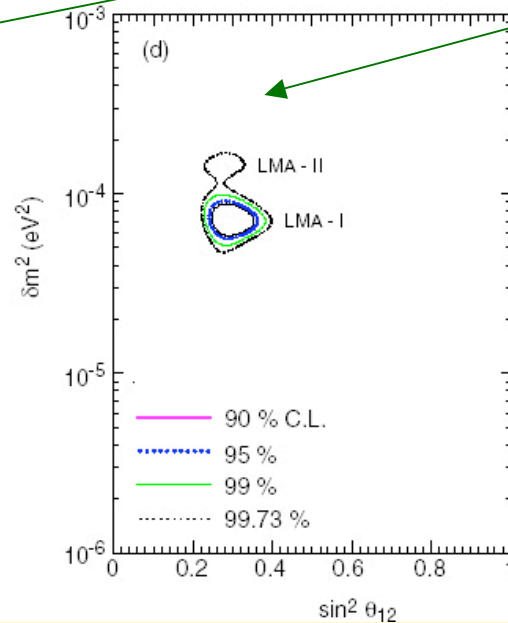
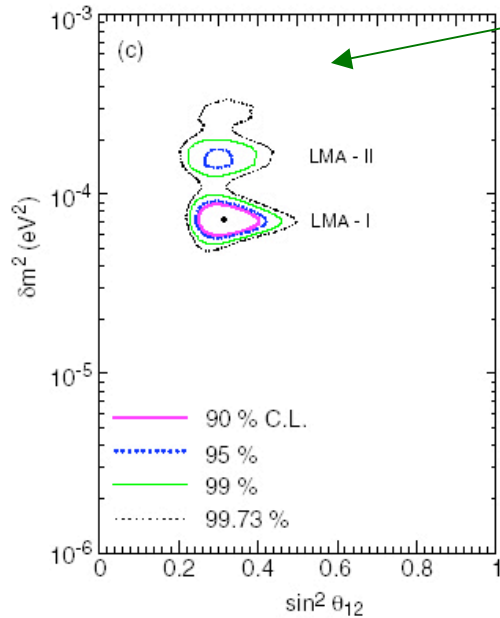
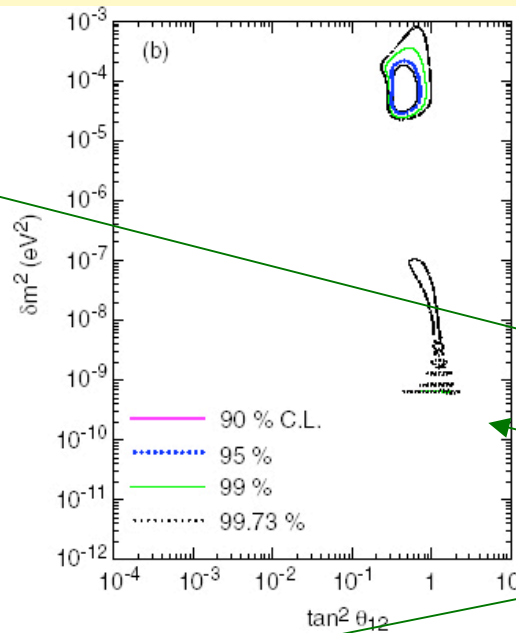
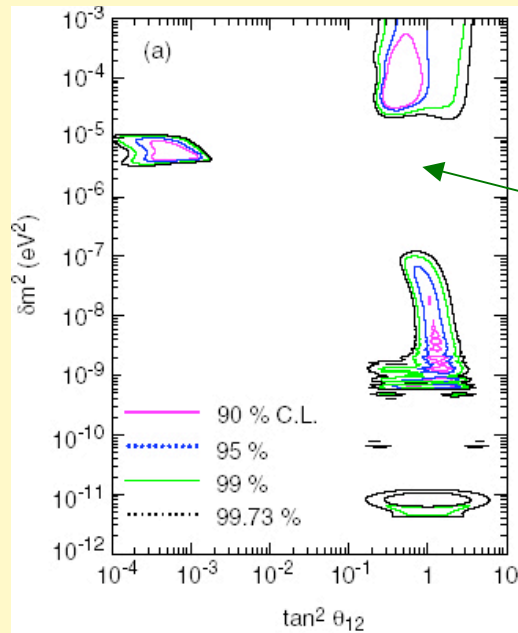
- **Leading parameters:** $(\delta m^2, \theta_{12})$
- **MSW effects must be carefully taken into account**

→ need electron density profile in the **Sun** (always) ...



... and in the **Earth**
(for night-time trajectories)





Dramatic reduction of the
 $(\delta m^2, \theta_{12})$ param. space in
2001-2003
 (note change of scales)

Cl+Ga+SK (2001)

+SNO-I (2001-2002)

+KamLAND-I (2002)

+SNO-II (2003)

(+ confirmation of solar model)

Direct proof of solar $\nu_e \rightarrow \nu_{\mu,\tau}$
 in SNO through comparison of

$$\text{CC} : \quad \nu_e + d \rightarrow p + p + e$$

$$\text{NC} : \nu_{e,\mu,\tau} + d \rightarrow p + n + \nu_{e,\mu,\tau}$$

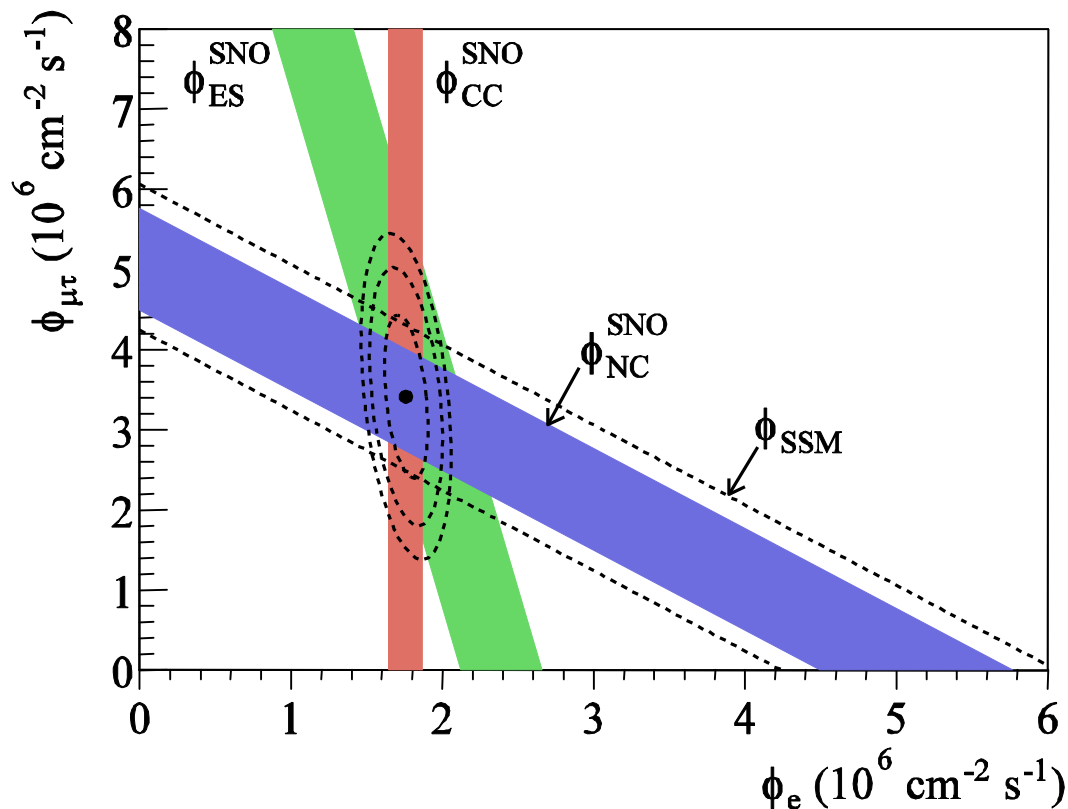
$$\text{ES} : \nu_{e,\mu,\tau} + e \rightarrow e + \nu_{e,\mu,\tau}$$

Solar neutrinos: The 1st SNO breakthrough (2002)

- Solar neutrino deficit in Cl, Ga, Č expt.: model-independent proof desirable
- Proof provided beyond any doubt by CC/NC event ratio in SNO:

$$R = \frac{R_{CC}}{R_{NC}} = \frac{\Phi(\nu_e)}{\Phi(\nu_e) + \Phi(\nu_\mu) + \Phi(\nu_\tau)} = P(\nu_e \rightarrow \nu_e) \text{ independently of SSM}$$

- $R \sim 1/3$ was found \rightarrow solar ν_e must oscillate into $\nu_{\mu\tau}$



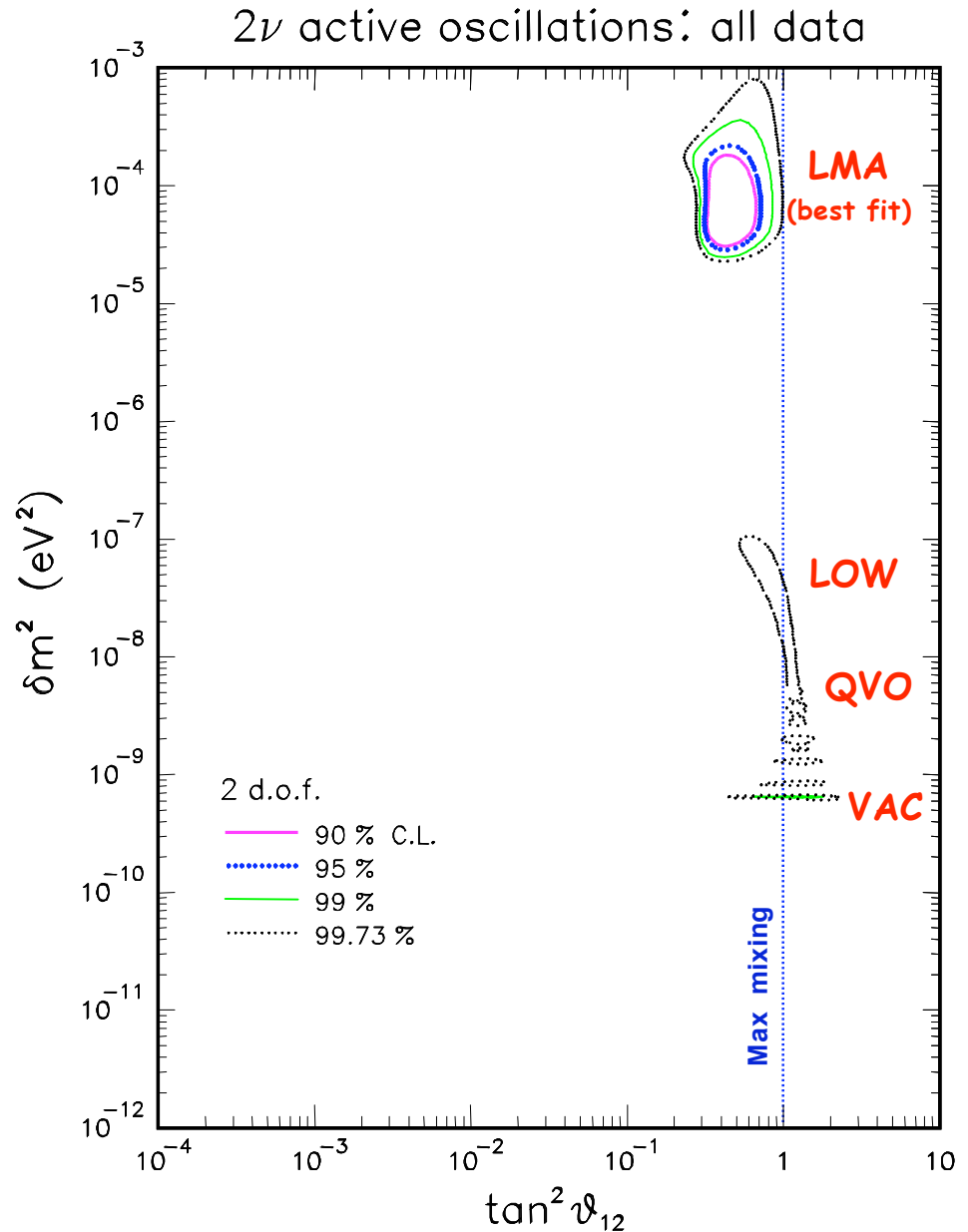
Solar neutrinos: Oscillation analysis (as of summer 2002)

All experiments
combined (summer '02)

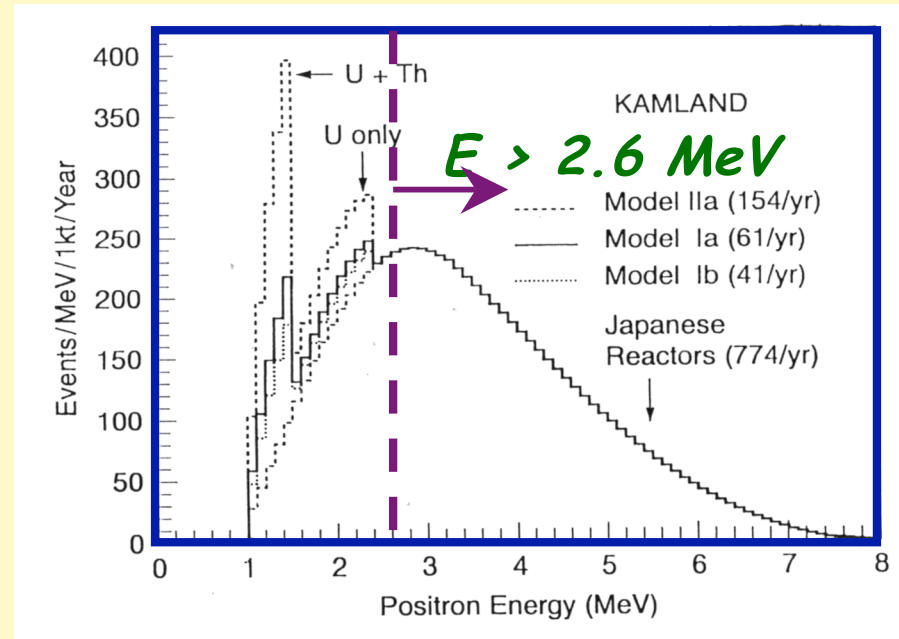
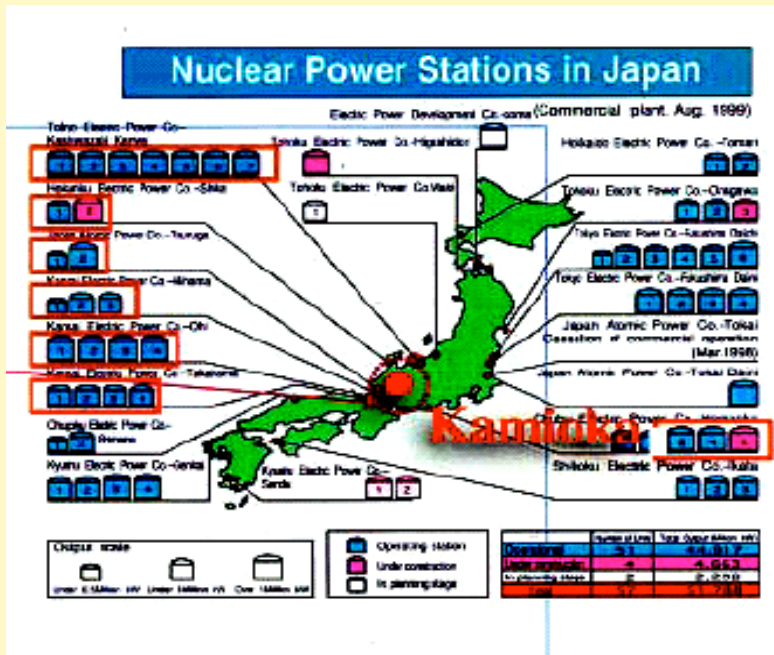
(90, 95, 99, 99.73% C.L.)

Jargon:

- LMA** Large Mixing Angle
- LOW** Low δm^2
- QVO** Quasi-vacuum oscillations
- VAC** Vacuum oscillations
- (SMA** Small mixing angle, †2001)



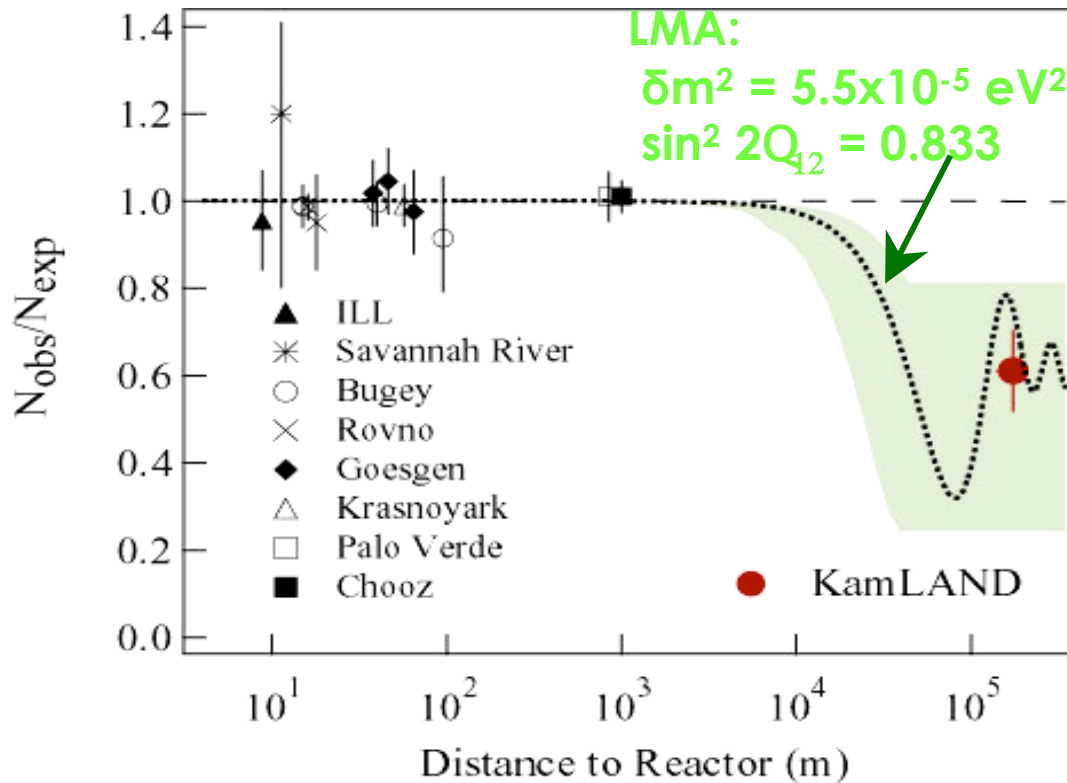
Man-made reactor neutrinos: KamLAND



- Average distance: $\sim 180 \text{ km}$ (two orders of magnitude greater than CHOOZ)
- CHOOZ was mainly sensitive to $\Delta m^2 \sim \text{few} \times 10^{-3} \text{ eV}^2$
- KamLAND is mainly sensitive to $\delta m^2 \sim \text{few} \times 10^{-5} \text{ eV}^2$ (LMA range!)
- KamLAND also opens fundamental new field of geoneutrino physics

KamLAND breakthrough (December 2002)

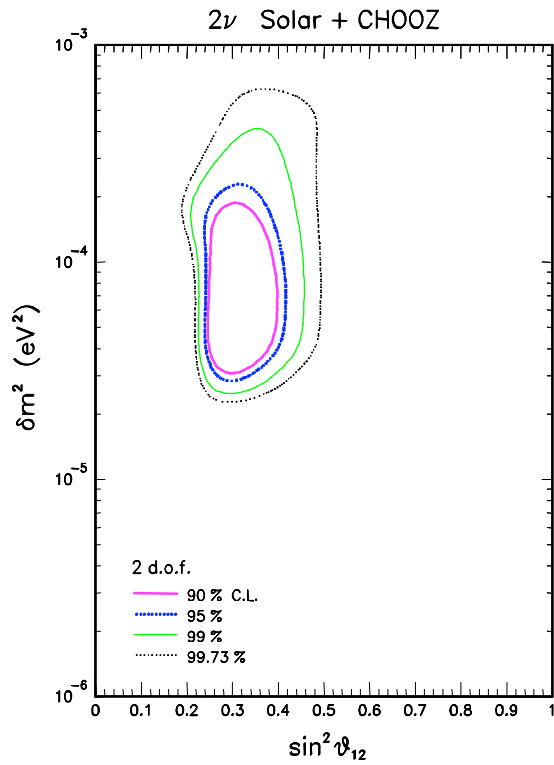
Disappearance of reactor ν_e measured



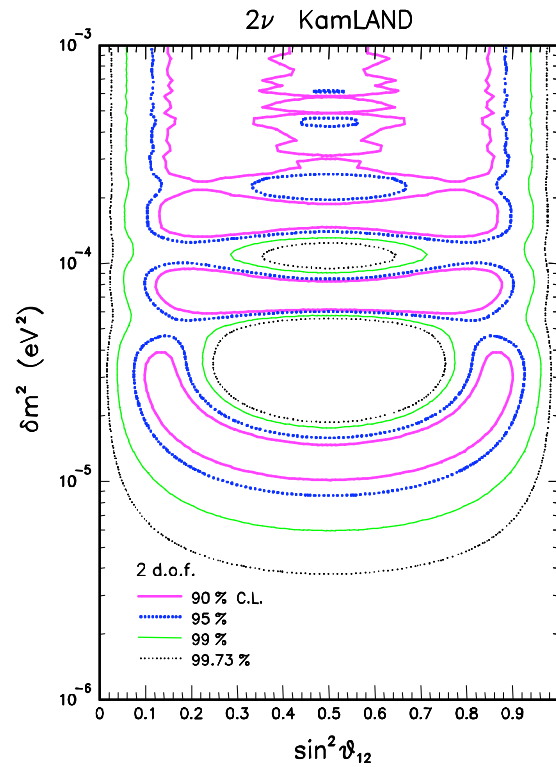
LMA solution confirmed; all others ruled out

KamLAND impact on $(\delta m^2, \theta_{12})$ parameter space

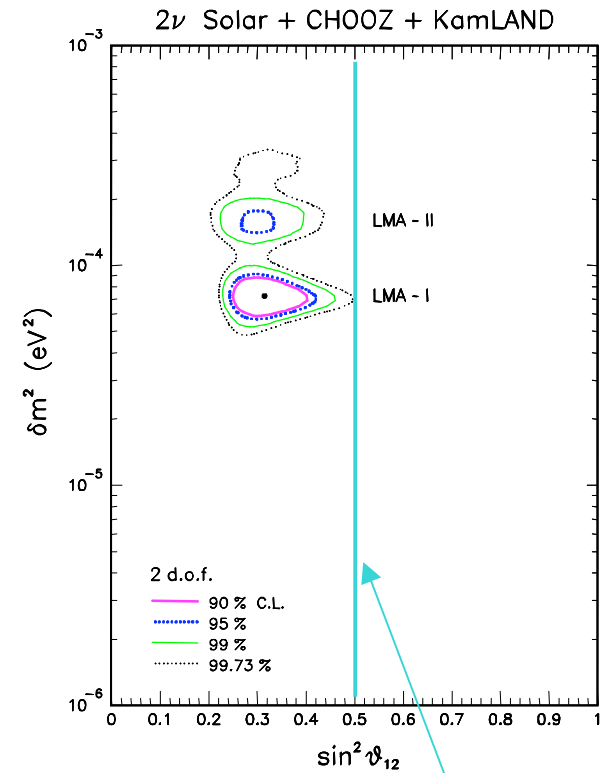
...before KamLAND



KamLAND 2002

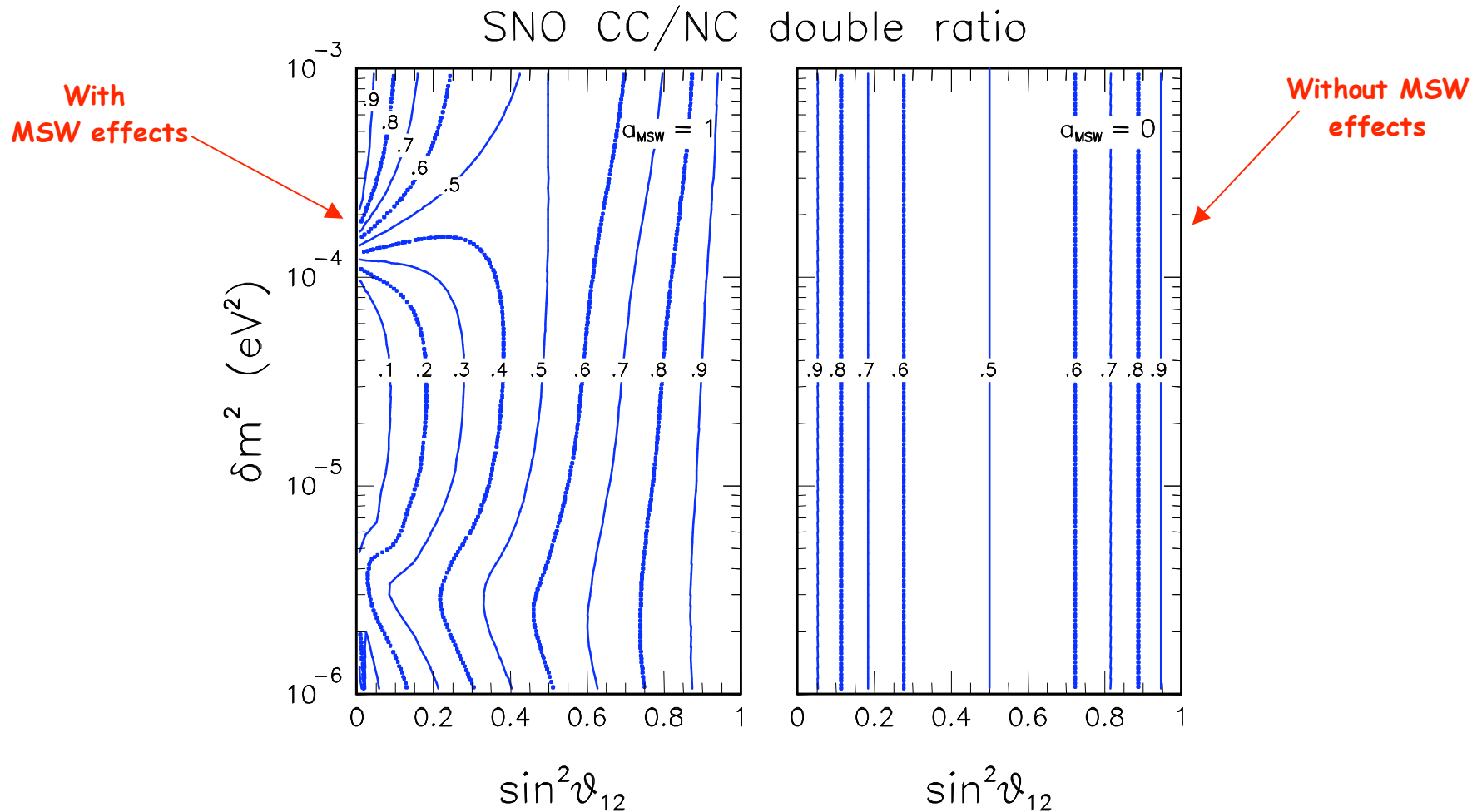


...after KamLAND



Note:
 Maximal θ_{12} mixing
 not ruled out in 2002

Why should we care about (non)maximal θ_{12}

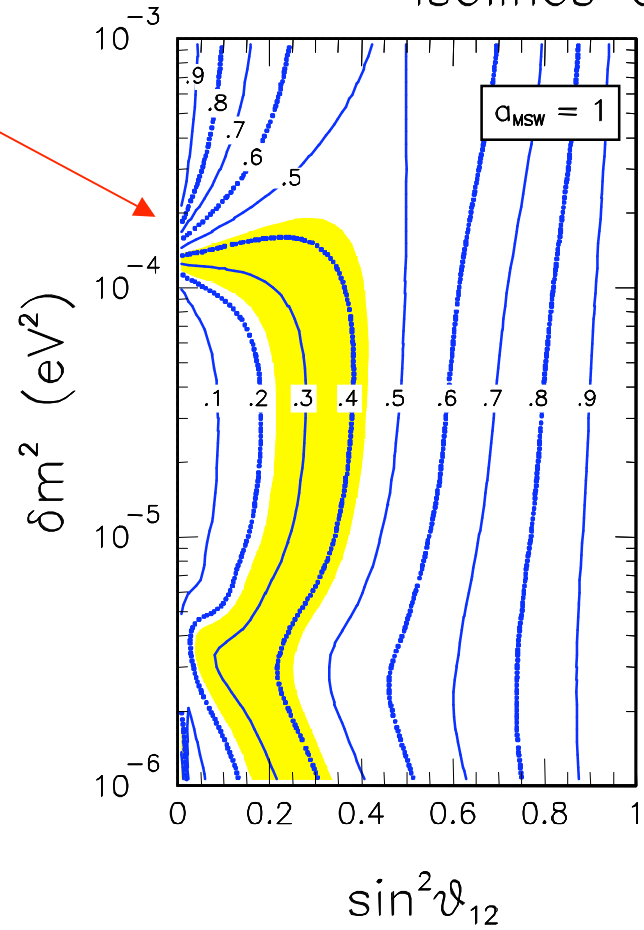


In LMA, SNO CC/NC can be < 0.5 only WITH matter effects AND mixing $< \pi/4$

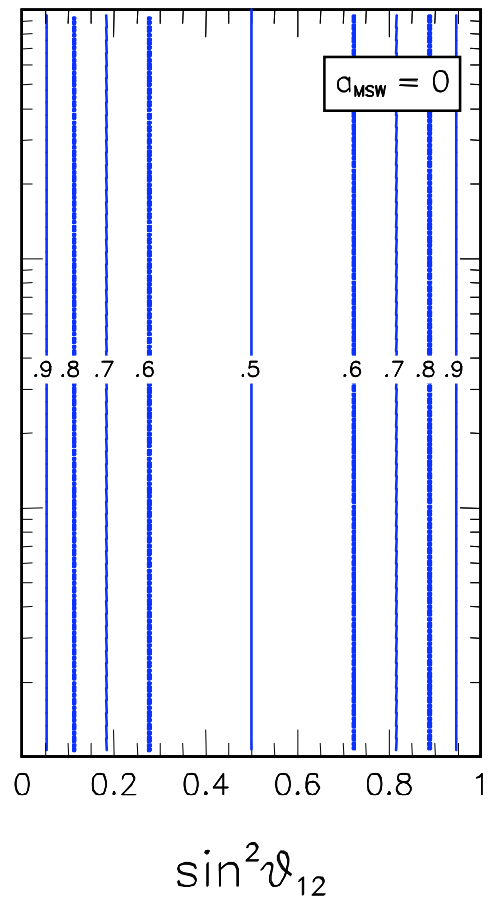
The 2nd SNO breakthrough (September 2003): maximal mixing ruled out

Isolines of $\langle P_{ee} \rangle$

With MSW effects



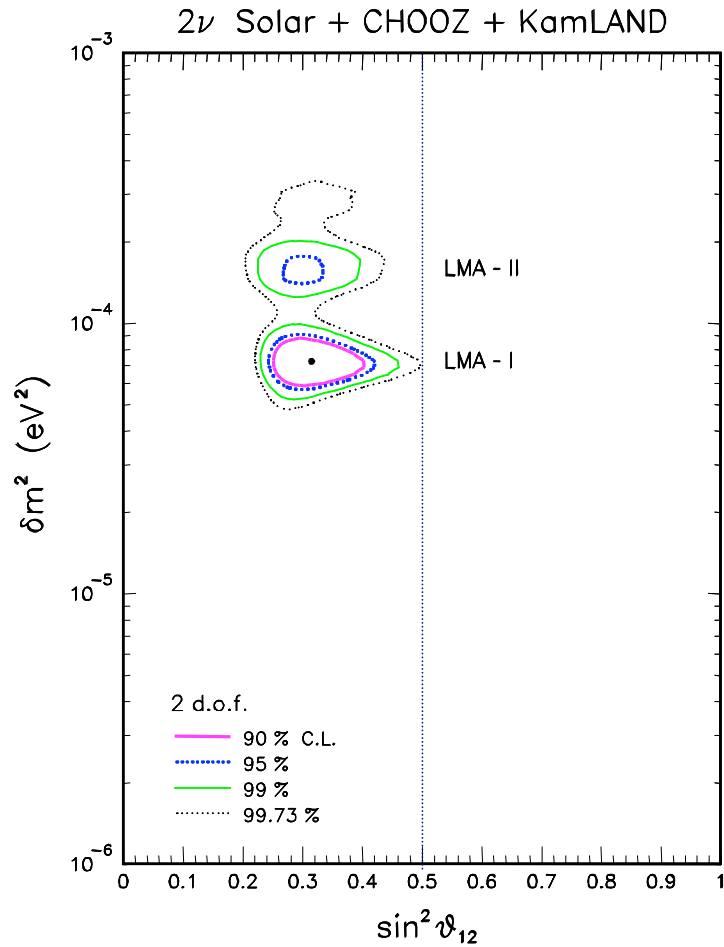
~~Without MSW effects~~



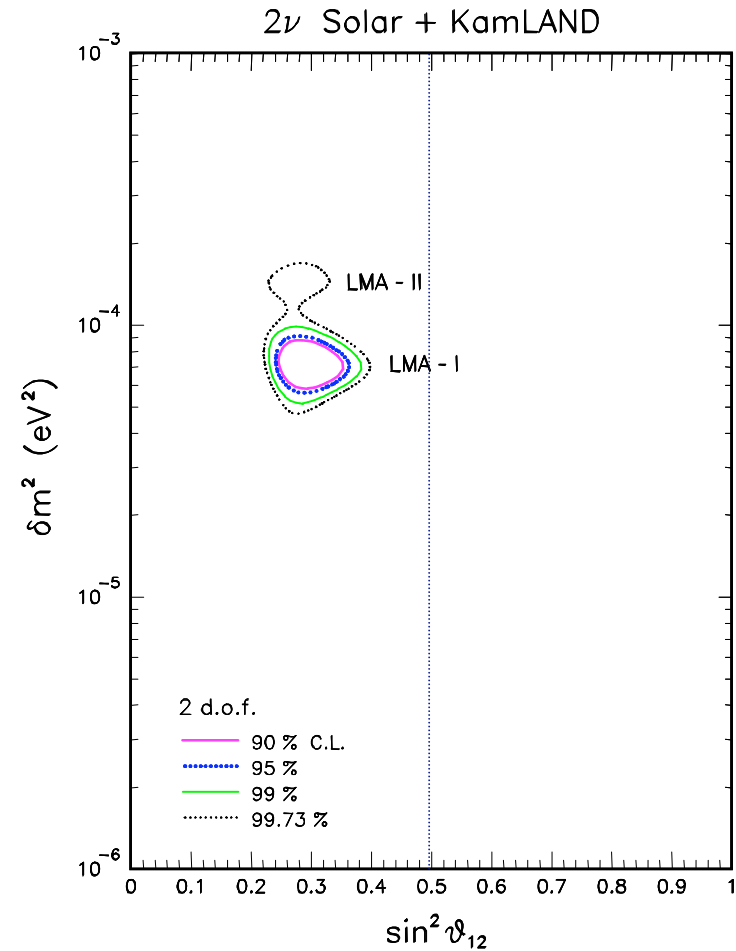
Compelling evidence for matter effects in the Sun

LMA analysis (as of september 2003)

Still: LMA-I vs LMA-II ambiguity

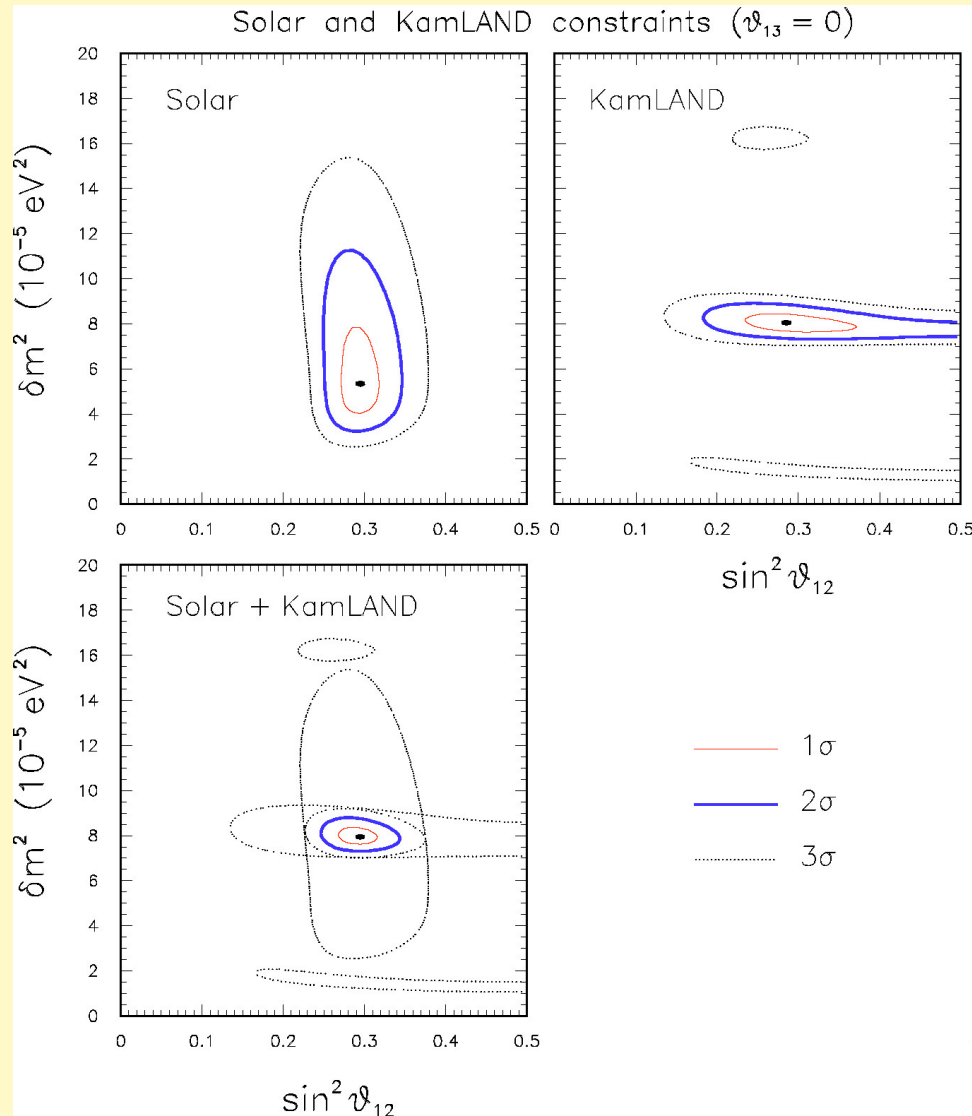


Before SNO 2003

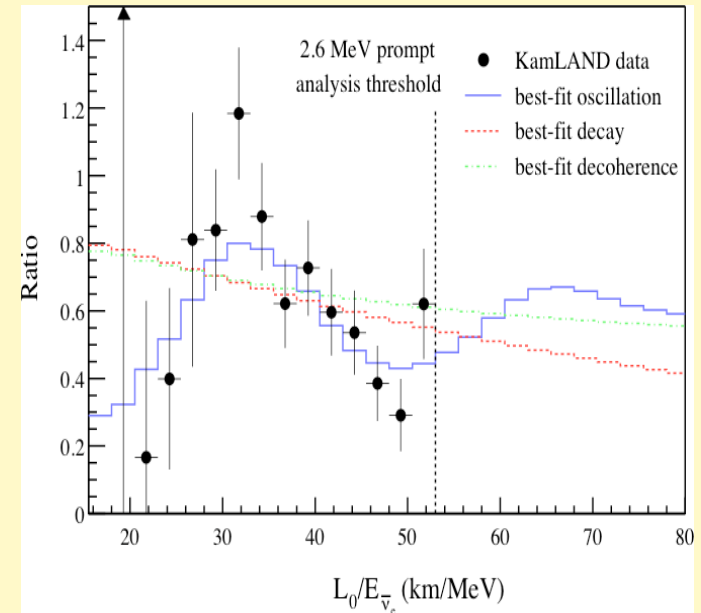


After SNO 2003

... in **2004** (KamLAND-II with revised background):
 unique Large Mixing Angle solution, and change to linear scales...

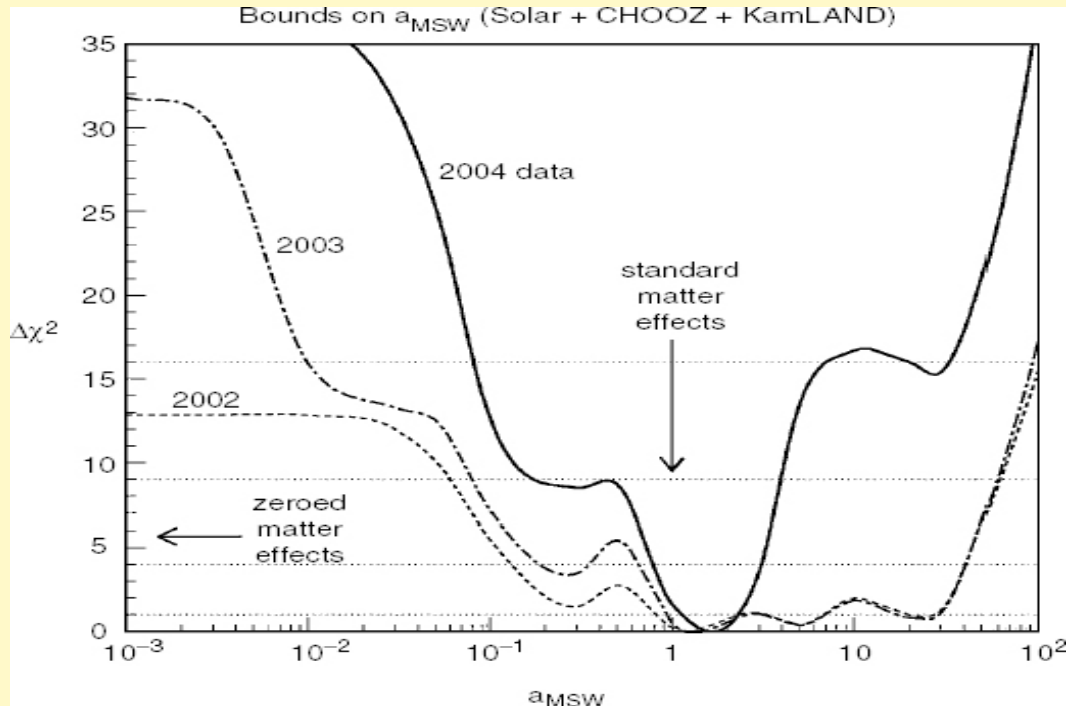


+ evidence for oscillatory effects
 in KamLAND reactor L/E spectrum



What about MSW effects?

- Exercise:** (1) Change MSW potential "by hand," $V \rightarrow a_{\text{MSW}}V$
 (2) Reanalyze all data with $(\delta m^2, \theta_{12}, a_{\text{MSW}})$ free
 (3) Project $(\delta m^2, \theta_{12})$ away and check if $a_{\text{MSW}} \sim 1$

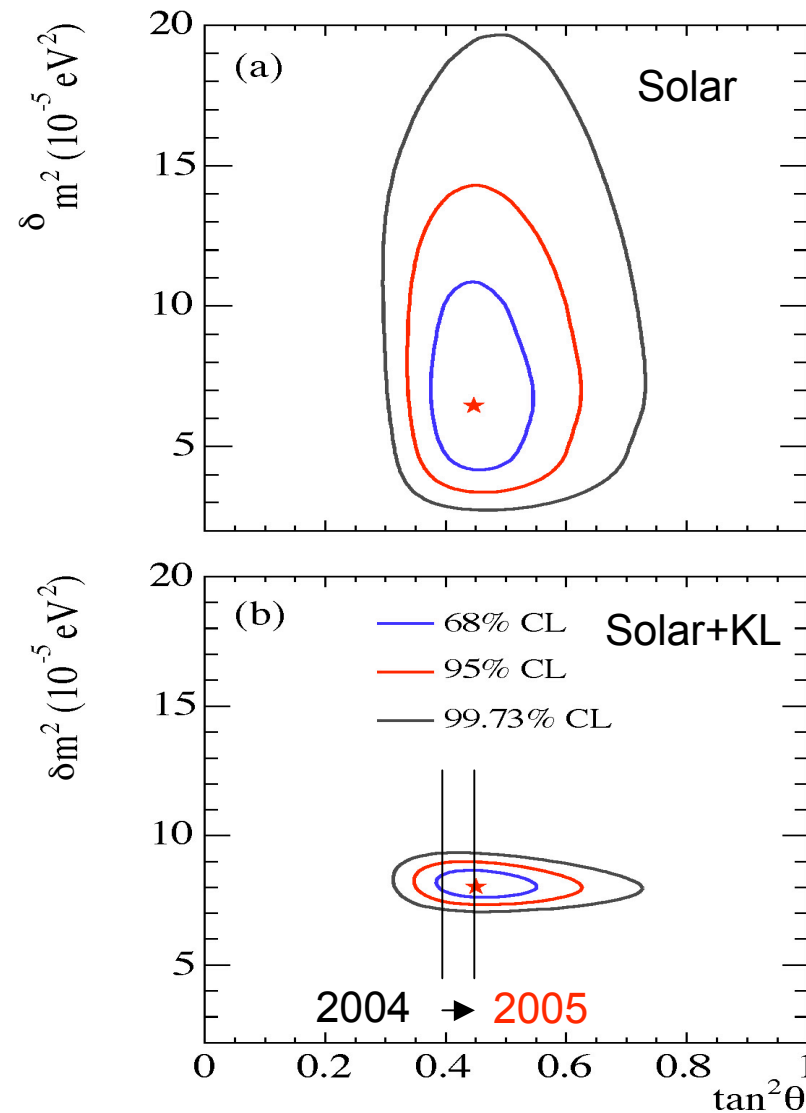


*(... a way of "measuring"
 G_F through solar
 neutrino oscillations ...)*

Results: with **2004** data, $a_{\text{MSW}} \sim 1$ confirmed within factor of ~ 2
 and $a_{\text{MSW}} \sim 0$ excluded \rightarrow **Evidence for standard MSW effects in the Sun**

But: expected subleading effect in the Earth (day-night difference) still below experimental uncertainties.

2005 (March): new data + detailed analysis from SNO

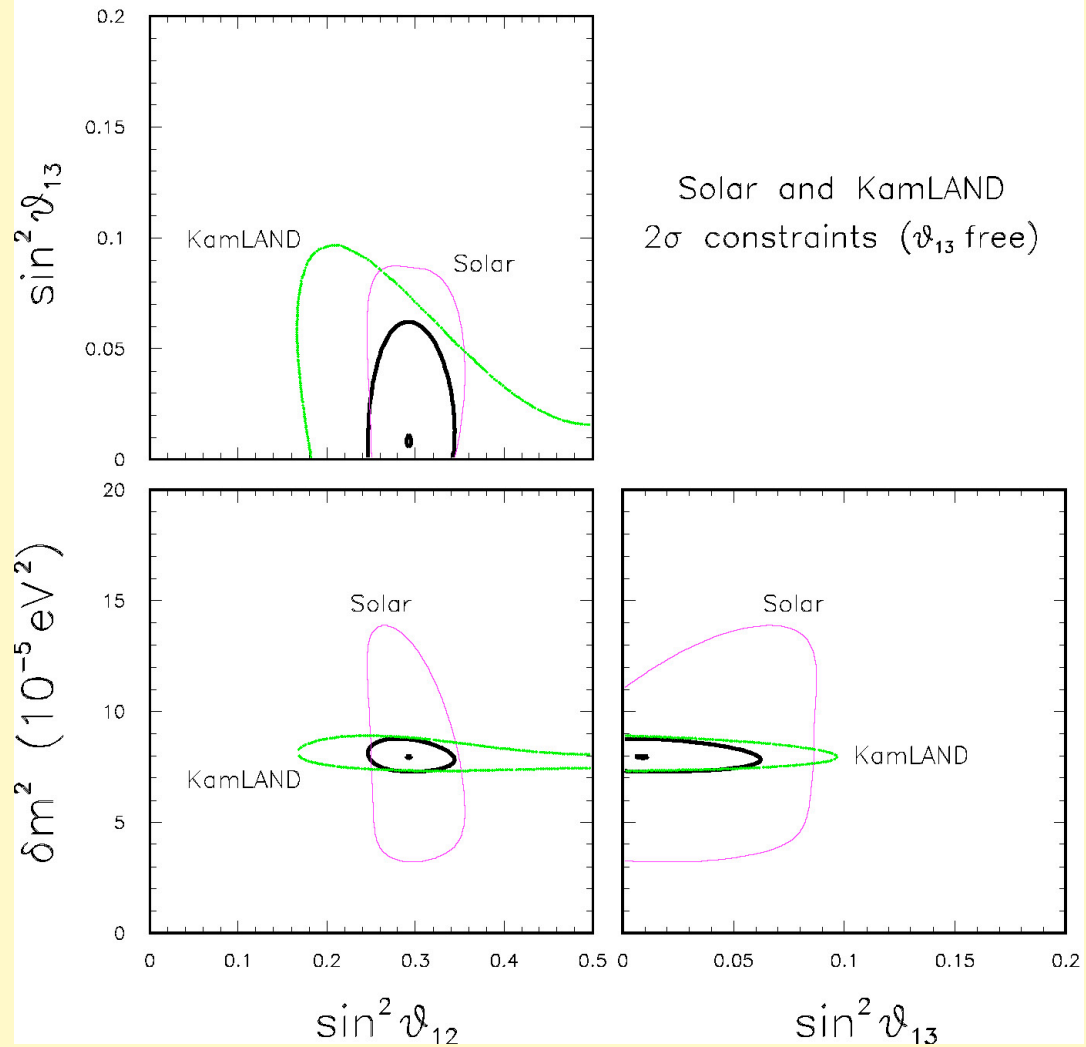


Previous results
basically confirmed

Slightly higher ratio
 $CC/NC \sim P(\nu_e \rightarrow \nu_e)$

Slight shift ($<1\sigma$ upwards)
of allowed range for θ_{12}

3ν analysis of 2004 solar+KamLAND data (θ_{13} free)



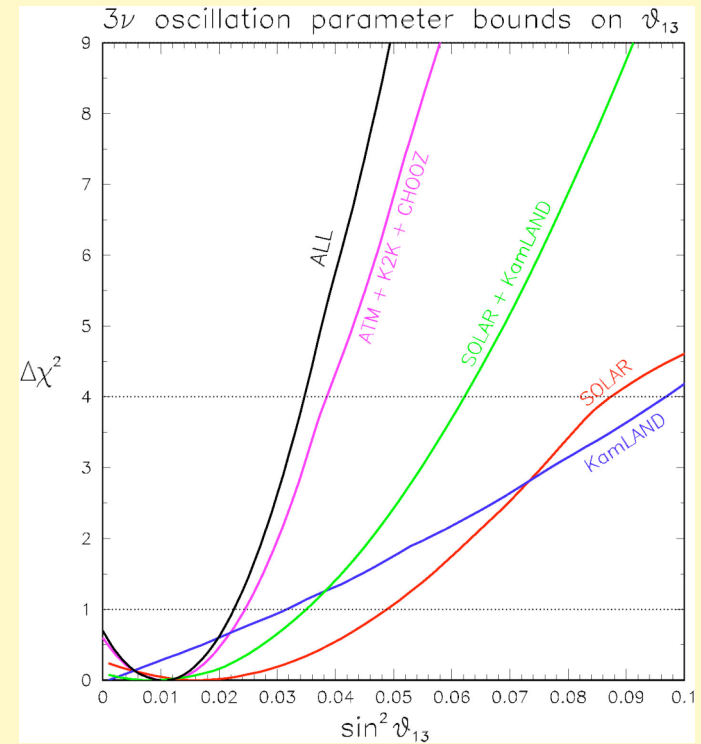
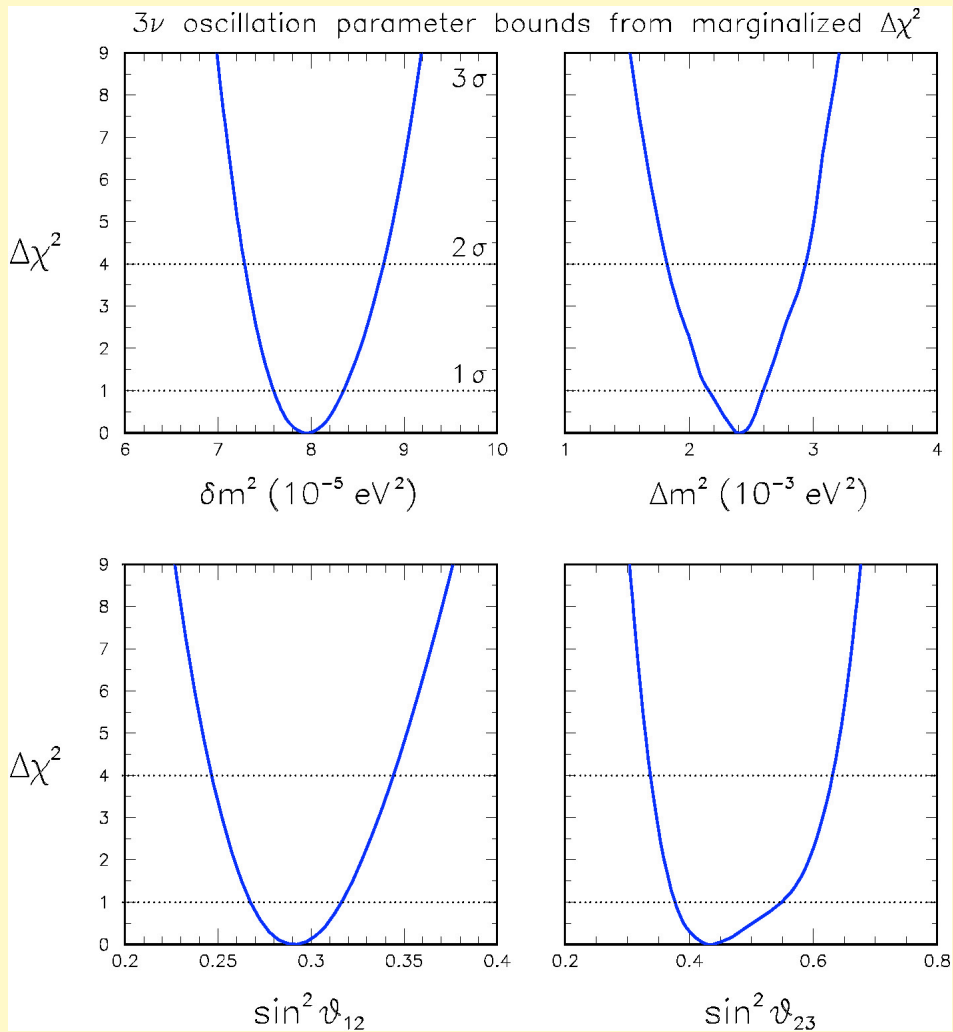
Solar and KamLAND
2σ constraints (ϑ_{13} free)

Solar and KamLAND data
also prefer $\theta_{13} \sim 0$ (nontrivial
consistency with SK+CHOOZ)

Bounds on $(\delta m^2, \theta_{12})$ not
significantly altered for
unconstrained θ_{13}

**"Grand Total" from global
analysis of oscillation data**

Marginalized $\Delta\chi^2$ curves for each parameter (2004)



Numerical $\pm 2\sigma$ ranges (95% CL for 1dof), 2004 data:

$$\delta m^2 \simeq 8.0_{-0.7}^{+0.8} \times 10^{-5} \text{ eV}^2$$

$$\Delta m^2 \simeq 2.4_{-0.6}^{+0.5} \times 10^{-3} \text{ eV}^2$$

$$\sin^2 \theta_{12} \simeq 0.29_{-0.04}^{+0.05} \quad (\text{SNO '05 : } 0.29 \rightarrow 0.31)$$

$$\sin^2 \theta_{23} \simeq 0.45_{-0.11}^{+0.18}$$

$$\sin^2 \theta_{13} < \sim 0.035$$

sign($\pm \Delta m^2$) : unknown

CP phase δ : unknown

Note: Precise values for θ_{12} and θ_{23} relevant for model building

**Probing absolute ν masses
through non-oscillation searches**

Three main tools (m_β , $m_{\beta\beta}$, Σ):

- 1) **β decay:** $m_i^2 \neq 0$ can affect spectrum endpoint. Sensitive to the "effective electron neutrino mass":

$$m_\beta = \left[c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2 \right]^{\frac{1}{2}}$$

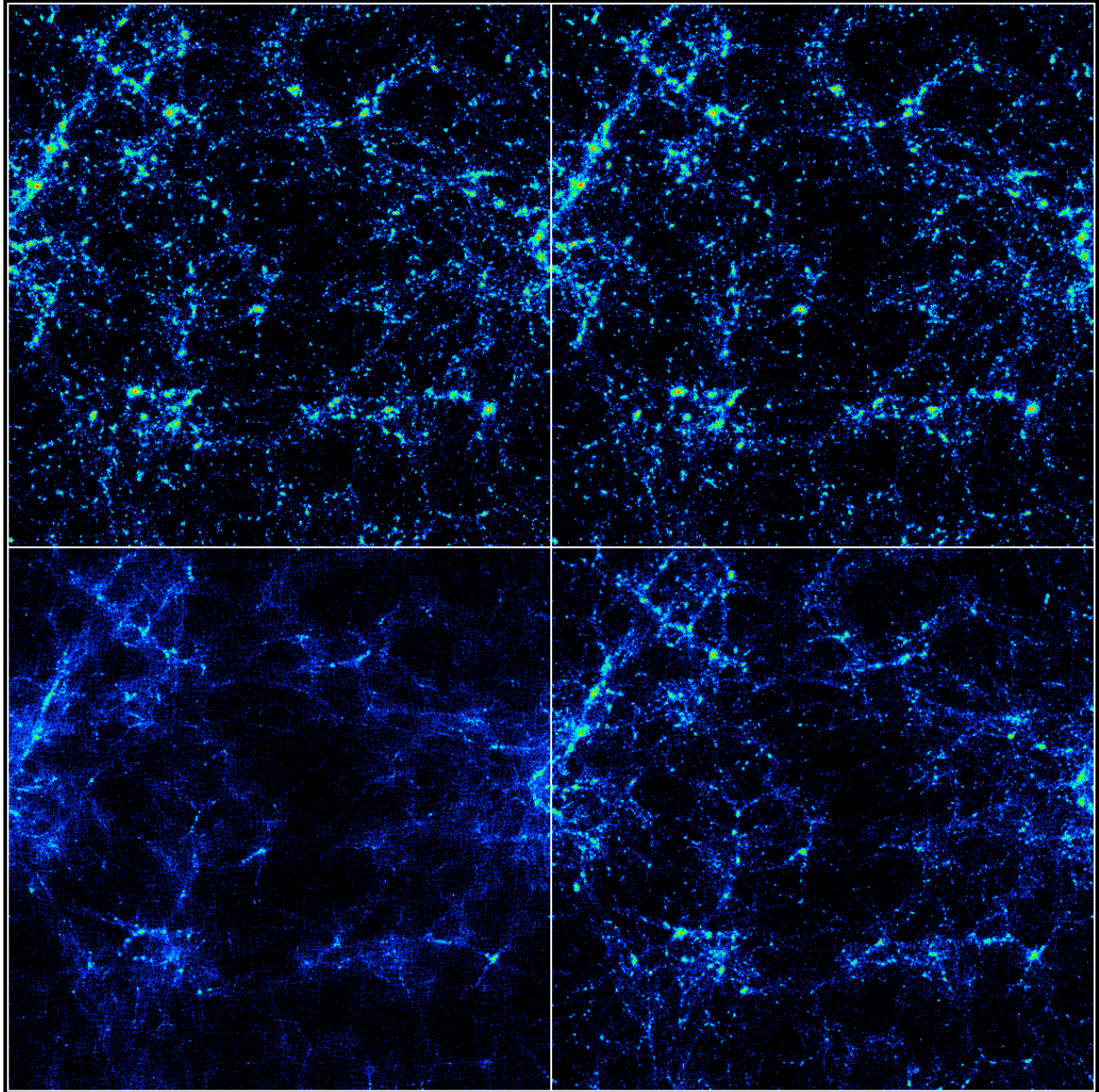
- 2) **$0\nu 2\beta$ decay:** Can occur if $m_i^2 \neq 0$ and $\nu = \bar{\nu}$. Sensitive to the "effective Majorana mass" (and phases):

$$m_{\beta\beta} = \left| c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3} \right|$$

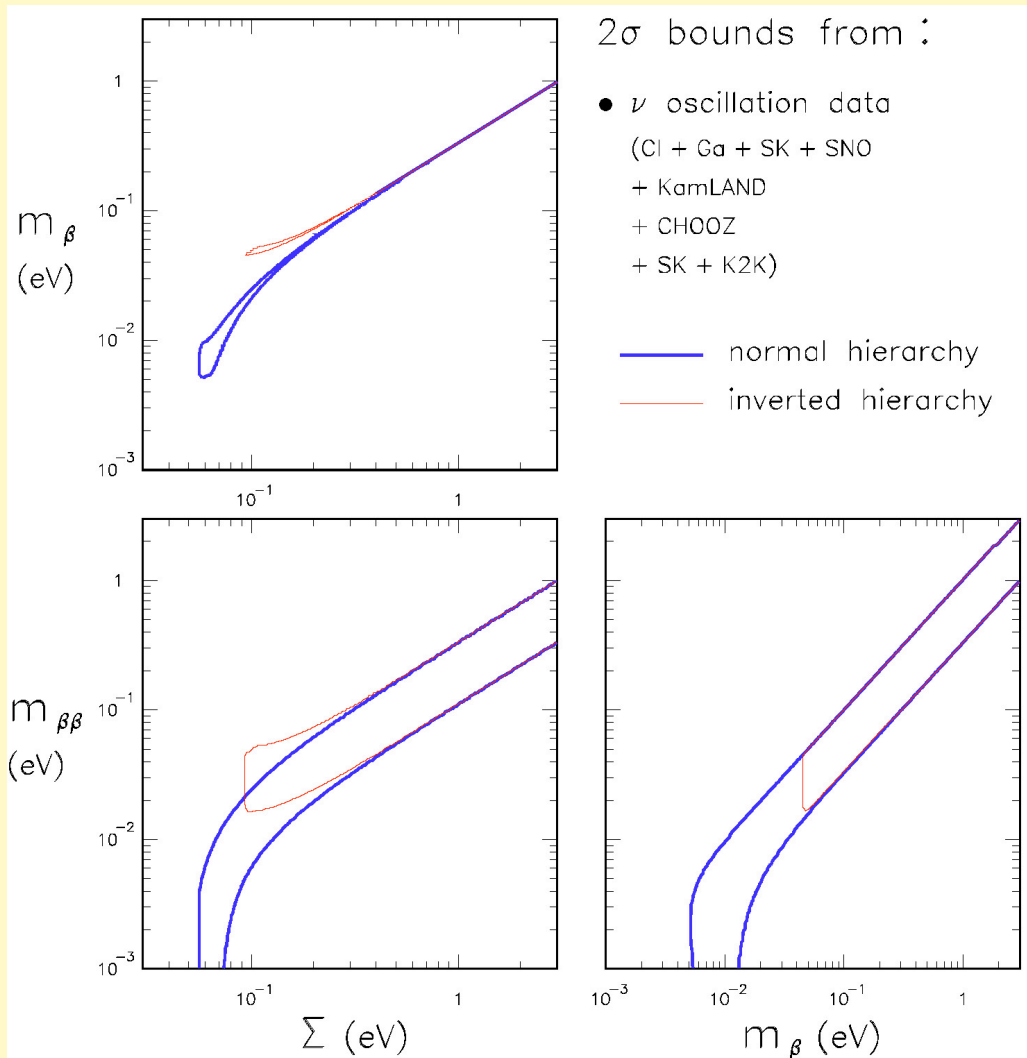
- 3) **Cosmology:** $m_i^2 \neq 0$ can affect large scale structures in (standard) cosmology constrained by CMB+other data. Probes:

$$\Sigma = m_1 + m_2 + m_3$$

$m_\nu =$ 0 1
7 4
eV



Even without non-oscillation data, the $(m_\beta, m_{\beta\beta}, \Sigma)$ parameter space is constrained by previous oscillation results:



Significant covariances

Partial overlap between
the two hierarchies

Large $m_{\beta\beta}$ spread due to
unknown Majorana phases

But we do have information from non-oscillation experiments:

1) β decay: no signal so far. Mainz & Troitsk expts: $m_\beta < O(eV)$

2) $0\nu 2\beta$ decay, no signal in all experiment, except in the most sensitive one (*Heidelberg-Moscow*). Rather debated claim.

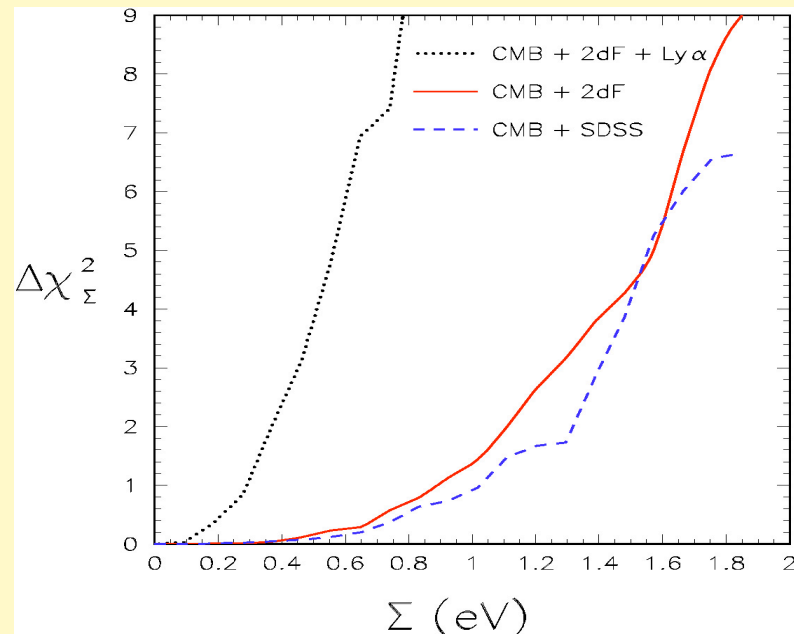
Claim accepted: $m_{\beta\beta}$ in sub-eV range (with large uncertainties)

Claim rejected: $m_{\beta\beta} < O(eV)$.

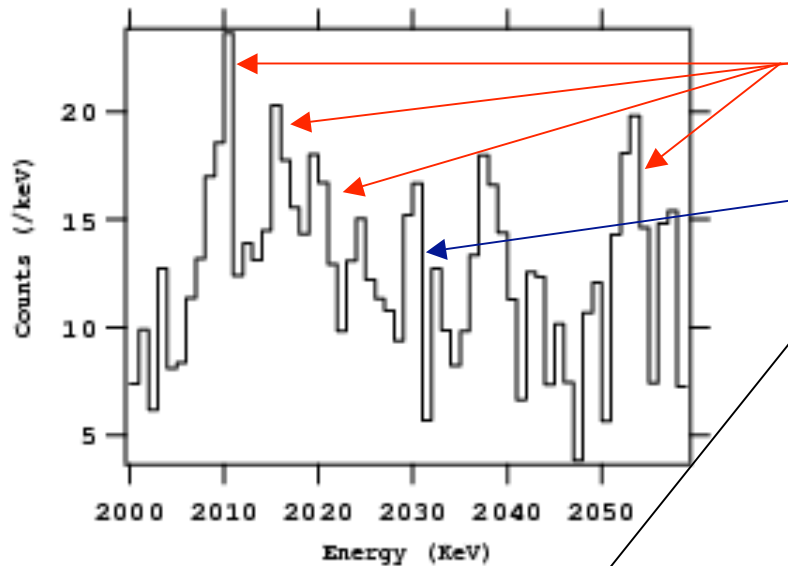
3) Cosmology. Upper bounds:

$\Sigma < eV/\text{sub-eV range}$,

depending on several inputs and priors. E.g.,



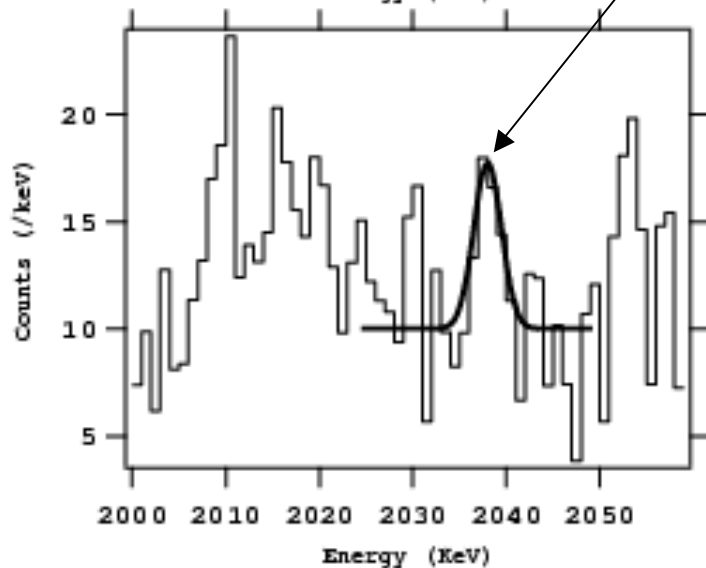
$0\nu 2\beta$ decay: Heidelberg-Moscow experiment final analysis (March 2004)



Four lines at 2010, 2017, 2022, 2053 keV are identified as due to ^{214}Bi decay

One possible line at 2030 keV is not identified

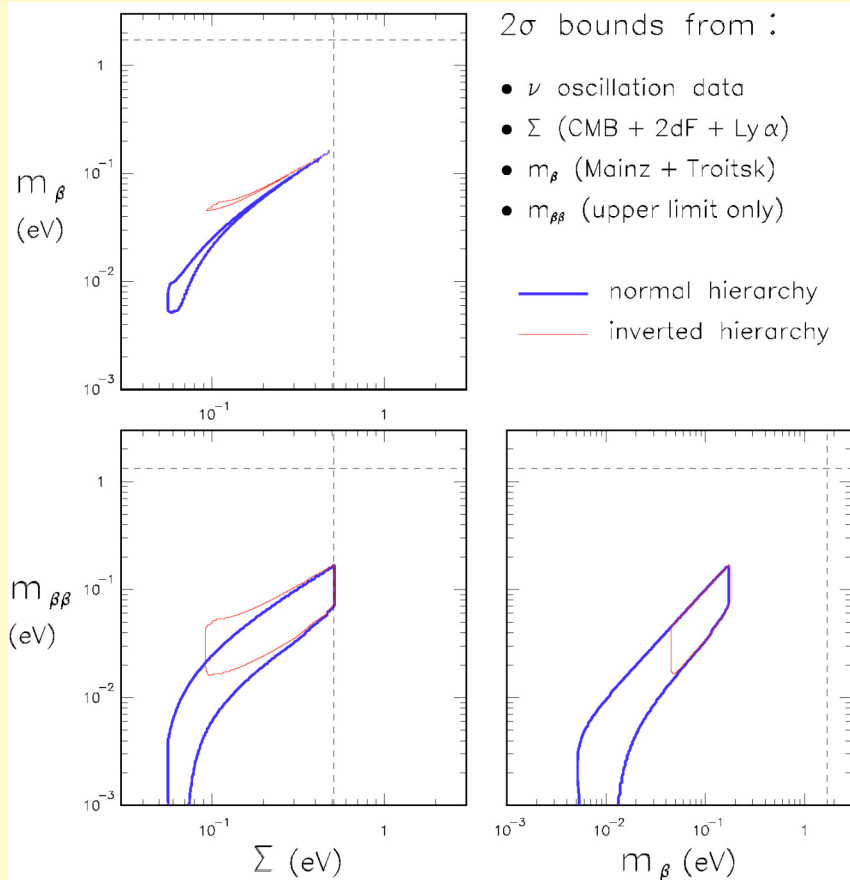
Claimed $0\nu\beta\beta$ line at ~ 2039 keV is now more clearly seen "by eye". Statistically, it emerges at about 4σ C.L. (~ 23 events)



We might have reached an "LSND-like" situation:

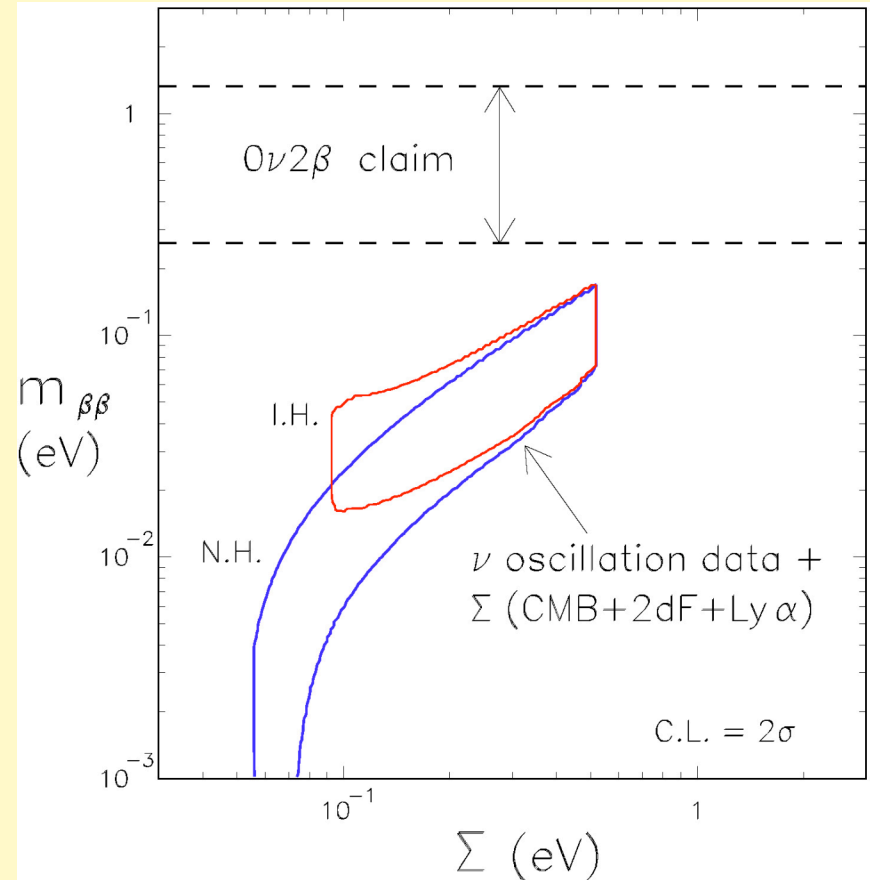
- Initial claim is rather controversial
- Then, further data/analysis strengthen it
- No current experiment can disprove it
- It will stay with us for a long time and will demand more sensitive expt. checks

$0\nu 2\beta$ claim rejected



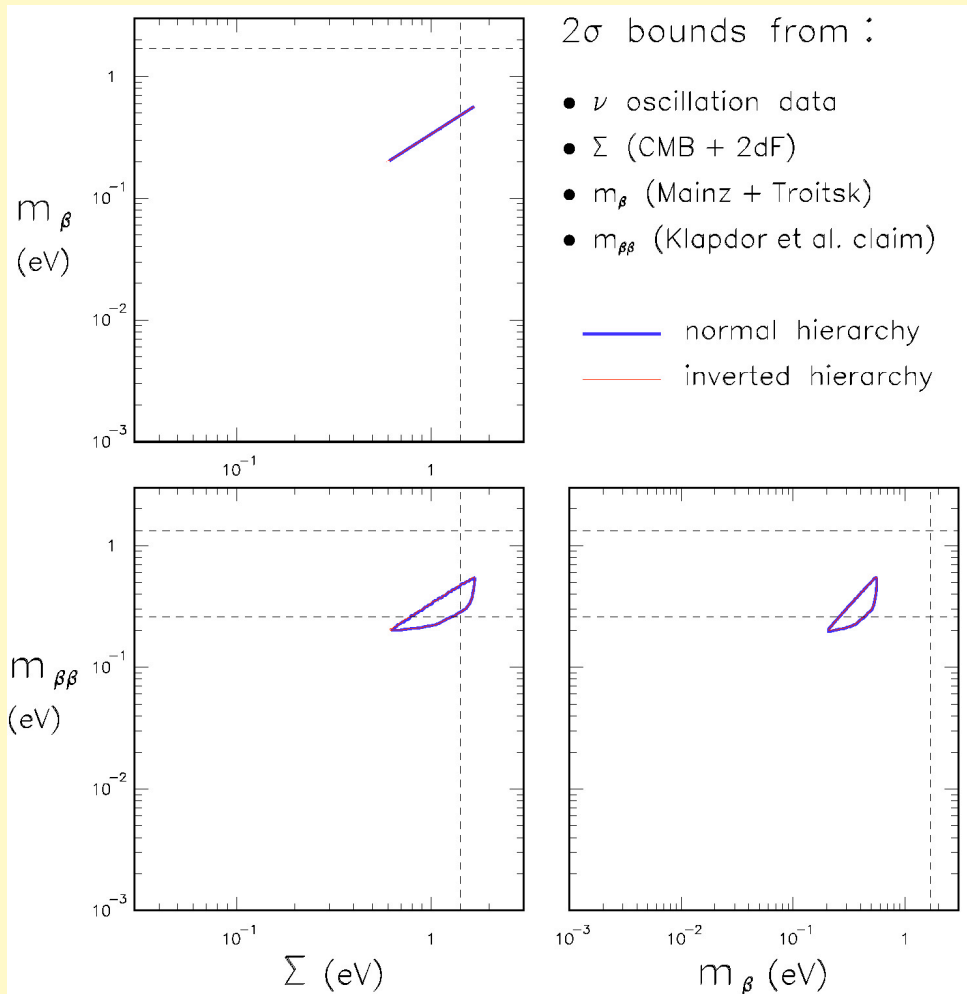
Cosmological bound dominates, but does not probe hierarchy yet

$0\nu 2\beta$ claim accepted



Tension with cosmological bound (no combination possible at face value)
But: too early to draw definite conclusions

E.g., if $0\nu 2\beta$ claim accepted & cosmological bounds relaxed:



Combination of all data
(osc+nonosc.) possible

Complete overlap of
the two hierarchies
(degenerate spectrum
with "large" masses)

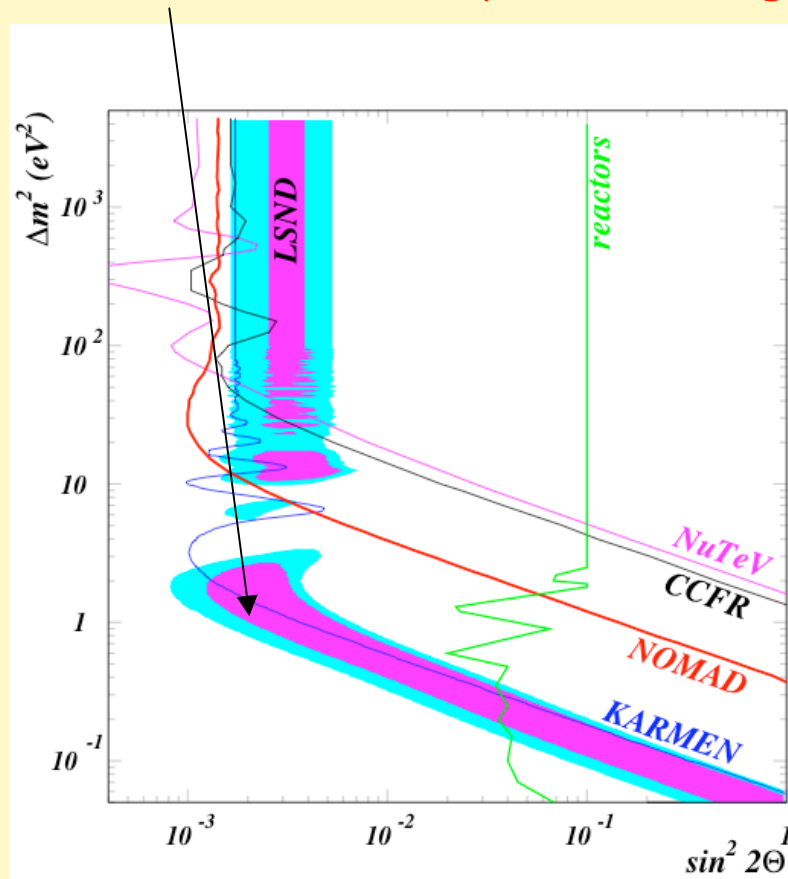
High discovery potential
in future (m_β , $m_{\beta\beta}$, Σ)
searches

Beyond three-neutrino mixing: LSND

Many theoretical reasons to go beyond the standard 3ν scenario

A purely experimental reason: the puzzling LSND oscillation claim

$\Delta M^2 \sim O(eV^2)$ with very small mixing?



Solutions invented so far (new sterile states, new interactions or properties) seem rather "ad hoc" and/or in poor agreement with world neutrino data

If MiniBoone confirms LSND this year (2005), many ideas will be revised, and neutrino schools > 2006 will really be fun!

Conclusions

Great
progress
in recent
years ...

Neutrino mass & mixing: established fact

Determination of $(\delta m^2, \theta_{12})$ and $(\Delta m^2, \theta_{23})$

Upper bounds on θ_{13}

Oscillation-induced spectral distortions

Direct evidence for solar ν flavor change

Evidence for matter effects in the Sun

Upper bounds on ν masses in (sub)eV range

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Determination of θ_{13}

Leptonic CP violation

Absolute m_ν from β -decay and cosmology

Test of $0\nu 2\beta$ claim and of Dirac/Majorana ν

Matter effects in the Earth

Normal vs inverted hierarchy

Beyond the standard 3ν scenario

Deeper theoretical understanding

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... and great
challenges
for the
future!